IMPERFECT MOBILITY OF LABOR ACROSS SECTORS AND FISCAL TRANSMISSION

TECHNICAL APPENDIX

NOT MEANT FOR PUBLICATION

Olivier CARDI, Peter CLAEYS, and Romain RESTOUT

- Section A presents the source and construction of the data used in the empirical and quantitative analysis, and empirical strategies to estimate the elasticity of substitution between traded and non traded goods and the elasticity of labor supply across sectors.
- Section B provides more VAR results and conduct a robustness check with respect to the classification of industries as tradables or non tradables, the exclusion of the public sector from aggregate and sectoral variables, the identifying assumption of government spending shocks.
- Section C provides more details about the interpretation of our empirical results and determines the conditions under which a government spending shock is biased toward non traded goods.
- Section D provides an elaborate investigation of the non tradable content of government spending shocks and the reactions of components of government consumption expenditure to a fiscal shock; this section also contrasts our results with those documented by earlier studies, conducts an investigation of the potential presence of anticipation effects, addresses a potential concern related to the fact that various VAR models could identify different structural government spending shocks, and deals with the potential endogeneity problem by using narratively identified government spending shocks from the dataset constructed by Guajardo, Leigh, and Pescatori [2014].
- Section E give more details on the model without physical capital accumulation, sets out the approach taken to solve the model, provides formal solutions for temporary fiscal shocks, investigates the effects of a rise in government consumption on non tradables and tradables as well, analyzes the role of the degree of labor mobility across sectors, and provides the main steps leading to equations in the main text of section 4.
- Section F gives more details on the model with physical capital accumulation, determines first-order conditions and sets out the approach taken to solve the model.
- In section G, we characterize graphically the initial steady-state and analyze the long-run effects of a temporary increase in government consumption.
- Section H provides the main steps leading to formal solutions following a temporary rise in government consumption in a continuous time setup.
- Section I considers a more general form for preferences by relaxing the assumption of separability in preferences in consumption and leisure.

- Section J introduces public debt in the setup.
- Section K lays out the same model except that we allow for the non traded sector to be imperfectly competitive and assume endogenous markups.
- Section L gives more details about the calibration of the model to data.
- Section M gives more numerical results. In this section, we explore the case of imperfect mobility of capital across sectors and we compare the theoretical responses from the baseline model with limited labor mobility and capital installation costs with those when one of these two features is shut down, together with the results from the VAR model. We also explore the case of endogenous markups and the implications of a rise in government spending which is debt-financed.

A Data Description

In this section, we present a complete description of our data set. First, we provide details on the data sources and variables construction used in the empirical analysis and to calibrate the model. Then, we describe empirical strategies to estimate two parameters involved in our quantitative analysis: the elasticity of substitution in consumption between traded and non traded goods, ϕ, and the degree of substitutability of hours worked across sectors, ϵ.

A.1 Data Description for Empirical Analysis

Coverage: Our sample consists of a panel of 16 countries: Australia (AUS), Austria (AUT), Belgium (BEL), Canada (CAN), Denmark (DNK), Finland (FIN), France (FRA), Ireland (IRL), Italy (ITA), Japan (JPN), the Netherlands (NLD), Norway (NOR), Spain (ESP), Sweden (SWE), the United Kingdom (GBR), and the United States (USA). The period is running from 1970 to 2007, with the exception of Japan (1974-2007) for which the starting date differs due to sectoral data availability. The choice of countries is restricted by the availability of sufficiently detailed data on sectoral variables over a long time horizon.

A.1.1 Data for Aggregate Variables: Source and Construction

Sources: All expenditure aggregates are obtained from the Economic Outlook Database provided by the Organisation for Economic Cooperation and Development [2017].

Series for aggregate variables are government final consumption expenditure (G), GDP (Y), total hours worked (L), the real consumption wage (W/CPI), private non-residential investment (I), and the current account-to-GDP ratio (CA). The database contains annual observations for the period running from 1970 to 2007 for the 16 OECD countries mentioned above. In the following, we provide details on data construction for aggregate variables (mnemonics are in parentheses):

- **Government spending**, G: real government final consumption expenditure (CGV). Source: OECD Economic Outlook Database.
- **Gross domestic product**, Y: real gross domestic product (GDPV). Source: OECD Economic Outlook Database.
- **Private investment**, JE: real private non-residential gross fixed capital formation (IBV). Source: OECD Economic Outlook Database.
- **Current account**, CA: ratio of the current account to the gross domestic product at current prices (CBGDPR). Source: OECD Economic Outlook Database.
- **Labor**, L: total hours worked by persons engaged (H_EMP). Sources: EU KLEMS and OECD STAN databases.
- **Real Consumption wage**, W/CPI: nominal wage divided by the consumer price index (CPI). Source: OECD Prices and Purchasing Power Parities for the consumer price index. The nominal wage is calculated by dividing labor compensation (LAB) by total hours worked by persons engaged (H_EMP). Sources: EU KLEMS and OECD STAN databases.

For government spending, GDP and investment, we directly use the volumes as reported by the OECD (the series are deflated with their own deflators). All quantity variables, with the exception of the current account, enter in the VAR models in log levels and scaled by the working age population (15-64 years old), while the real consumption wage rate is in natural log. The data source for the working age population is the OECD ALFS database.

A.1.2 Data for Sectoral Variables: Source and Construction

Sources: Our primary data sources are the OECD and EU KLEMS databases. We use the EU KLEMS [2011] sectoral database (the March 2011 data release, available at `http://www.euklems.net`) which provides for all countries of our sample with the exception of Canada and Norway annual data for eleven 1-digit ISIC-rev.3 industries. For Canada and Norway, sectoral data are taken from the Structural Analysis (STAN) database provided by the OECD [2011].

The eleven 1-digit ISIC-rev.3 industries are classified as tradables or non tradables. To do so, we adopt the classification proposed by De Gregorio et al. [1994] who treat an industry as traded when it exports at least 10% of its output. Following Jensen and Kletzer [2006], we have updated the classification suggested by De Gregorio et al. [1994] by treating "Financial Intermediation" as a traded industry. Jensen and Kletzer [2006] use the geographic concentration of service activities within the United States to identify which service activities are traded domestically. The authors classify activities that are traded domestically as potentially traded internationally. The idea is that when a good or a service is traded, the production of the activity is concentrated in a particular region to take advantage of economies of scale in production.

Jensen and Kletzer [2006] use the two-digit NAICS (North American Industrial Classification System) to identify tradable and non tradable sectors. We map their classification into the NACE-ISIC-rev.3 used by the EU KLEMS and STAN databases. The mapping was clear for all sectors except for "Real Estate, Renting and Business Services". According to the EU KLEMS/STAN classification, the industry labelled "Real Estate, Renting and Business Services" is an aggregate of five sub-industries: "Real estate activities" (NACE code: 70), "Renting of Machinery and Equipment" (71), "Computer and Related Activities" (72), "Research and Development" (73) and "Other Business Activities" (74). While Jensen and Kletzer [2006] find that industries 70 and 71 can be classified as tradable, they do not provide information for industries 72, 73 and 74. We decided to classify "Real Estate, Renting and Business Services" as non tradable but conduct a robustness check by contrasting our empirical findings when "Real Estate, Renting and Business Services" is non traded with those when "Real Estate, Renting and Business Services" is traded. As shown in section B.2, our conclusions hold and remain unsensitive to the classification. We construct traded and non traded sectors as follows (EU KLEMS codes are given in parentheses):

- **Traded Sector**: "Agriculture, Hunting, Forestry and Fishing" (AtB), "Mining and Quarrying" (C), "Total Manufacturing" (D), "Transport, Storage and Communication" (I) and "Financial Intermediation" (J).
- **Non Traded Sector**: "Electricity, Gas and Water Supply" (E), "Construction" (F), "Wholesale and Retail Trade" (G), "Hotels and Restaurants" (H), "Real Estate, Renting and Business Services" (K) and "Community Social and Personal Services" (LtQ).

Once industries have been classified as tradables or non tradables, for any macroeconomic variable X, its sectoral counterpart X^j for $j = T, N$ is constructed by adding the X_k of all sub-industries k classified in sector $j = T, N$ as follows $X^j = \sum_{k \in j} X_k$.

Relevant to our work, EU KLEMS and OECD STAN database provide data, for each industry and year, on value added at current and constant prices, thus allowing us to construct series for sectoral value added deflators; the database also provide details on labor compensation and employment data, allowing the construction for sectoral wage rates. In the VAR models, with the exception of the current account, all quantity variables are in log levels and scaled by the working age population (15-64 years old), while price deflators and wage rates are in natural logs. Source: OECD ALFS Database for the working age population. We detail below the construction of sectoral data employed in section 2 (mnemonics are given in parentheses):

- **Sectoral output**, Y^j: sectoral value added at constant prices in sector $j = T, N$ (VA_QI). Sources: EU KLEMS and OECD STAN databases.
- **Relative output**, Y^T/Y^N: ratio of traded value added at constant prices to non traded value added at constant prices.
- **Sectoral output share**, $\nu^{Y,j}$: ratio of value added at constant prices in sector j to GDP at constant prices, i.e., $Y^j/(Y^T + Y^N)$ for $j = T, N$.
- **Relative price of non tradables**, P: ratio of the non traded value added deflator to the traded value added deflator, i.e., $P = P^N/P^T$. The sectoral value added deflator P^j for sector $j = T, N$ is calculated by dividing value added at current prices (VA) by value added at constant prices (VA_QI) in sector j. Sources: EU KLEMS and OECD STAN databases.
- **Sectoral labor**, L^j: total hours worked by persons engaged in sector j (H_EMP). Sources: EU KLEMS and OECD STAN databases.
- **Relative labor**, L^T/L^N: ratio of hours worked in the traded sector to hours worked in the non traded sector.
- **Sectoral labor share**, $\nu^{L,j}$: ratio of hours worked in sector j to total hours worked, i.e., $L^j/(L^T + L^N)$ for $j = T, N$.
- **Sectoral real consumption wage**, W^j/CPI: nominal wage in sector j divided by the consumer price index (CPI). Source: OECD Prices and Purchasing Power Parities for the consumer price index. The sectoral nominal wage W^j for sector $j = T, N$ is calculated by dividing labor compensation in sector j (LAB) by total hours worked by persons engaged (H_EMP) in that sector. Sources: EU KLEMS and OECD STAN databases.
- **Relative wage**, Ω: ratio of the nominal wage in the non traded sector W^N to the nominal wage in the traded sector W^T, i.e., $\Omega = W^N/W^T$.

- **Labor reallocation index**, LR: measures the fraction of workers who are working in year t in a different sector than in year $t-2$ and is computed as:

$$LR_t(2) = 0.5 \sum_{j=T}^{N} \left| \frac{L_t^j}{\sum_{j=T}^{N} L_t^j} - \frac{L_{t-2}^j}{\sum_{j=T}^{N} L_{t-2}^j} \right|.$$

Data for labor (H_EMP) are taken from EU KLEMS and STAN databases.

A.2 Data Description for Calibration

In the numerical analysis, we calibrate a set of parameters by choosing them so that the initial steady-state of the model matches key empirical properties of a representative OECD economy. In particular, we pay attention to the adequacy of the non tradable content of the model to the data. This section gives information on our estimates of the non tradable content of GDP, consumption, investment, government spending, labor and labor compensation. In addition, it gives information about the share of government spending on traded and non traded goods in the corresponding sectoral value added and the labor income shares in sector $j = T, N$.

Our sample covers the 16 OECD countries mentioned in section A.1. In the following, statistics for the sample as a whole represent (unweighted) averages of the corresponding variables among the group. Our reference period for the calibration corresponds to the period 1990-2007. The choice of this period has been dictated by data availability. In the following, we provide details on data construction for non tradable shares:

- **Output, labor and labor compensation**: we split the eleven industries into traded and non traded sectors by adopting the classification proposed by De Gregorio et al. [1994] and updated by Jensen and Kletzer [2006]. Details about data construction for output and labor are provided in Section A.1.2. We calculate the non tradable share of labor compensation as the ratio of labor compensation of non tradables, i.e., $W^N L^N$, to overall labor compensation, i.e., WL. Sources: EU KLEMS [2011] and STAN databases. Data coverage: 1990-2007 for all countries.
- **Consumption**: to split consumption expenditure (at current prices) into consumption in traded and non traded goods, we made use of the Classification of Individual Consumption by Purpose (COICOP) published by the United Nations (Source: United Nations [2011]). Among the twelve items, the following ones are treated as consumption in traded goods: "Food and Non-Alcoholic Beverages", "Alcoholic Beverages Tobacco and Narcotics", "Clothing and Footwear", "Furnishings, Household Equipment" and "Transport". The remaining items are treated as consumption in non traded goods: "Housing, Water, Electricity, Gas and Fuels", "Health", "Communication", "Recreation and Culture", "Education", "Restaurants and Hotels". Because the item "Miscellaneous Goods and Services" is somewhat problematic, we decided to consider it as both tradable (50%) and non tradable (50%) with equal shares. Data coverage: 1990-2007 for AUS, AUT, CAN, DNK, FIN, FRA, GBR, ITA, JPN, NLD, NOR and USA, 1993-2007 for SWE and 1995-2007 for BEL, ESP and IRL.
- **Investment**: to map investment expenditure (at current prices) into expenditures on tradables and non tradables, we follow the classification proposed by Burstein et al. [2004], we consider "Housing", "Other Constructions" and "Other Products" as non tradable investment and "Products of Agriculture, Forestry, Fisheries and Aquaculture", "Metal Products and Machinery", "Transport Equipment" as tradable investment expenditure. Source: OECD Input-Output database [2012]. Data coverage: 1990-2007 for AUT, CAN, ESP, FIN, GBR, IRL, JPN, NLD, and NOR, 1990-2006 for DNK, FRA, ITA and USA, and 1993-2007 for SWE. Data are not available for AUS and BEL. Thus, for these two countries, when we calibrate the model to each OECD country, we target a non tradable content of investment expenditure that is given by the unweighed average, i.e., 0.64.
- **Government spending**: Sectoral government final consumption expenditure data (at current prices) were obtained from the OECD General Government Accounts database (Source: COFOG, OECD [2017]). "Economic Affairs" which includes "Fuel and Energy", "Agriculture, Forestry, Fishing, and Hunting", "Mining, Manufacturing, and Construction", "Transport and Communications" is classified as tradable. Items treated as non traded are: "General Public Services", "Defense", "Public Order and Safety", "Environment Protection", "Housing and Community Amenities", "Health", "Recreation, Culture and Religion", "Education", "Social Protection". Data coverage: 1995-2007 for AUT, BEL, DNK, ESP, FRA, GBR, IRL, ITA, NLD, NOR and SWE, 1998-2007 for AUS, 1990-2007 for FIN, 2005-2007 for JPN and 1970-2007 for the USA. Data are not available for CAN. Thus, for this country, when we calibrate the model to each OECD country, we choose a non tradable content of government expenditure that is given by the unweighed average, i.e., 0.90.

Next, the labor income share for sector $j = T, N$, denoted by θ^j, is calculated as the ratio of labor compensation in sector j (LAB) to value added at current prices (VA_QI) in that sector, i.e., $\theta^j = (W^j L^j)/(P^j Y^j)$. Sources: EU KLEMS [2011] and STAN databases. Data coverage: 1990-2007 for all countries.

Finally, we approximate technological change in sector j with labor productivity in this sector which we measure by dividing the value added at constant prices in sector j (VA_QI) by total hours worked by persons engaged (H_EMP) in this sector, i.e., $Z^j = Y^j/L^j$. The relative productivity, Z^T/Z^N, is calculated as the ratio of labor productivity of tradables, Z^T, to labor productivity of non tradables, Z^N. Sources: EU KLEMS [2011] and STAN databases. Data coverage: 1990-2007 for all countries.

Because data source and construction are heterogenous across variables as a result of different nomenclatures, Table 6 provides a summary of the classification adopted to split value added and its demand components as well intro traded and non traded goods.

A.3 Estimates of ϕ: Empirical Strategy

In this section, we detail our empirical strategy to estimate the elasticity of substitution between traded and non traded goods ϕ. Estimates of the elasticity of substitution ϕ by the existing literature are rather diverse. The cross-section studies report an estimate of ϕ ranging from 0.44 to 0.74, see e.g., Stockman and Tesar [1995] and Mendoza [1995], respectively.[59] The literature adopting the Generalized Method of Moments and the cointegration methods, see e.g. Ostry and Reinhart [1992] and Cashin and Mc Dermott [2003], respectively, reports a value in the range $[0.75, 1.50]$ for developing countries and in the range $[0.63, 3.50]$ for developed countries. Since estimates for ϕ display a sharp dispersion across empirical studies, we conduct an empirical analysis in order to estimate this parameter for each country in our sample.

A.3.1 Empirical Strategy

Using Time Series by Industry Taken from EU KLEMS and STAN

To estimate ϕ, we adopt the following strategy. To determine an empirical relationship, we combine the optimal rule for intra-temporal allocation of consumption (14) (that we repeat for clarity purposes)

$$\frac{C^T}{C^N} = \left(\frac{\varphi}{1-\varphi}\right) P^{\phi}. \tag{47}$$

with the goods market equilibrium

$$\frac{C^T}{C^N} = \frac{Y^T - NX - G^T - I^T}{Y^N - G^N - I^N}, \tag{48}$$

where we used the fact that $\dot{B} - r^{\star} B = Y^T - C^T - G^T - I^T \equiv NX$. Inserting (47) into (48) leads to

$$\frac{Y^T - NX - G^T - I^T}{Y^N - G^N - I^N} = \left(\frac{\varphi}{1-\varphi}\right) P^{\phi}. \tag{49}$$

According to the market clearing condition, we could alternatively use data for consumption or for sectoral value added along with times series for its demand components to estimate ϕ. Unfortunately, nomenclatures for valued added by industry and for consumption by items are different and thus it is most likely that C^T differs from $Y^T - NX - G^T - I^T$, and C^N from $Y^N - G^N - I^N$ as well. Because time series for traded and non traded consumption display a short time horizon for half countries of our sample while data for sectoral value added and net exports are available for the 16 OECD countries of our sample over the period running from 1970 to 2007 (except for Japan: 1974-2007), we find appropriate to estimate ϕ by computing $Y^T - NX - G^T - I^T$ and $Y^N - G^N - I^N$. Yet, an additional difficulty shows up because the classification adopted to split government spending and investment expenditure into traded and non traded items is different from that adopted to break down

[59] While the sample used by Stockman and Tesar [1995] covers 30 countries (including 17 developing and 13 industrialized), Mendoza [1995] uses exactly the same data set in his estimation but includes only the 13 industrialized countries. Note that the estimate of ϕ has been obtained by using the cross sectional dataset by Kravis, Heston and Summers for the year 1975.

Table 6: Construction of Variables and Data Sources

Variable	Countries covered	Period	Construction and aggregation
Value added Y^T & Y^N (constant prices)	AUS, AUT, BEL, CAN, DNK, ESP, FIN, FRA, GBR, IRL, ITA, JPN, NLD, NOR, SWE, USA	1970-2007 (JPN: 74-07)	T: Agriculture, Mining, Manufacturing, Transport, Finance Intermediation N: Electricity, Construction, Trade, Hotels, Real Estate, Personal Services
Value added P^TY^T & P^NY^N (current prices)	AUS, AUT, BEL, CAN, DNK, ESP, FIN, FRA, GBR, IRL, ITA, JPN, NLD, NOR, SWE, USA	1970-2007 (JPN: 74-07)	T: Agriculture, Mining, Manufacturing, Transport, Finance Intermediation N: Electricity, Construction, Trade, Hotels, Real Estate, Personal Services
Labor L^T & L^N (total hours worked by persons engaged)	AUS, AUT, BEL, CAN, DNK, ESP, FIN, FRA, GBR, IRL, ITA, JPN, NLD, NOR, SWE, USA	1970-2007 (JPN: 74-07)	T: Agriculture, Mining, Manufacturing, Transport, Finance Intermediation N: Electricity, Construction, Trade, Hotels, Real Estate, Personal Services
Labor compensation LAB^T & LAB^N (current prices)	AUS, AUT, BEL, CAN, DNK, ESP, FIN, FRA, GBR, IRL, ITA, JPN, NLD, NOR, SWE, USA	1970-2007 (JPN: 74-07)	T: Agriculture, Mining, Manufacturing, Transport, Finance Intermediation N: Electricity, Construction, Trade, Hotels, Real Estate, Personal Services
Price P^T & P^N (value added deflator)	AUS, AUT, BEL, CAN, DNK, ESP, FIN, FRA, GBR, IRL, ITA, JPN, NLD, NOR, SWE, USA	1970-2007 (JPN: 74-07)	Value added at current prices (P^jY^j) over value added at constant prices (Y^j)
Relative Price P (index 1995=100)	AUS, AUT, BEL, CAN, DNK, ESP, FIN, FRA, GBR, IRL, ITA, JPN, NLD, NOR, SWE, USA	1970-2007 (JPN: 74-07)	Value added deflator of non traded goods (P^N) over value added deflator of traded goods (P^T)
Wage W^T & W^N (nominal and per hour)	AUS, AUT, BEL, CAN, DNK, ESP, FIN, FRA, GBR, IRL, ITA, JPN, NLD, NOR, SWE, USA	1970-2007 (JPN: 74-07)	Labor compensation (LAB^j) over total hours worked by persons engaged (L^j)
Wage W (nominal and per hour)	AUS, AUT, BEL, CAN, DNK, ESP, FIN, FRA, GBR, IRL, ITA, JPN, NLD, NOR, SWE, USA	1970-2007 (JPN: 74-07)	Labor compensation (LAB) over total hours worked by persons engaged (L)
Wage W^T/CPI & W^N/CPI (real and per hour)	AUS, AUT, BEL, CAN, ESP, DNK, FIN, FRA, GBR, IRL, ITA, JPN, NLD, NOR, SWE, USA	1970-2007 (JPN: 74-07)	Nominal wage (W^j) divided by the consumer price index (CPI)
Wage W/CPI (real and per hour)	AUS, AUT, BEL, CAN, DNK, ESP, FIN, FRA, GBR, IRL, ITA, JPN, NLD, NOR, SWE, USA	1970-2007 (JPN: 74-07)	Nominal wage (W) divided by the consumer price index (CPI)
Relative Wage Ω (index 1995=100)	AUS, AUT, BEL, CAN, DNK, ESP, FIN, FRA, GBR, IRL, ITA, JPN, NLD, NOR, SWE, USA	1970-2007 (JPN: 74-07)	Nominal wage in non tradables (W^N) over nominal wage in tradables (W^T)
Relative Productivity Z^T/Z^N	AUS, AUT, BEL, CAN, DNK, ESP, FIN, FRA, GBR, IRL, ITA, JPN, NLD, NOR, SWE, USA	1970-2007 (JPN: 74-07)	Real labor productivity in tradables (Z^T) over real labor productivity in non tradables (Z^N). Z^j is calculated as $Z^j = Y^j/L^j$
Labor Reallocation Index LR	AUS, AUT, BEL, CAN, DNK, ESP, FIN, FRA, GBR, IRL, ITA, JPN, NLD, NOR, SWE, USA	1972-2007 (JPN: 76-07)	Fraction of workers who in year t are working in a different sector than in year $t-2$. Computed from Kambourov [2009]
Consumer Price Index CPI (index 1995=100)	AUS, AUT, BEL, CAN, DNK, ESP, FIN, FRA, GBR, IRL , ITA, JPN, NLD, NOR, SWE, USA	1970-2007 (IRL: 76-07)	Consumer prices, all items index
Government spending G (constant prices)	AUS, AUT, BEL, CAN, DNK, ESP, FIN, FRA, GBR, IRL, ITA, JPN, NLD, NOR, SWE, USA	1970-2007	Log of real per capita government final consumption expenditure (CGV) Population is working age population (15-64 years old), source: OECD
Gross domestic product Y (constant prices)	AUS, AUT, BEL, CAN, DNK, ESP, FIN, FRA, GBR, IRL, ITA, JPN, NLD, NOR, SWE, USA	1970-2007	Log of real per capita gross domestic product (GDPV)
Private investment I (constant prices)	AUS, AUT, BEL, CAN, DNK, ESP, FIN, FRA, GBR, IRL, ITA, JPN, NLD, NOR, SWE, USA	1970-2007	Log of real per capita private non-residential gross fixed capital formation (IBV)
Current account CA (in % of GDP)	AUS (70-07), AUT (70-07), BEL (75-07), CAN (70-07), DNK (88-07), ESP (75-07), FIN (75-07), FRA (73-07), GBR (70-07), IRL (90-07), ITA (71-07), JPN (70-07), NLD (70-07), NOR (75-07), SWE (75-07), USA (70-07)		Ratio of the current account balance to the gross domestic product at current prices (CBGDPR)
Investment P^TI^T & P^NI^N (current prices)	AUT (76-07), CAN (70-07), DNK (70-06), ESP (80-07), FIN (70-07), FRA (78-06), GBR (70-07), IRL (90-07), ITA (70-06), JPN (80-07), NLD (70-07), NOR (70-07), SWE (93-07), USA (77-06)		T: Products of Agriculture, Machinery, Transport N: Housing, Other Constructions, Other Products
Consumption P^TC^T & P^NC^N (current prices)	AUS (70-07), AUT (76-07), BEL (95-07), CAN (70-07), DNK (70-07), ESP (95-07), FIN (75-07), FRA (70-07), GBR (90-07), IRL (95-07), ITA (70-07), JPN (80-07), NLD (80-07), NOR (70-07), SWE (93-07), USA (70-07)		T: Food, Beverages, Clothing, Furnishings, Transport, Other N: Housing, Health, Communication, Recreation, Education, Restaurants and Other (Other is defined as 50% tradable and 50% non tradable)
Government spending P^TG^T & P^NG^N (current prices)	AUS (98-07), AUT (95-07), BEL (95-07), CAN (95-07), DNK (95-07), ESP (95-07), FIN (90-07), FRA (95-07), GBR (95-07), IRL (95-07), ITA (95-07), JPN (05-07), NLD (95-07) NOR (90-07), SWE (95-07), USA (70-07)		T: Economic Affairs N: General Public Services, Defense, Public Order and Safety, Environment Protection, Housing and Communi Health, Recreation, Culture and Religion, Education, Social Protection

Notes: times series for P^TI^T & P^NI^N are not available for AUS and BEL together with P^TG^T & P^NG^N for CAN.

value added into traded and non traded components. Moreover, the time horizon is short at a disaggregated level (for I^j and G^j) for most of the countries, especially for time series of G^j. To overcome these difficulties, we proceed as follows. Denoting by $\upsilon_{G^T} = \frac{P^T G^T}{P^T Y^T - P^T NX}$ and $\upsilon_{I^T} = \frac{P^T I^T}{P^T Y^T - P^T NX}$ the ratio of government and investment expenditure on tradables to traded value added adjusted with net exports at current prices, respectively, and by $\upsilon_{G^N} = \frac{P^N G^N}{P^N Y^N}$ and $\upsilon_{I^N} = \frac{P^N I^N}{P^N Y^N}$ the ratio of government and investment expenditure on non tradables to non traded value added at current prices, the goods market equilibrium can be rewritten as follows:

$$\frac{\left(P^T Y^T - P^T NX\right)\left(1 - \upsilon_{G^T} - \upsilon_{I^T}\right)}{P^N Y^N \left(1 - \upsilon_{G^N} - \upsilon_{I^N}\right)} = \left(\frac{\varphi}{1-\varphi}\right) P^{\phi - 1},$$

or alternatively

$$\frac{\left(Y^T - NX\right)\left(1 - \upsilon_{G^T} - \upsilon_{I^T}\right)}{Y^N \left(1 - \upsilon_{G^N} - \upsilon_{I^N}\right)} = \left(\frac{\varphi}{1-\varphi}\right) P^{\phi}. \tag{50}$$

Setting

$$\alpha \equiv \ln \frac{\left(1 - \upsilon_{G^N} - \upsilon_{I^N}\right)}{\left(1 - \upsilon_{G^T} - \upsilon_{I^T}\right)} + \ln\left(\frac{\varphi}{1-\varphi}\right), \tag{51}$$

and taking logarithm, eq. (50) can be rewritten as follows:

$$\ln\left(\frac{Y^T - NX}{Y^N}\right) = \alpha + \phi \ln P. \tag{52}$$

Indexing time by t and countries by i, and adding an error term μ, we estimate ϕ by exploring the following empirical relationship:

$$\ln\left(\frac{Y^T - NX}{Y^N}\right)_{it} = f_i + f_t + \alpha_i t + \phi \ln P_{it} + \mu_{it}. \tag{53}$$

f_i captures the country fixed effects, f_t are time dummies, and μ_{it} are the i.i.d. error terms. Because the term (51) may display a trend over time, we add country-specific trends, as captured by $\alpha_i t$.

Because data to construct time series for traded (I^T) and non traded investment (I^N) are available for twelve countries over the sixteen in our sample over a time horizon varying between 37 years (1970-2007) and 27 years (1980-2007), we computed time series $Y^T - NX - I^T$ and $Y^N - I^N$. In this case, eq. (50) can be rewritten as follows:

$$\frac{\left(Y^T - NX - I^T\right)\left(1 - \upsilon_{G^T}\right)}{\left(Y^N - I^N\right)\left(1 - \upsilon_{G^N}\right)} = \left(\frac{\varphi}{1-\varphi}\right) P^{\phi}. \tag{54}$$

Denoting by

$$\kappa \equiv \ln \frac{\left(1 - \upsilon_{G^N}\right)}{\left(1 - \upsilon_{G^T}\right)} + \ln\left(\frac{\varphi}{1-\varphi}\right), \tag{55}$$

where $\upsilon_{G^T} = \frac{P^T G^T}{P^T (Y^T - NX - I^T)}$ and $\upsilon_{G^N} = \frac{P^N G^N}{P^N (Y^N - I^N)}$ and taking logarithm, we explore alternatively the following relationship to estimate ϕ:

$$\ln\left(\beta^T / \beta^N\right)_{it} = f_i + f_t + \alpha_i t + \phi \ln P_{it} + \nu_{it}. \tag{56}$$

where $\beta^T = \left(Y^T - NX - I^T\right)$ and $\beta^N = \left(Y^N - I^N\right)$.

When determining (52), we can alternatively make use of first-order conditions equating the marginal revenue of labor and the sectoral wage:

$$\frac{\theta^j P^j Y^j}{L^j} = W^j, \tag{57}$$

where θ^j is labor's share in value added in sector $j = T, N$. Using (57) to eliminate the nominal sectoral value added, $P^j Y^j$, the goods market clearing condition can be rewritten as follows:

$$\frac{\left(W^T L^T - \theta^T P^T NX\right) \frac{\theta^N}{\theta^T} \left(1 - \upsilon_{G^T} - \upsilon_{I^T}\right)}{W^N L^N \left(1 - \upsilon_{G^N} - \upsilon_{I^N}\right)} = \left(\frac{\varphi}{1-\varphi}\right) P^{\phi - 1}. \tag{58}$$

We first set

$$\eta \equiv \ln \frac{(1-\varrho_{G^N}-\varrho_{I^N})}{(1-\varrho_{G^T}-\varrho_{I^T})} + \ln\left(\frac{\theta^T}{\theta^N}\right) + \ln\left(\frac{\varphi}{1-\varphi}\right), \tag{59}$$

where $\varrho_{G^T} = \frac{P^T G^T}{(W^T L^T - \theta^T P^T NX)}$ and $\varrho_{G^N} = \frac{P^N G^N}{W^N L^N}$, $\varrho_{I^T} = \frac{P^T I^T}{(W^T L^T - \theta^T P^T NX)}$ and $\varrho_{I^N} = \frac{P^N I^N}{W^N L^N}$. Denoting by $\gamma^T = \left(W^T L^T - \theta^T P^T NX\right)$ and $\gamma^N = W^N L^N$, and taking logarithm, eq. (59) can be rewritten as follows:

$$\ln\left(\frac{\gamma^T}{\gamma^N}\right) = \eta + (\phi - 1)\ln P. \tag{60}$$

Indexing time by t and countries by i, and adding an error term ζ, we estimate ϕ by exploring the following empirical relationship:

$$\ln\left(\gamma^T/\gamma^N\right)_{it} = g_i + g_t + \sigma_i t + \rho p_{it} + \zeta_{it}. \tag{61}$$

Because η_i (see eq. (59)) is composed of both preference (i.e., φ) and production (i.e., θ^j) parameters, and (logged) ratios which may display trend over time, we introduce country fixed effects g_i and add country-specific trends, as captured by $\sigma_i t$. Once we have estimated ρ, we can compute $\hat{\phi} = \hat{\rho} + 1$ where a hat refers to point estimate in this context.

Using Time Series for Consumption by Purpose Taken from COICOP

The cross-section studies by Stockman and Tesar [1995] and Mendoza [1995] estimate ϕ by running a regression of the (logged) ratio of consumption in non tradables to consumption in tradables on the (logged) relative price of non tradables:

$$\ln\left(\frac{C^N}{C^T}\right) = \ln\left(\frac{1-\varphi}{\varphi}\right) - \phi \ln P. \tag{62}$$

Note that when exploring the relationship (62) empirically, we abstract from the goods market clearing condition. Indexing time by t and countries by i, and adding an error term ι, we explore the following relationship empirically by using panel data:

$$\ln\left(C^N/C^T\right)_{it} = d_i + d_t + \zeta_i t - \phi \ln P_{C,it} + \iota_{it}, \tag{63}$$

where $P_{C,it} = P^N_{C,it}/P^T_{C,it}$ is the ratio of the price deflator for consumption in non traded goods ($P^N_{C,it}$) to the price deflator for consumption in traded goods ($P^T_{C,it}$); d_i are country fixed effects while d_t are time dummies; ι_{it} are the i.i.d. error terms. Because preferences may not be homothetic, there might be income effects in the relative demand for tradable and non tradable goods. Cross-section studies by Stockman and Tesar [1995] and Mendoza [1995] include GDP per capita in the regression to capture the wealth effect. Because it is likely that GDP per capita is correlated with the relative price of non tradables, we capture the wealth effect by time trend, i.e., $\zeta_i t$.

A.3.2 Data Construction and Source

Using Time Series by Industry Taken from EU KLEMS and STAN

We provide more details below on the construction of data employed to estimate equations (53), (56) and (61) (codes in EU KLEMS/STAN are reported in parentheses):

- Sectoral value added price deflator P^j_t ($j = T, N$): value added at current prices (VA) over value added at constant prices (VA_QI) in sector j. The relative price of non tradables, P_t, corresponds to the ratio of the non traded value added deflator to the traded value added deflator: $P_t = P^N_t/P^T_t$. Sources: EU KLEMS and OECD STAN databases. Data coverage: 1970-2007 except for JPN 1974-2007.

- Sectoral output Y^j_t ($j = T, N$): value added at constant prices in sector j (VA_QI). Sources: EU KLEMS and OECD STAN databases. Data coverage: 1970-2007 except for JPN 1974-2007.

- Net exports NX_t: net exports deflated by the traded value added deflator, P_t^T. Net exports correspond to the external balance of goods and services at current prices. Source: OECD Economic Outlook Database. Data coverage: 1970-2007 except for JPN 1974-2007.

- Sectoral investment I_t^j ($j = T, N$): Real investment in sector j, I_t^j, is investment expenditure in sector j deflated by the value added price index P_t^j defined above. Investment expenditure are gross capital formation at current prices; to split aggregate investment expenditure into tradables and non tradables, we use the methodology presented in section A.2 of the Technical Appendix. Source: OECD Input-Output database [2012]. Data coverage: AUT (1976-2007), CAN (1970-2007), DNK (1970-2006), ESP (1980-2007), FIN (1970-2007), FRA (1978-2006), GBR (1970-2007), ITA (1970-2006), JPN (1980-2007), NLD (1970-2007), NOR (1970-2007) and USA (1977-2006). AUS and BEL (no data), and, IRL (1990-2007) and SWE (1993-2007) are excluded from the sample due to data limitation.

- Sectoral labor compensation $W_t^j L_t^j$ ($j = T, N$): labor compensation in sector j (LAB). Sources: EU KLEMS and OECD STAN databases. Data coverage: 1970-2007 except for JPN 1974-2007.

- Sectoral labor income share θ^j ($j = T, N$): labor compensation in sector j (LAB) over value added at current prices (VA) averaged over the period 1970-2007 (1974-2007 for JPN). Sources: EU KLEMS and OECD STAN databases.

We also use the time series described above to construct time series for $\frac{Y_t^T - NX_t}{Y_t^N}$, $\frac{\beta_t^T}{\beta_t^N}$, $\frac{\gamma_t^T}{\gamma_t^N}$, and P_t. When estimating equations (53), (56) and (61), all variables are converted into index 1995=100 and are expressed in log levels.

Using Time Series for Consumption By Purpose Taken from COICOP

Panel data estimations of ϕ are based upon a data set provided by the COICOP database. To split aggregate consumption expenditure into tradables and non tradables, we use the methodology detailed in Appendix A.2 where we provide detailed information about the construction of the non tradable share of consumption expenditure. The COICOP database provides annual data for the sixteen OECD countries of our sample but it has the disadvantage to be unbalanced. Only a few countries have long time series. For example, the US enters the panel with 38 observations, whereas the UK has merely 18. We therefore eschew countries providing no data for periods that extend before 1988 (i.e., countries with more than 20 years). We made this choice in order to ensure the consistency of the estimates of cointegrating vectors. Accordingly, the sample is restricted to eleven countries: AUS (1970-2007), AUT (1976-2007), CAN (1971-2007), DNK (1970-2007), FIN (1975-2007), FRA (1970-2007), ITA (1970-2007), JPN (1980-2007), NLD (1980-2007), NOR (1970-2007) and USA (1970-2007). The following countries: BEL (1995-2007), ESP (1995-2007), GBR (1990-2007), IRL (1995-2007) and SWE (1993-2007) are excluded from the sample due to data limitation.

We now provide information about the construction for the data used to estimate equation (63) :

- sectoral price deflator for consumption good j ($P_{C,t}^j$): consumption expenditure in good j at current prices over consumption expenditure in good j at constant prices. Source: COICOP database. The consumption relative price of non tradables, $P_{C,t}$, corresponds to the price deflator for consumption in non tradable goods over the price deflator for consumption in tradable goods: $P_t = P_{C,t}^N / P_{C,t}^T$.

- sectoral consumption expenditure C_t^j ($j = T, N$): final consumption expenditure of households in good j at constant prices (name in COICOP: P31DC). Source: COICOP database.

In equation (63), time series for $\left(C^N/C^T\right)_t$ and P_t^C are converted into index 1995=100 and are expressed in log levels.

A.3.3 Empirical Results

Since the set of variables of interest in regressions (53), (56), (61) and (63) display trends, we first run panel unit root tests, see Table 7. By and large, all tests, with the exceptions of Breitung and MW(PP) for the variable $\ln(Y^T - NX/Y^N)$, show that non stationarity is pervasive, making it clear that pursuing a cointegration analysis is appropriate. We thus implement the seven Pedroni's [2004] tests of the null hypothesis of no cointegration, see Table 8. Across almost all cases the null hypothesis of no cointegration is rejected but only at the 10% level. In small samples, Pedroni's [2004] simulations reveal that the group-mean parametric t-stat is the most powerful. Based on this result, in the three specifications, the null hypothesis of no cointegration is strongly rejected at the 5% level.

Table 7: Panel Unit Root Tests (p-values)

	LLC (t-stat)	Breitung (t-stat)	IPS (W-stat)	MW (ADF)	MW (PP)	Hadri (Z_μ-stat)
$\ln(P^{C,N}/P^{C,T})$	0.206	0.879	0.998	0.441	0.137	0.000
$\ln(C^N/C^T)$	0.156	0.844	0.255	0.132	0.293	0.000
$\ln(P^{VA,N}/P^{VA,T})$	0.670	0.370	1.000	0.976	0.889	0.000
$\ln(Y^T - NX/Y^N)$	0.322	0.000	0.164	0.061	0.028	0.000
$\ln(Y^T - NX - I^T)/(Y^N - I^N)$	0.616	0.799	0.938	0.959	0.960	0.000
$\ln(W^T L^T - \theta^T P^T NX)/(W^N L^N)$	0.843	0.854	1.000	1.000	1.000	0.000

Notes: For all tests, except for Hadri [2000], the null of a unit root is not rejected if p-value $\geq$ 0.05 at a 5% significance level. For Hadri [2000], the null of stationarity is rejected if p-value $\leq$ 0.05 at a 5% significance level.

Table 8: Panel Cointegration Tests (p-values)

Dependent variable	$\frac{C^N}{C^T}$	$\frac{Y^T - NX}{Y^N}$	$\frac{Y^T - NX - I^T}{Y^N - I^N}$	$\frac{W^T L^T - \theta^T P^T NX}{W^N L^N}$
Explanatory variable	$P^{C,N}/P^{C,T}$	$P^{VA,N}/P^{VA,T}$	$P^{VA,N}/P^{VA,T}$	$P^{VA,N}/P^{VA,T}$
Panel tests				
Non-parametric ν	0.274	0.065	0.000	0.009
Non-parametric ρ	0.441	0.001	0.006	0.011
Non-parametric t	0.347	0.000	0.001	0.004
Parametric t	0.006	0.048	0.000	0.040
Group-mean tests				
Non-parametric ν	0.059	0.047	0.383	0.232
Non-parametric t	0.245	0.000	0.311	0.021
Parametric t	0.000	0.068	0.001	0.021

Notes: the null hypothesis of no cointegration is rejected if the p-value is below 0.05 (0.10 resp.) at 5% (10% resp.) significance level.

To estimate the cointegrating vector, we use the group-mean fully modified OLS and the group-mean dynamic OLS estimators of Pedroni [2001]. Table 9 reports panel estimations of the coefficient ϕ, when running the regression (53), (56), (61) and (63) respectively; the three former empirical relationships are derived by taking into account the goods market equilibrium. Moreover, exploring alternatively the relationship (53) or (61) empirically has the advantage of allowing us to use time series for sectoral value added or labor compensation which are available over the period 1970-2007 for all countries of our sample (except JPN: 1974-2007).

The first column of Table 9 presents the results corresponding to eq. (63). The dependent variable in both cases is the log of consumption in non tradables in terms of tradables, i.e. $\ln(C^N/C^T)$. The regressor is the log of the ratio of the price deflator for consumption in non tradables to the price deflator for consumption in tradables. The estimated coefficient for ϕ of 0.579 (DOLS) and 0.615 (FMOLS) are highly significant with a t-statistic of 8.72 and 11.85 respectively. However, there is substantial evidence of parameter heterogeneity across countries of the sample. One drawback of this approach is that when determining the testable equation (63), we abstract from the goods market equilibrium.

Panel data estimates of ϕ when running the regression (53) where the dependent variable is $(Y^T - NX)/Y^N$, are shown in column 2 of Table 9. The regressor in this case (and for the rest of the analysis) is the log of the non traded value added deflator to the traded value added deflator. The sample covers all countries we are interested in. For the whole sample, the DOLS and FMOLS estimates give a significant value of ϕ of 0.680 and 0.656 respectively. The two estimated coefficients are statistically significant. The vast majority (14 out of 16) of the individual FMOLS estimated coefficients are statistically significant. They vary from a low of 0.070 for BEL to a high of 2.071 for DNK. In addition, we find that ϕ is larger than one in only two countries (DNK and FIN). Column 3 of Table 9 shows panel data estimations of ϕ when running the regression (56) which explicitly takes into account investment expenditures. This, however, reduces the size of the sample: the series for investment are not available for AUS and BEL, and, SWE and IRL are excluded from the sample due to data limitation. We find that both estimators provide positive and statistically significant ϕ coefficients about 0.590. Among the 12 countries, we find that 8 have positive and statistically significant ϕ coefficients according to the FMOLS estimator, ranging from a low of 0.252 (CAN) to a high of 1.758 (NLD). Note that the coefficient ϕ is found to be larger than one in 6 countries (AUT, FIN, FRA, NLD, NOR and USA). Three estimated coefficients are negative (DNK, ESP and ITA), although none of them are statistically significant. Due to data limitations and inconsistent estimates (i.e., negative or statistically insignificant at conventional level for several countries), we find that including investment expenditure does not improve the precision of our estimates, likely due to the classification of investment items which is different to that we used to classify value added and labor as tradables or non tradables.

The last column of Table 9 gives panel data estimates of ϕ when running the regression (61); the dependent variable is the (logged) ratio of the labor income in tradables adjusted with net exports at current prices to labor income in non tradables, i.e., $(W^T L^T - \theta^T P^T NX)/W^N L^N$. By and large, estimates are somewhat higher than those shown in columns 1-3 of Table 9: the DOLS and FMOLS estimates give a significant value of ϕ of 0.817 and 0.837, respectively. Focusing only on FMOLS estimates which are positive and statistically significant, we find large differences in estimated coefficients across countries. They vary from a low of 0.409 for AUS to a high of 2.056 for NOR.

To calibrate the model, we take FMOLS estimates shown in column 2 as they are in line with earlier studies and values of ϕ are consistent for almost all countries in sample, except for Belgium and Italy. Estimate of ϕ for Belgium is not statistically significant at a standard threshold while estimates of ϕ for Italy are negative. Running the regression (61) allows us to obtain a consistent estimate for ϕ for Belgium, i.e., 0.795. Thus, we use this value to calibrate the model to each country. In contrast, estimates of ϕ are all inconsistent for Italy. When we calibrate the model to each country, we set ϕ to the unweighed average, i.e., 0.77.

A.4 Estimates of ϵ: Empirical Strategy

In this section, we detail our empirical strategy to estimate the elasticity of labor supply across sectors, ϵ, which captures the degree of labor mobility across sectors.

A.4.1 Limited Substitutability of Hours Worked across Sectors and the Derivation of the Testable Equation

To determine the equation we explore empirically, we follow closely Horvath [2000]. The representative agent is endowed with one unit of time, supplies a fraction $L(t)$ as labor, and consumes the remainder $1-L(t)$ as leisure. At any instant of time, households derive utility from their consumption and experience disutility from working. Assuming that the felicity function is additively separable in consumption and labor, the representative household maximizes the following objective function:

$$U = \int_0^\infty (1-\gamma) \ln C(t) + \gamma \ln (1 - L(t)) \, e^{-\rho t} \mathrm{d}t, \tag{64}$$

Table 9: DOLS and FMOLS Estimates of ϕ

Dependent variable	$\frac{C^N}{C^T}$		$\frac{Y^T - NX}{Y^N}$		$\frac{Y^T - NX - I^T}{Y^N - I^N}$		$\frac{W^T L^T - \theta^T P^T NX}{W^N L^N}$	
Sectoral prices	consumption		value-added		value-added		value-added	
	(1)		(2)		(3)		(4)	
	DOLS	FMOLS	DOLS	FMOLS	DOLS	FMOLS	DOLS	FMOLS
AUS	1.013^a	1.041^a	0.290^a	0.268^a			0.286	0.409^b
	(7.53)	(9.08)	(2.93)	(2.99)			(1.22)	(2.52)
AUT	−0.008	0.309	0.927^b	0.986^a	1.274	1.368^c	1.337^a	1.413^a
	(−0.01)	(0.57)	(2.07)	(3.09)	(0.73)	(1.75)	(3.92)	(4.99)
BEL			0.073	0.070			0.800^a	0.795^a
			(0.40)	(0.41)			(6.80)	(4.99)
CAN	-0.183^b	-0.212^c	0.437^a	0.391^a	0.550^a	0.252^b	0.625^a	0.582^a
	(−2.56)	(−1.80)	(4.17)	(3.74)	(5.02)	(2.40)	(6.21)	(5.53)
DNK	0.515^a	0.740^a	2.234^a	2.071^a	2.036	−0.270	1.036^c	1.323^a
	(2.77)	(6.44)	(2.72)	(2.95)	(1.56)	(−0.41)	(1.74)	(2.93)
ESP			0.745^a	0.783^a	−0.734	−0.040	0.372	0.413^b
			(3.71)	(4.96)	(−1.12)	(−0.08)	(1.48)	(2.04)
FIN	−0.461	0.047	1.213^a	1.072^a	1.087^a	1.471^a	1.590^a	1.421^a
	(−0.43)	(0.06)	(9.88)	(8.57)	(4.75)	(4.72)	(8.66)	(8.12)
FRA	1.292^a	0.922^a	0.955^a	0.937^a	1.150^a	1.031^a	1.028^a	1.038^a
	(7.86)	(8.94)	(5.75)	(6.22)	(6.99)	(6.31)	(4.67)	(5.25)
GBR			0.517^a	0.477^a	0.255^a	0.289^b	1.167^a	1.164^a
			(11.30)	(9.64)	(2.59)	(2.19)	(12.59)	(14.07)
IRL			0.184	0.374^c			0.070	0.158
			(0.63)	(1.71)			(0.13)	(0.35)
ITA	−0.341	−0.153	-0.436^a	−0.308	-0.729^a	−0.410	-0.320^b	−0.187
	(−0.58)	(−0.40)	(−2.92)	(−1.60)	(−3.91)	(−1.60)	(−2.55)	(−0.98)
JPN	0.768^b	0.856^a	1.012^a	0.654^a	−0.371	0.322	0.898^a	0.676^a
	(2.15)	(2.81)	(4.35)	(2.98)	(−1.02)	(1.34)	(5.95)	(4.33)
NLD	0.194	0.841^a	0.820^b	0.709^b	1.910^a	1.758^a	0.529	0.428
	(1.38)	(5.32)	(1.99)	(2.33)	(3.00)	(3.23)	(1.39)	(1.18)
NOR	0.308^c	0.328^b	0.992^a	0.979^a	1.329^a	1.025^a	1.957^a	2.056^a
	(1.72)	(2.50)	(8.38)	(9.72)	(3.77)	(7.23)	(10.29)	(13.66)
SWE			0.330^a	0.356^a			0.907^a	0.900^a
			(3.69)	(4.02)			(7.31)	(7.23)
USA	3.396^a	3.269^a	0.586	0.668^a	0.794^a	1.003^a	0.786	0.799^b
	(5.45)	(6.41)	(1.57)	(2.81)	(2.81)	(5.53)	(1.20)	(2.02)
Whole Sample	0.579^a	0.615^a	0.680^a	0.656^a	0.595^a	0.588^a	0.817^a	0.837^a
	(8.72)	(11.85)	(15.15)	(16.13)	(6.69)	(8.99)	(16.59)	(14.16)
Countries	11		16		12		16	
Observations	386		605		412		605	
Country fixed effects	yes		yes		yes		yes	
Time dummies	yes		yes		yes		yes	
Time trend	yes		yes		yes		yes	

Notes: all variables enter in regression in logarithms. ^{a}, ^{b} and ^{c} denote significance at 1%, 5% and 10% levels. Heteroskedasticity and autocorrelation consistent t-statistics are reported in parentheses.

subject to

$$\dot{A}(t) = r^{\star}A(t) + W(t)L(t) - P_C\left(P(t)\right)C(t). \tag{65}$$

For the sake of clarity, we drop the time argument below when this causes no confusion. First-order conditions are:

$$\frac{1-\gamma}{C} = \left(P_C\lambda\right), \tag{66a}$$

$$\frac{\gamma}{1-L} = W\lambda, \tag{66b}$$

$$\dot{\lambda} = \lambda\left(\beta - r^{\star}\right). \tag{66c}$$

The economic system consists of M distinct sectors, indexed by $j = 0, 1, ..., M$ each producing a different good. Along the lines of Horvath [2000], the aggregate leisure index is assumed to take the form:

$$1 - L\left(.\right) = 1 - \left[\sum_{j=1}^{M}\left(L^j\right)^{\frac{\epsilon+1}{\epsilon}}\right]^{\frac{\epsilon}{\epsilon+1}}. \tag{67}$$

The agent maximizes (67) subject to

$$\sum_{j=1}^{M} W^j L^j = X, \tag{68}$$

where L^j is labor supply in sector j, W^j the wage rate in sector j and X total labor income. Applying standard methods, we obtain labor supply L^j in sector j:

$$L^j = \left(\frac{W^j}{W}\right)^{\epsilon} L. \tag{69}$$

where we used the fact that $X = WL$.

Combining (66a) and (66b), the aggregate wage index is:

$$W = \frac{\gamma}{1-\gamma}\frac{P_C C}{1-L} \tag{70}$$

which allows us to rewrite (69) as follows:

$$L^j = \left(W^j\right)^{\epsilon} L\left(\frac{\gamma}{1-\gamma}\frac{P_C C}{1-L}\right)^{-\epsilon} \tag{71}$$

A quantity Q^j of good j is produced by combining capital, K^j, labor devoted to the sector, L^j, and intermediate inputs, IM^j, in a production process described by:

$$Q^j = Z^j\left(L^j\right)^{\xi^j}\left(K^j\right)^{\gamma^j}\left(IM^j\right)^{1-\xi^j-\gamma^j}, \tag{72}$$

where ξ^j (γ^j) is the share of labor (capital) income in gross output of sector j.

We assume that labor is imperfectly mobile across sectors, while capital can move freely across sectors. Perfectly competitive firms in sector j seek to maximize the profit function given by:

$$\Pi^j = P^j Q^j - W^j L^j - RK^j - P_{IM} IM^j, \tag{73}$$

where P^j is the price of gross output, R is the user capital cost, W^j the wage rate in sector j, and P_{IM} the price of intermediate inputs. Firms take the wage rate (capital rental cost) as given and equate marginal product of labor (capital) to the wage (capital rental rate) to determine demand. First-order conditions are:

$$P^j\frac{\xi^j Q^j}{L^j} = W^j, \quad P^j\frac{\gamma^j Q^j}{K^j} = R, \quad P^j\frac{\left(1-\xi^j-\gamma^j\right)Q^j}{IM^j} = P_{IM}. \tag{74}$$

Eliminating the sectoral wage W^j into (71) by using labor demand given by (74), the equilibrium condition for labor is given by:

$$L^j = \left(\xi^j P^j Q^j\right)^{\frac{\epsilon}{\epsilon+1}} L^{\frac{1}{1+\epsilon}} \left(\frac{\gamma}{1-\gamma}\frac{P_C C}{1-L}\right)^{-\frac{\epsilon}{\epsilon+1}}. \tag{75}$$

Summing over the M sectors and using (67), we get:

$$\left(\frac{\gamma}{1-\gamma}\frac{P_C C}{1-L}\right) = \frac{\sum_{j=1}^{M} \theta^j P^j Q^j}{L}$$

Plugging this equation into (75) yields:

$$L^j = \left(\frac{\xi^j P^j Q^j}{\sum_{j=1}^{M} \xi^j P^j Q^j}\right)^{\frac{\epsilon}{\epsilon+1}} L. \tag{76}$$

As in Horvath [2000], we denote by β^j the fraction of labor's share of aggregate output accumulating to labor in sector j:

$$\beta^j = \frac{\xi^j P^j Q^j}{\sum_{j=1}^{M} \xi^j P^j Q^j}. \tag{77}$$

We introduce the time subscript to avoid confusion. Expressing (76) in percentage changes and adding an estimation error term ν results in the M estimation equations:

$$\hat{l}_t^j - \hat{l}_t = \frac{\epsilon}{\epsilon+1}\hat{\beta}_t^j + \nu_t^j, \quad j = 1, ..., M, \tag{78}$$

where

$$\hat{l}_t = \sum_{j=1}^{M} \beta_{t-1}^j \hat{l}_t^j. \tag{79}$$

To derive (79), we proceed as follows. Because we consider a traded and a non traded sectors, the labor index (67) can be rewritten as follows:

$$L\left(L_t^T, L_t^N\right) = \left[\left(L_t^T\right)^{\frac{\epsilon+1}{\epsilon}} + \left(L_t^N\right)^{\frac{\epsilon+1}{\epsilon}}\right]^{\frac{\epsilon}{\epsilon+1}}. \tag{80}$$

Approximate changes in aggregate labor with differentials, we get:

$$\mathrm{d}L_t \equiv L_t - L_{t-1} = \left(L_{t-1}^T\right)^{\frac{1}{\epsilon}} \left(L_{t-1}\right)^{-\frac{1}{\epsilon}} \mathrm{d}L_t^T + \left(L_{t-1}^N\right)^{\frac{1}{\epsilon}} \left(L_{t-1}\right)^{-\frac{1}{\epsilon}} \mathrm{d}L_t^N. \tag{81}$$

Expressing (81) in percentage changes and inserting (76), i.e., $\left(\frac{L^j}{L}\right)^{\frac{\epsilon+1}{\epsilon}} = \beta^j$, we have:

$$\begin{aligned} \hat{l}_t \equiv \frac{L_t - L_{t-1}}{L_{t-1}} &= \left(\frac{L_{t-1}^T}{L_{t-1}}\right)^{\frac{\epsilon+1}{\epsilon}} \hat{l}_t^T + \left(\frac{L_{t-1}^N}{L_{t-1}}\right)^{\frac{\epsilon+1}{\epsilon}} \hat{l}_t^N, \\ &= \beta_{t-1}^T \hat{l}_t^T + \beta_{t-1}^N \hat{l}_t^N. \end{aligned} \tag{82}$$

According to eq. (82), the percentage change in total hours worked, $\hat{l}_t$, can be approximated by a weighted average of changes in sectoral hours worked $\hat{l}_t^j$ (in percentage), the weight being equal to β_{t-1}^j.

Combining optimal rules for labor supply and labor demand, we find that the change in employment in sector j is driven by the change in the fraction β^j of the labor's share of aggregate output accumulating to labor in sector j. We use panel data to estimate (78). Including country fixed effects captured by country dummies, f_i, and common macroeconomic shocks by year dummies, f_t, (78) can be rewritten as follows:

$$\hat{l}_{it}^j - \hat{l}_{it} = f_i + f_t + \gamma_i \hat{\beta}_{it}^j + \nu_{it}^j, \tag{83}$$

where $\gamma_i = \frac{\epsilon_i}{\epsilon_i+1}$ and β_{it}^j is given by (77); j indexes the sector, i the country, and t indexes time. When exploring empirically (83), the coefficient γ is alternatively assumed to be identical, i.e., $\gamma_i = \gamma$, or to vary across countries. The LHS term of (83), i.e., $\hat{l}_{it}^j - \hat{l}_{it}$, gives the percentage change in hours worked in sector j driven by the pure reallocation of labor across sectors.

A.4.2 Data Description

Data are taken from EU KLEMS and STAN databases. EU KLEMS data provide yearly information for the period 1970-2007 (except for JPN: 1974-2007) for 16 countries of our sample (AUS, AUT, BEL, DNK, ESP, FIN, FRA, GBR, IRL, ITA, JPN, NLD,SWE and USA). For CAN and NOR, annual sectoral data stems from the STAN database. To classify employment and gross output as traded or non traded, we adopt the classification described in subsection A.1.2. We provide more details below about the data used to estimate equation (83):

- Sectoral labor L_t^j ($j = T, N$): total hours worked by persons engaged in sector j (H_EMP). Sources: EU KLEMS and STAN databases.

- Sectoral nominal gross output $P_t^j Q_t^j$ ($j = T, N$): gross output at current prices in millions of national currency in sector j (GO). Sources: EU KLEMS and STAN databases.

- Sectoral share of labor income in gross output ξ^j for $j = T, N$: labor compensation in sector j (LAB) over gross output at current prices in that sector (GO) averaged over the period 1970-2007 (1974-2007 for JPN). Sources: EU KLEMS and STAN databases.

By combining ξ^j and $P_t^j Q_t^j$, we can construct time series β_t^j defined by (77).

A.4.3 Exogeneity of the Regressor

By using optimal rules for both labor supply (69) and labor demand (74), we avoid any endogeneity problem. To see it more clearly, when restricting our attention to the optimal labor supply schedule without using firms' first order conditions, eq. (69) in percentage changes is:

$$\hat{l}_t^j - \hat{l}_t = \epsilon \left(\hat{w}_t^j - \hat{w}_t \right). \tag{84}$$

where $\hat{l}_t$ is given by (82). An endogeneity problem may arise because to construct time series for sectoral wages W_t^j, we have to divide the labor compensation $W_t^j L_t^j$ in sector j by sectoral hours worked L_t^j; likewise, we have to divide the overall labor compensation $W_t L_t$ by total hours worked L_t to construct time series for the aggregate wage index W_t. A way to circumvent any endogeneity problem is to use labor demand $\frac{\xi^j P_t^j Q_t^j}{L_t^j} = W_t^j$ to eliminate the sectoral wage from eq. (84), and $W_t = \frac{\sum_j \xi^j P_t^j Q_t^j}{L_t}$ to eliminate the aggregate wage index; we get $L_t^j / L_t = \left(\frac{\xi^j P_t^j Q_t^j}{L_t^j} / \frac{\sum_j \xi^j P_t^j Q_t^j}{L_t} \right)^{\epsilon}$. Isolating L_t^j / L_t and differentiating yields (78). Because wages do not show up in eq. (78) as we use the labor income share which is constant over time and gross output (at current prices), we avoid any endogeneity problem. More precisely, the labor's share in gross output ξ^j in sector j is defined as the ratio of the compensation of employees to gross output in the jth sector, averaged over the period 1970-2007 so that the explanatory variable (i.e., the RHS term in eq. (83)) is constructed independently from the dependent variable (i.e., the LHS term in eq. (83)).

To check that endogeneity is not a major issue in eq. (83), we test for strict exogeneity of the regressor with respect to the dependent variable. Engle et al. [1983] refer to a variable x_t as strongly exogenous with respect to the variable y_t if y_t does not Granger-cause x_t (see Granger [1969]). Formally, y_t Granger causes x_t if its past value can help to predict the future value of x_t beyond what could have been done with the past value of x_t only. To implement the test of whether $(\hat{l}_{it}^j - \hat{l}_{it})$ (i.e., the LHS term in eq. (83)) Granger-causes $\hat{\beta}_{it}^j$ (i.e., the RHS term in eq. (83)) we run the following regression:

$$\hat{\beta}_{it}^j = \alpha_i^j + \sum_{k=1}^{k} a_{i,k}^j \hat{\beta}_{i,t-k}^j + \sum_{k=1}^{p} b_{i,k}^j \left(\hat{l}_{i,t-k}^j - \hat{l}_{i,t-k} \right) + u_{it}^j, \tag{85}$$

where p is the autoregressive lag length and u_{it}^j the error term. With respect to (85), in country i and sector j, the test of the null hypothesis that $(\hat{l}_{it}^j - \hat{l}_{it})$ does not Granger cause

$\hat{\beta}^j_{it}$ is a F test of the form: $H_0 : b^j_{i,1} = b^j_{i,2} = \cdots = b^j_{i,p} = 0$. By not rejecting the null, one may conclude that the regressor in (83) is strictly exogenous to the dependent variable $(\hat{l}^j_{it} - \hat{l}_{it})$.

Table 10: Granger Causality Test (p-values)

Country	Sector	$p = 1$	$p = 2$	$p = 3$	Country	Sector	$p = 1$	$p = 2$	$p = 3$
AUS	T	0.946	0.833	0.935	GBR	T	0.216	0.508	0.505
AUS	N	0.215	0.132	0.088	GBR	N	0.087	0.247	0.399
AUT	T	0.893	0.665	0.091	IRL	T	0.470	0.511	0.819
AUT	N	0.099	0.040	0.014	IRL	N	0.252	0.535	0.798
BEL	T	0.263	0.934	0.206	ITA	T	0.481	0.303	0.054
BEL	N	0.655	0.962	0.176	ITA	N	0.362	0.262	0.022
CAN	T	0.070	0.118	0.258	JPN	T	0.049	0.019	0.051
CAN	N	0.179	0.098	0.218	JPN	N	0.130	0.070	0.112
DNK	T	0.172	0.494	0.006	NLD	T	0.239	0.533	0.703
DNK	N	0.230	0.491	0.015	NLD	N	0.285	0.426	0.615
ESP	T	0.015	0.024	0.022	NOR	T	0.359	0.652	0.712
ESP	N	0.018	0.020	0.021	NOR	N	0.773	0.799	0.647
FIN	T	0.191	0.120	0.160	SWE	T	0.344	0.218	0.204
FIN	N	0.341	0.153	0.107	SWE	N	0.133	0.111	0.096
FRA	T	0.727	0.844	0.796	USA	T	0.958	0.459	0.634
FRA	N	0.951	0.535	0.362	USA	N	0.832	0.632	0.885

Notes: the null hypothesis that $(\hat{l}^j_{it} - \hat{l}_{it})$ does not Granger-cause $(\hat{\beta}^j_{it})$ is rejected if p-value ≤ 0.05 at a 5% significance level.

The results of causality tests for $p = 1, 2, 3$ from the change in hours worked in sector j driven by the pure reallocation of labor across sectors $(\hat{l}^j_{it} - \hat{l}_{it})$ to the fraction of labor's share of aggregate output accumulating to labor in sector j $(\hat{\beta}^j_{it})$ are displayed in Table 10. The results for $p = 1$ show that, with the exception of JPN (sector T) and ESP (both sectors), there is no causality running from $(\hat{l}^j_{it} - \hat{l}_{it})$ to $\hat{\beta}^j_{it}$ at the 5% level of significance. Setting $p = 2$ and $p = 3$ leads to similar qualitative results (with the exceptions of the sector N in AUT for $p = 2, 3$ and in DNK and ITA for $p = 3$). By and large, these results show that one can consider the regressor in eq. (83) as exogenous with respect to the dependent variable.

A.4.4 Panel Data Estimates of ϵ

The parameter we are interested in, the degree of substitutability of hours worked across sectors, is given by $\epsilon_i = \gamma_i/(1 - \gamma_i)$. In the regressions that follow, the coefficient γ_i is alternatively assumed to be identical across countries when estimating for the whole sample ($\gamma_i = \gamma_{i'} \equiv \gamma$ for $i \neq i'$) or to be different across countries when estimating for each economy ($\gamma_i \neq \gamma_{i'}$ for $i \neq i'$). The sample is running from 1971 to 2007 but we run regression (83) over two sub-periods 1971-1989 and 1990-2007 as well in order to investigate whether our estimates of the degree of labor mobility are relatively stable across sub-periods.

Empirical results reported in Table 11 are consistent with $\epsilon > 0$. For the whole sample, we find $\hat{\gamma} = 0.324$ over the period 1971-2007. Using the fact that $\hat{\epsilon} = \frac{1}{1-\hat{\gamma}}$, we find empirically that an increase by 1 percentage point of the labor's share of aggregate output accumulating to labor in sector j shifts employment by 0.479 percentage point of total employment toward that sector. When estimating ϵ for each economy of our sample over the period 1971-2007, all coefficients are statistically significant, as shown in Table 11, except for DNK and NOR. Excluding these countries, we find that the degree of substitutability of hours worked across sectors ranges from a low of 0.224 for NLD to a high of 1.642 for ESP, with a mean value (across countries) of 0.746. Moreover, the panel data estimations of ϵ for the whole sample are quite similar whether the sample is running from 1971 to 2007 or is split into two sub-periods.

Table 11: Panel Data Estimate of ϵ (eq. (83))

	1971-2007				1971-1989				1990-2007			
	$\hat{\gamma}_i$	$\hat{\epsilon}_i$	$\hat{\gamma}$	$\hat{\epsilon}$	$\hat{\gamma}_i$	$\hat{\epsilon}_i$	$\hat{\gamma}$	$\hat{\epsilon}$	$\hat{\gamma}_i$	$\hat{\epsilon}_i$	$\hat{\gamma}$	$\hat{\epsilon}$
AUS	0.389^a (5.80)	0.635^a (3.55)			0.457^a (5.51)	0.841^a (2.99)			0.247^b (2.11)	0.327 (1.59)		
AUT	0.354^a (4.12)	0.548^a (2.66)			0.387^a (3.72)	0.632^b (2.28)			0.281^c (1.85)	0.391 (1.33)		
BEL	0.246^a (3.32)	0.326^b (2.51)			0.263^a (2.60)	0.357^c (1.92)			0.225^b (2.08)	0.290 (1.61)		
CAN	0.312^a (4.96)	0.454^a (3.41)			0.258^a (2.81)	0.348^b (2.08)			0.363^a (4.18)	0.571^a (2.66)		
DNK	0.131^c (1.67)	0.150 (1.46)			0.161 (1.57)	0.191 (1.32)			0.087 (0.72)	0.095 (0.66)		
ESP	0.622^a (7.97)	1.642^a (3.02)			0.828^a (6.14)	4.827 (1.05)			0.514^a (5.42)	1.059^a (2.63)		
FIN	0.352^a (5.59)	0.544^a (3.62)			0.502^a (4.78)	1.007^b (2.38)			0.264^a (3.34)	0.358^b (2.46)		
FRA	0.563^a (5.57)	1.287^b (2.44)			0.568^a (4.06)	1.314^c (1.75)			0.556^a (3.76)	1.252^c (1.67)		
GBR	0.502^a (7.61)	1.008^a (3.79)			0.400^a (4.94)	0.667^a (2.96)			0.714^a (6.15)	2.496^c (1.76)		
IRL	0.209^a (4.02)	0.264^a (3.18)			0.068 (0.79)	0.073 (0.73)			0.294^a (4.52)	0.417^a (3.19)		
ITA	0.407^a (4.79)	0.686^a (2.84)			0.423^a (3.81)	0.734^b (2.20)			0.383^a (2.86)	0.620^c (1.76)		
JPN	0.498^a (5.73)	0.993^a (2.87)			0.535^a (4.65)	1.149^b (2.16)			0.449^a (3.40)	0.815^c (1.87)		
NLD	0.183^b (2.41)	0.224^b (1.97)			0.107 (1.16)	0.120 (1.04)			0.354^a (2.60)	0.547^c (1.68)		
NOR	0.088 (1.63)	0.097 (1.49)			0.179^b (2.45)	0.217^b (2.01)			−0.024 (−0.30)	−0.023 (−0.31)		
SWE	0.307^a (5.20)	0.443^a (3.61)			0.280^a (3.45)	0.388^b (2.49)			0.339^a (3.94)	0.513^a (2.61)		
USA	0.581^a (6.18)	1.387^a (2.59)			0.578^a (5.12)	1.371^b (2.16)			0.588^a (3.46)	1.430 (1.42)		
Whole Sample			0.324^a (17.99)	0.479^a (12.16)			0.332^a (13.27)	0.496^a (8.87)			0.314^a (11.62)	0.457^a (7.97)
R-squared	0.276		0.226		0.307		0.238		0.272		0.208	
Observations	1178		1178		602		602		576		576	
Countries	16		16		16		16		16		16	
Sectors	2		2		2		2		2		2	
Country fixed effects	yes		yes		yes		yes		yes		yes	
Time dummies	yes		yes		yes		yes		yes		yes	
Time trend	no		no		no		no		no		no	

Notes: ^{a}, ^{b} and ^{c} denote significance at 1%, 5% and 10% levels; t-statistics are reported in parentheses.

B More VAR Results and Robustness Check

In this section, we provide more VAR results and conduct a robustness check. In particular, for reason of space, in the main text, we report results of selected variables. Subsection B.1 below reports results for all variables and all VAR models. Due to data availability, we use annual data for eleven 1-digit ISIC-rev.3 industries that we classify as tradables or non tradables. Because at this level of disaggregation, the classification is somewhat ambiguous as some sub-industries could be classified as tradables while other sub-industries are treated as non tradables, subsection B.2 investigates the sensitivity of our empirical results to the classification of industries as tradables or non tradables. In subsection B.3, we estimate the same VAR models as in the main text and investigate empirically the effects of government spending shocks on the business sector by excluding the public sector from aggregate and sectoral variables. Finally, in subsection B.4, since we are constrained to employ annual data as we wish to estimate the sectoral effects of a government spending shock, we investigate the extent to which our empirical results could be altered by our assumption that government spending is predetermined within the year.

B.1 Additional VAR Evidence for the Whole and the Split-Sample Analysis

In section 2, we present VAR evidence on the fiscal transmission. For reason of space and clarity purposes, when we consider the second, third and fourth VAR model that we estimate for the whole sample, we dot not show the responses of government spending and the responses of sectoral real consumption wages. Figure 11 report the responses of government spending along with the adjustment of real consumption wages for the second VAR specification. Results are almost identical for the third VAR specification. Panels A and B of Table 1 report the endogenous cumulative response of government spending for the 'labor market' (i.e., $z_{it}^W = \left[g_{it}, l_{it}^T - l_{it}^N, \omega_{it}\right]$) and the 'product market' specifications (i.e, $z_{it}^P = \left[g_{it}, y_{it}^T - y_{it}^N, p_{it}\right]$). Contrasting the endogenous cumulative response of government consumption displayed in column 1 of Table 1 with that reported in column 1 of Table 13, we can see immediately that the difference is very small while it shows somewhat higher degree of persistence in the latter case, so that the cumulative response is merely higher.

In section 2.4, we split the sample into two sub-samples: a sample of 'low mobility' economies and a sample of 'high mobility' economies. For each country in our sample, we estimate the elasticity of labor supply across sectors, denoted by ϵ, that captures the extent of workers' mobility costs across sectors: as ϵ takes higher values, workers support relatively less mobility costs and thus are more willing to shift their hours worked from one sector to another. The 'low mobility' economies comprise Australia, Austria, Belgium, Canada, Denmark, Finland, Italy, Ireland, Netherlands, Norway, Sweden, while 'high mobility' economies consist of France, Japan, Spain, United-Kingdom, United States.

In order to give some support for our measure of workers' mobility cost, we compute an intersectoral labor reallocation index for each country i, which we denote by $LR_{i,t}(\tau)$; we expect the labor reallocation index to increase less in countries where the elasticity of labor supply across sectors ϵ takes lower values. To estimate the labor reallocation effect of a government spending shock, we replace the (log) ratio of hours worked in the traded sector to hours worked in the non traded sector, i.e., $l_{it}^T - l_{it}^N$, with the labor reallocation index $LR_{i,t}(2)$, in the 'labor market' specification; this index measures the fraction of workers that shift from one sector to another between year t and year $t-2$. Our vector of endogenous variables for the 'labor reallocation' specification is thus given by: $z_{it}^W = [g_{it}, LR_{it}(2), \omega_{it}]$. In Table 1, we do not show the cumulative responses for neither government spending nor the relative wage to an exogenous fiscal shock by 1 percentage point of GDP. Panel C of Table 13 shows cumulates responses for these two variables and the labor reallocation index as well for selected horizons, i.e, at a first-, two-, four-year horizon. First, for the whole sample, we find that a government spending shock increases the labor reallocation across sectors above trend. As emphasized in the main text, contrasting the cumulative responses reported in columns 2 and 3 of Table 13, we find that countries with a smaller elasticity of labor supply across sectors experiences a lower increase in the fraction of workers that shift

Table 12: Cumulative Responses to Spending Shock

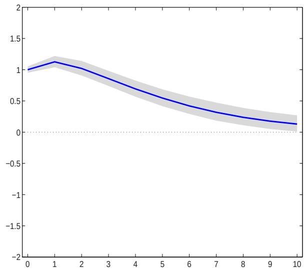
Variables	Horizon	All sample (1)	Low Mobility (2)	High Mobility (3)
A.Labor Market				
Gov. spending	1	1.000*	1.000*	1.000*
	2	2.190*	2.214*	2.213*
	4	4.294*	4.439*	3.874*
Relative Labor	1	−0.705*	−0.362*	−1.657*
(L^T/L^N)	2	−2.007*	−1.366	−3.719*
	4	−4.968*	−4.141	−6.835*
Relative Wage	1	0.926*	1.242*	−0.099
(W^N/W^T)	2	2.500*	3.311*	−0.087
	4	5.169*	7.483*	−1.785
B.Product Market				
Gov. spending	1	1.000*	1.000*	1.000*
	2	2.186*	2.201*	2.2113*
	4	4.195*	4.284*	3.939*
Relative Output	1	−1.025*	−0.674*	−1.936*
(Y^T/Y^N)	2	−2.240*	−1.764*	−3.405*
	4	−4.547*	−4.293*	−5.389*
Relative Price	1	1.063*	1.052*	0.655
(P^N/P^T)	2	3.416*	3.312*	2.246
	4	7.984*	8.340*	4.023
C.Labor Reallocation				
Gov. spending	1	1.000*	1.000*	1.000*
	2	2.207*	2.199*	2.198*
	4	4.337*	4.304*	4.417*
Mobility Indicator	1	0.304*	0.163*	0.851*
(LR)	2	0.754*	0.482*	1.772*
	4	1.110*	0.824*	2.191*
Relative Wage	1	0.939*	1.320*	−0.687
(W^N/W^T)	2	2.667*	3.603*	−1.307
	4	5.222*	7.683*	−5.248

Notes: Horizon measured in year units. * denote significance at 10% level. Standard errors are bootstrapped with 10000 replications.

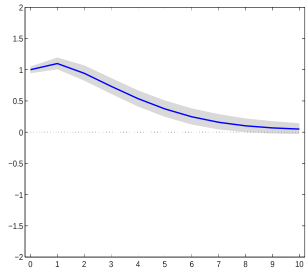
from one sector to another. Moreover, the responses of the relative wage shown in panels A and C are similar and and thus do not merit additional comments.

For reasons of space, figures in section 2 restrict attention to the responses of selected variables which are included in the VAR models. In this section, we document the effects of an exogenous fiscal shock on all variables which are included in the four specifications of VAR models:

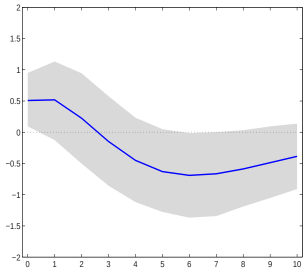
- $z_{it} = [g_{it}, y_{it}, l_{it}, je_{it}, w_{C,it}]$ and $z_{it} = [g_{it}, y_{it}, l_{it}, ca_{it}, w_{C,it}]$ (see Fig. 10, columns 1 and 2 resp.);
- $z^T_{it} = \left[g_{it}, y^T_{it}, l^T_{it}, w^T_{C,it}\right]$, $z^N_{it} = \left[g_{it}, y^N_{it}, l^N_{it}, w^N_{C,it}\right]$, $z^{S,T}_{it} = \left[g_{it}, \nu^{Y,T}_{it}, \nu^{L,T}_{it}, w^T_{C,it}\right]$, and $z^{S,N}_{it} = \left[g_{it}, \nu^{Y,N}_{it}, \nu^{L,N}_{it}, w^N_{C,it}\right]$ (see Fig. 12, columns 1, 2, 3 and 4 resp.);
- $z^W_{it} = [g_{it}, l^T_{it} - l^N_{it}, \omega_{it}]$ and $z^P_{it} = [g_{it}, y^T_{it} - y^N_{it}, p_{it}]$ (see Fig. 13, columns 1 and 2 resp.);
- $z^W_{it} = [g_{it}, l^T_{it} - l^N_{it}, \omega_{it}]$ and $z^W_{it} = [g_{it}, LR_{it}(2), \omega_{it}]$ for the 'high' and 'low mobility' sub-samples (see Fig. 14, columns 1 and 2 resp.).



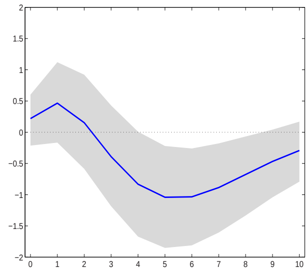
(a) Gov. spending, G



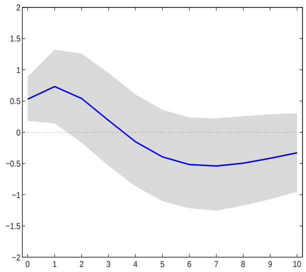
(b) Gov. spending, G



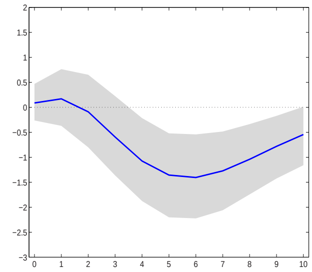
(c) Real GDP



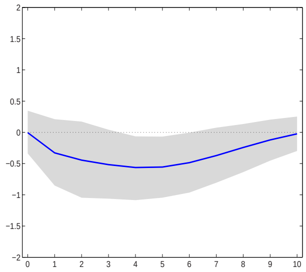
(d) Real GDP



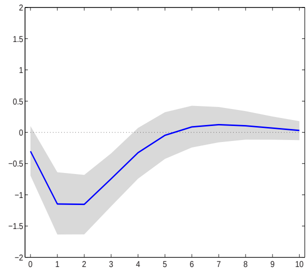
(e) Labor, L



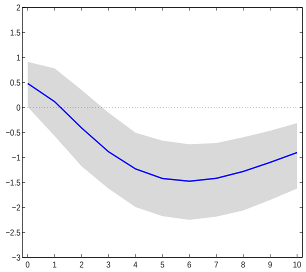
(f) Labor, L



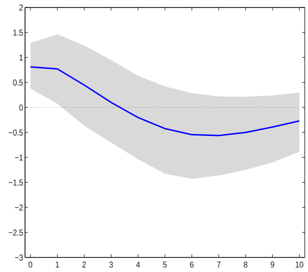
(g) Investment, JE



(h) Current Account, CA



(i) Real Wage, W/P_C



(j) Real Consumption Wage, W/P_C

Figure 10: Effects of Unanticipated Government Spending Shock on Aggregate Variables. Notes: Exogenous increase of government consumption by 1% of GDP. Aggregate variables include GDP (constant prices), total hours worked, private fixed investment, the current account and the real consumption wage. Horizontal axes indicate years. Vertical axes measure percentage deviation from trend in output units (government spending, GDP, investment, current account), percentage deviation from trend in labor units (total hours worked), percentage deviations from trend (real consumption wage). Results for baseline specification are displayed by solid lines with shaded area indicating 90 percent confidence bounds obtained by bootstrap sampling; sample: 16 OECD countries, 1970-2007, annual data.

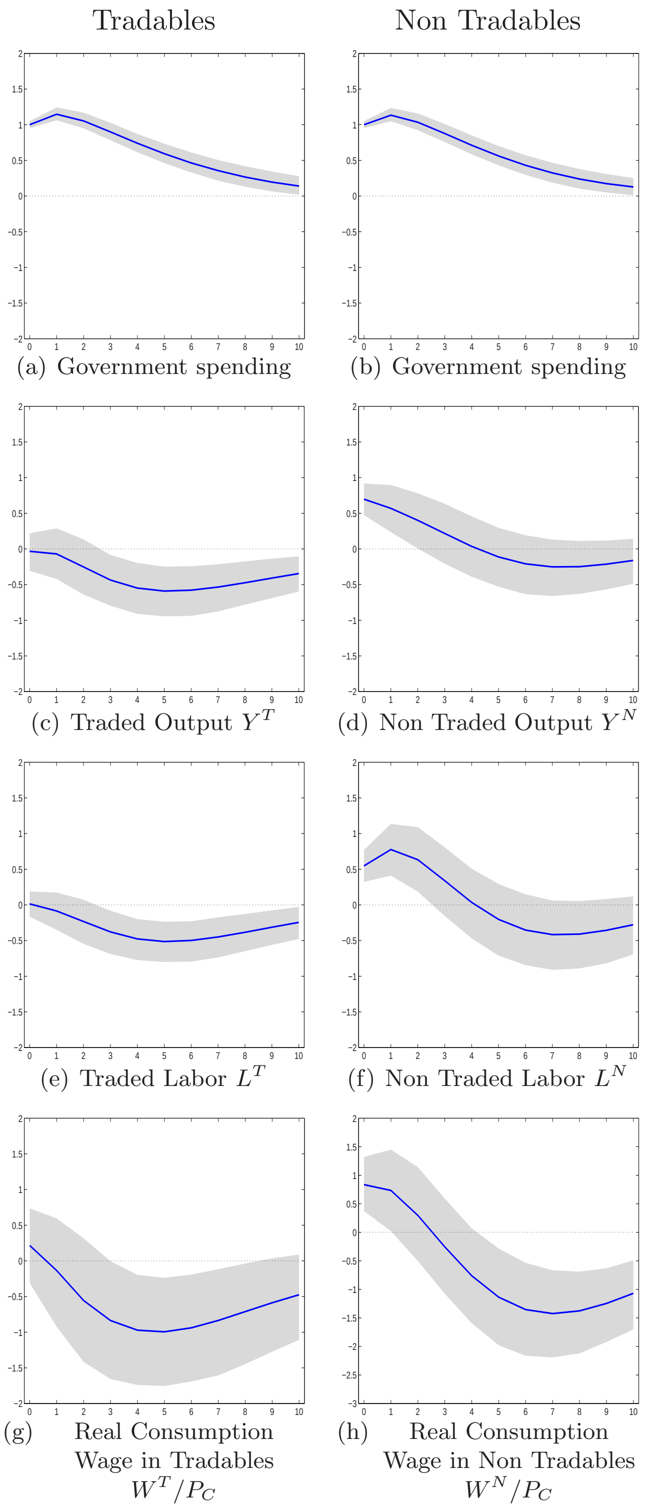
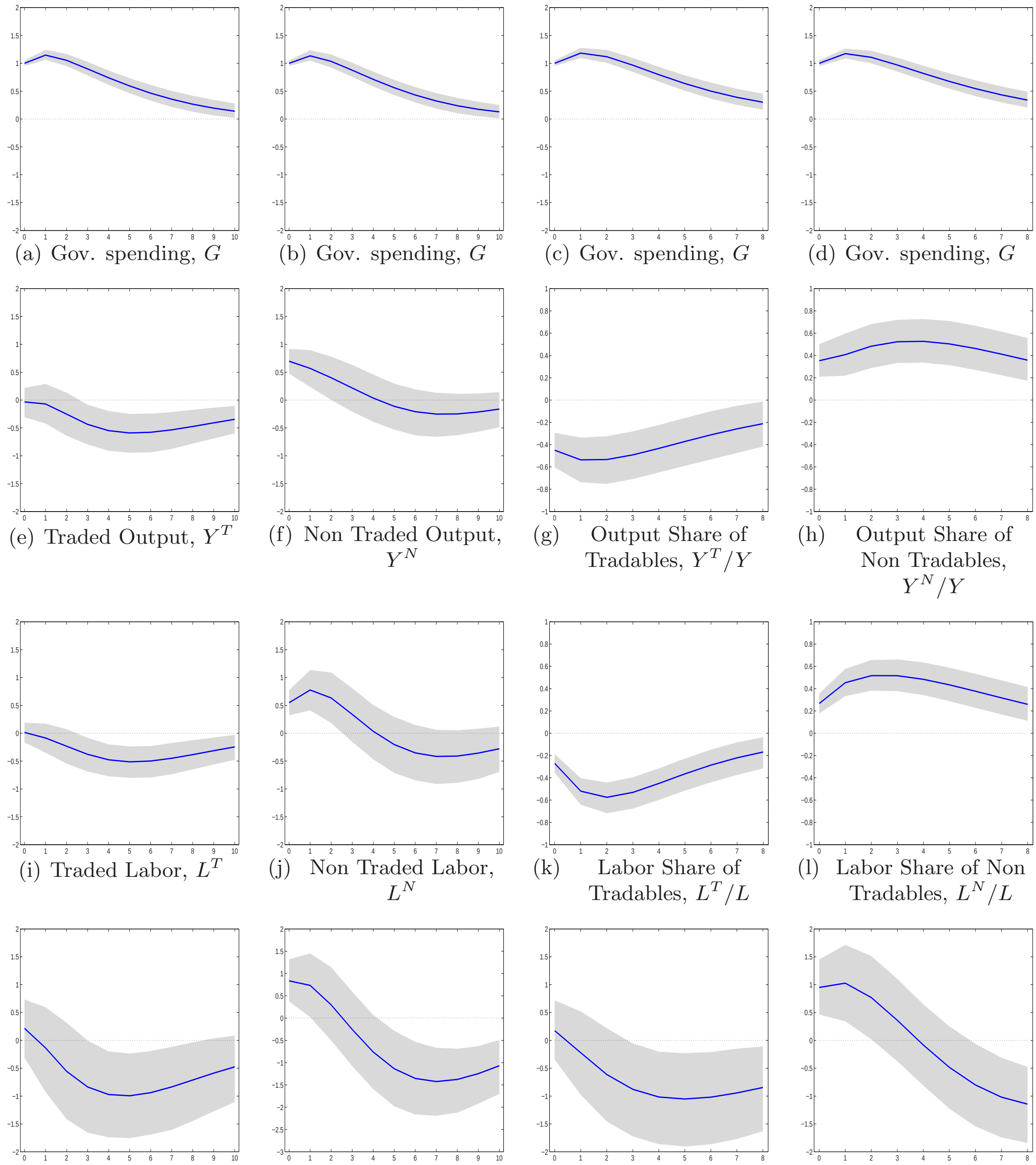


Figure 11: Effects of Unanticipated Government Spending Shock on Sectoral Variables. Notes: Exogenous increase of government consumption by 1% of GDP. Sectoral variables include sectoral valued added at constant prices, sectoral hours worked, and real consumption sectoral wages. Horizontal axes indicate years. Vertical axes measure percentage deviation from trend in output units (sectoral output), percentage deviation from trend in labor units (sectoral labor), percentage deviation from trend (real consumption sectoral wages). Results for baseline specification are displayed by solid lines with shaded area indicating 90 percent confidence bounds obtained by bootstrap sampling; sample: 16 OECD countries, 1970-2007, annual data.



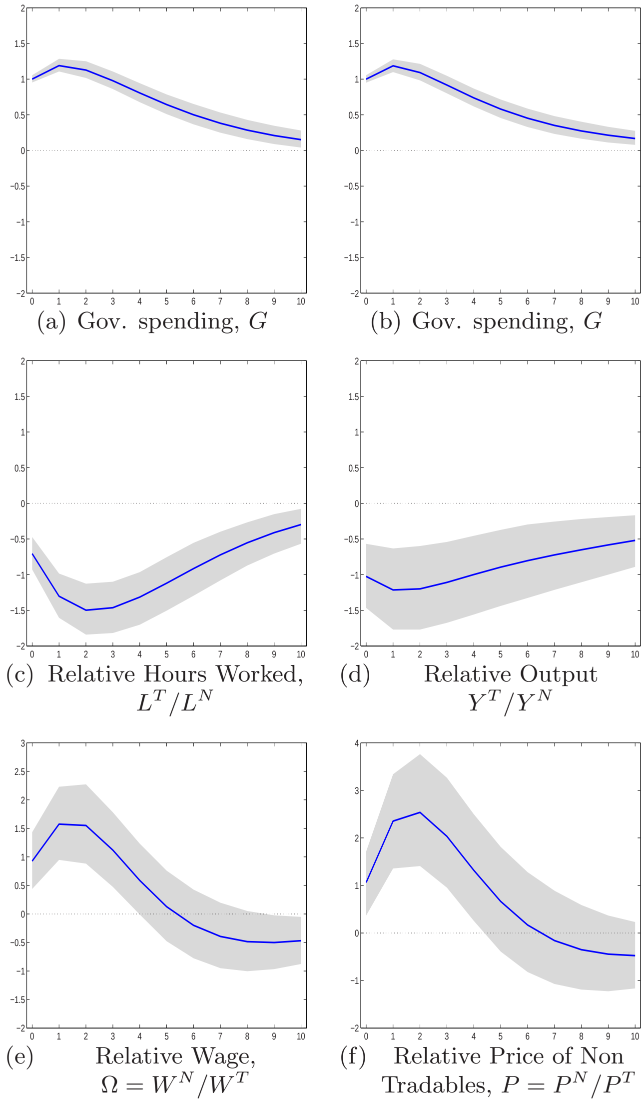
(a) Gov. spending, G (b) Gov. spending, G (c) Gov. spending, G (d) Gov. spending, G

(e) Traded Output, Y^T (f) Non Traded Output, Y^N (g) Output Share of Tradables, Y^T/Y (h) Output Share of Non Tradables, Y^N/Y

(i) Traded Labor, L^T (j) Non Traded Labor, L^N (k) Labor Share of Tradables, L^T/L (l) Labor Share of Non Tradables, L^N/L

(m) Real Consumption Wage in Tradables, W^T/P_C (n) Real Consumption Wage in Non Tradables, W^N/P_C (o) Real Consumption Wage in Tradables, W^T/P_C (p) Real Consumption Wage in Non Tradables, W^N/P_C

Figure 12: Effects of Unanticipated Government Spending Shock on Sectoral Variables. Notes: Exogenous increase of government consumption by 1% of GDP. Sectoral variables include sectoral valued added at constant prices, sectoral hours worked, sectoral labor and sectoral output shares, and real consumption sectoral wages. Horizontal axes indicate years. Vertical axes measure percentage deviation from trend in output units (sectoral output, sectoral output share), percentage deviation from trend in labor units (sectoral labor, sectoral labor share), percentage deviations from trend (real consumption sectoral wages). Results for baseline specification are displayed by solid lines with shaded area indicating 90 percent confidence bounds obtained by bootstrap sampling; sample: 16 OECD countries, 1970-2007, annual data.

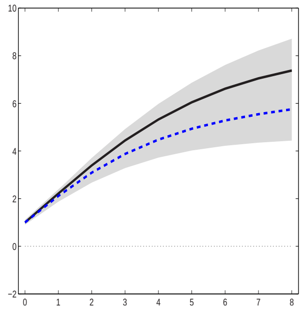


(a) Gov. spending, G (b) Gov. spending, G

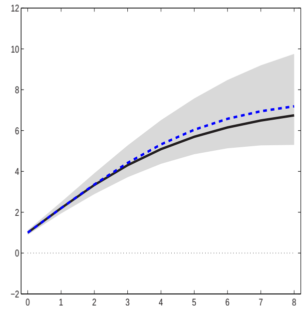
(c) Relative Hours Worked, L^T/L^N (d) Relative Output Y^T/Y^N

(e) Relative Wage, $\Omega = W^N/W^T$ (f) Relative Price of Non Tradables, $P = P^N/P^T$

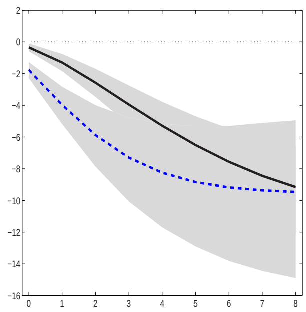
Figure 13: Effects of Unanticipated Government Spending Shock on Relative Price and Relative Wage. Notes: Exogenous increase of government consumption by 1% of GDP. Sectoral variables include hours worked of tradables in terms of non tradables, the relative wage, output of tradables in terms of non tradables, the relative price of non tradables. Horizontal axes indicate years. Vertical axes measure deviations from trend (ratio of traded value added to non traded value added, ratio of hours worked of tradables to hours worked of non tradables), and percentage deviations from trend (relative price, relative wage). Results for baseline specification are displayed by solid lines with shaded area indicating 90 percent confidence bounds obtained by bootstrap sampling; sample: 16 OECD countries, 1970-2007, annual data.



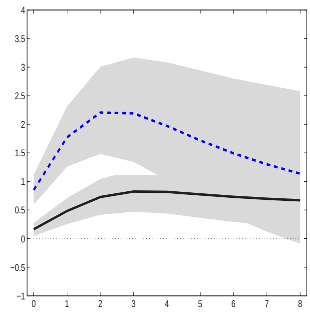
(a) Gov. spending, G



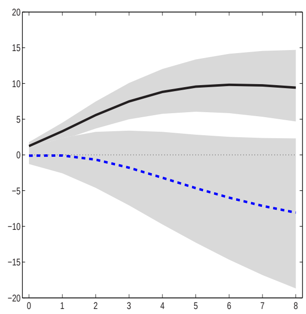
(b) Gov. spending, G



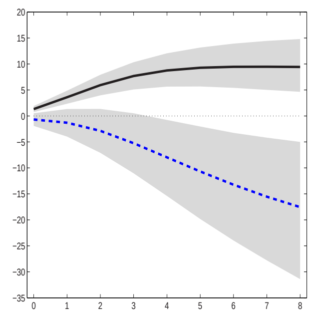
(c) Relative Hours Worked, L^T/L^N



(d) Labor Reallocation



(e) Relative Wage, $\Omega = W^N/W^T$



(f) Relative Wage, $\Omega = W^N/W^T$

Figure 14: Effects of Unanticipated Government Spending Shock on Labor Reallocation across Sectors. Notes: Exogenous increase of government consumption by 1% of GDP. Sectoral variables include hours worked of tradables in terms of non tradables, the relative wage, the intersectoral labor reallocation index. Horizontal axes indicate years. Vertical axes measure percentage deviation from trend in labor units (intersectoral labor reallocation index), deviations from trend (ratio of hours worked of tradables to hours worked of non tradables), and percentage deviations from trend (relative wage). Panels report cumulative responses for the 'high mobility' and the 'low mobility'countries' group in the black solid line and the blue dashed line, respectively, with shaded area indicating 90 percent confidence bounds obtained by bootstrap sampling; sample: 16 OECD countries, 1970-2007, annual data.

B.2 Robustness Check: Sectoral Classification

This section explores the robustness of our findings to the classification of the eleven 1-digit ISIC-rev.3 industries as tradables or non tradables. When we conduct the robustness analysis, we modify the baseline classification in a number of ways to ensure that some industries with specific characteristics are not driving the results. In particular, the classification of items "Wholesale and Retail Trade", "Hotels and Restaurants", "Transport, Storage and Communication", "Financial Intermediation" and "Real Estate, Renting and Business Services" may display some ambiguity. In order to address this issue, we re-estimate the various VAR specifications for different classifications in which one of the five above industries initially marked as tradable (non tradable resp.) is classified as non tradable (tradable resp.), all other industries staying in their original sector. In doing so, the classification of only one industry is altered, allowing us to see if the results are sensitive to the inclusion of a particular industry in the traded or the non traded sector. The baseline and the five alternative classifications considered in this exercise are shown in Table 13.

Table 13: Robustness check: Classification of Industries as Tradables or Non Tradables

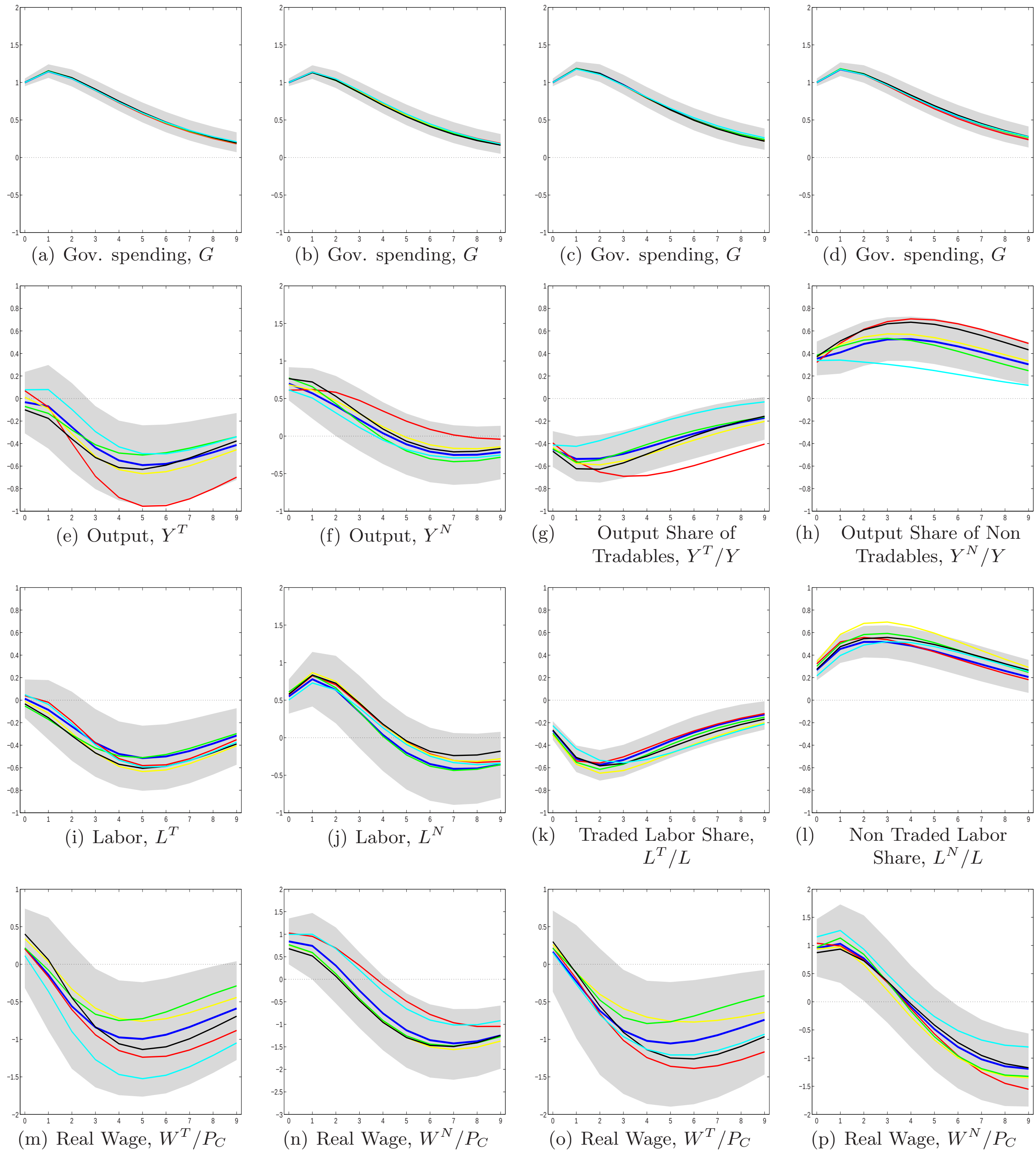
	KLEMS code	Classification					
		Baseline	#1	#2	#3	#4	#5
Agriculture, Hunting, Forestry and Fishing	AtB	T	T	T	T	T	T
Mining and Quarrying	C	T	T	T	T	T	T
Total Manufacturing	D	T	T	T	T	T	T
Electricity, Gas and Water Supply	E	N	N	N	N	N	N
Construction	F	N	N	N	N	N	N
Wholesale and Retail Trade	G	N	**T**	N	N	N	N
Hotels and Restaurants	H	N	N	**T**	N	N	N
Transport, Storage and Communication	I	T	T	T	**N**	T	T
Financial Intermediation	J	T	T	T	T	**N**	T
Real Estate, Renting and Business Services	K	N	N	N	N	N	**T**
Community Social and Personal Services	LtQ	N	N	N	N	N	N
Color line in Fig. 15 and 16		blue	red	yellow	green	black	cyan

Notes: T stands for the Traded sector and N for the Non traded sector.

Figures 15 and 16 report the responses of variables of interest to an exogenous increase in government spending by one percent of GDP. The solid blue line shows results for the baseline classification while the responses for alternative classifications are shown in the five colored lines. The last line of Table 13 provides the matching between the color line and the classification between tradables and non tradables. In each panel, the shaded area corresponds to the 90% confidence bounds.[60] Figure 15 contrasts the responses of sectoral output (Y^j), sectoral labor (L^j), sectoral output shares (Y^j/Y), sectoral labor shares (L^j/L), real consumption sectoral wages (W^j/P_C) for the baseline classification with those obtained for alternative classifications of industries as tradables or non tradables. Alternative responses are fairly close to those for the baseline classification as they lie within the confidence interval (for the baseline classification) for almost all the selected horizons (8 years). Figure 16 reports the effects of an exogenous increase in government consumption by 1% of GDP on the ratio of sectoral output (Y^T/Y^N), sectoral labor (L^T/L^N), the intersectoral labor reallocation index (LR), the relative price (P) and the relative wage (Ω). For LR, P and Ω, the responses are remarkably similar across the baseline and alternative classifications. While the pattern of the dynamic adjustment of Y^T/Y^N is similar across all classifications, the decline in output of tradables relative to non tradables is more pronounced when the industry "Wholesale and Retail Tarde" is treated as tradables (classification #1). We can also notice some differences in responses of L^T/L^N across the baseline and the five alternative classifications. For specifications #1 and #5, the response of L^T/L^N does not lie within the confidence interval of the baseline. Yet, across all classifications, L^T/L^N declines significantly on impact, and stay below trend for a number of periods. By and large, our main

[60]We do not report the responses for aggregate variables included since these variables, by construction, are unsensitive to the definition of traded and non traded sectors.

findings hold and remain unsensitive to the classification of one specific industry as tradable or non tradable; in sum, the specific treatment of "Wholesale and Retail Trade", "Hotels and Restaurants", "Transport, Storage and Communication", "Financial Intermediation" and "Real Estate, Renting and Business Services" does not drive the results.



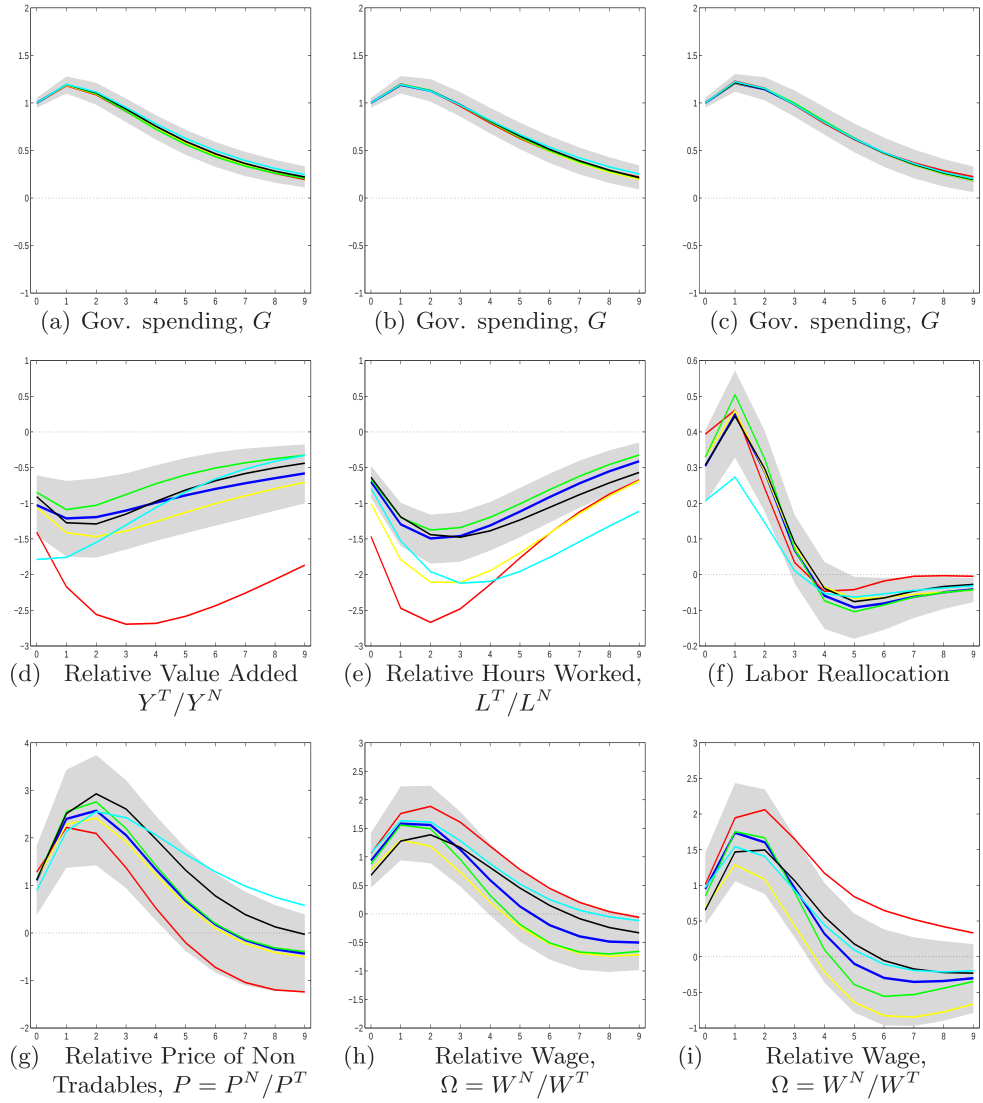
(a) Gov. spending, G (b) Gov. spending, G (c) Gov. spending, G (d) Gov. spending, G

(e) Output, Y^T (f) Output, Y^N (g) Output Share of Tradables, Y^T/Y (h) Output Share of Non Tradables, Y^N/Y

(i) Labor, L^T (j) Labor, L^N (k) Traded Labor Share, L^T/L (l) Non Traded Labor Share, L^N/L

(m) Real Wage, W^T/P_C (n) Real Wage, W^N/P_C (o) Real Wage, W^T/P_C (p) Real Wage, W^N/P_C

Figure 15: Sensitivity of the Effects of Unanticipated Government Spending Shock on Sectoral Variables to the Classification of Industries as Tradable or Non Tradable. Notes: The blue line shows results for the baseline classification. The red line and the yellow line show results when 'Whole and retail traded' and 'Hotels and restaurants' are treated as tradables, respectively. The green line and the black line show results when 'Transport, storage and communication' and 'Financial intermediation' are classified as tradables, respectively. The cyan line reports results when 'Real Estate, renting and business services' is treated as tradables.



(a) Gov. spending, G (b) Gov. spending, G (c) Gov. spending, G

(d) Relative Value Added Y^T/Y^N (e) Relative Hours Worked, L^T/L^N (f) Labor Reallocation

(g) Relative Price of Non Tradables, $P = P^N/P^T$ (h) Relative Wage, $\Omega = W^N/W^T$ (i) Relative Wage, $\Omega = W^N/W^T$

Figure 16: Sensitivity of the Effects of Unanticipated Government Spending Shock on Relative Price and Relative Wage to the Classification of Industries as Tradable or Non Tradable. Notes: The blue line shows results for the baseline specification. The red line and the yellow line show results when 'Whole and retail traded' and 'Hotels and restaurants' are treated as tradables, respectively. The green line and the black line show results when 'Transport, storage and communication' and 'Financial intermediation' are classified as tradables, respectively. The cyan line reports results when 'Real Estate, renting and business services' is treated as tradables.

B.3 Robustness Check: Excluding the Public Sector

As an additional robustness check, we exclude the industry "Community Social and Personal Services" from the non tradable industries' set. This robustness analysis is based on the presumption that among the eleven industries provided by the EU KLEMS and STAN databases, this industry is government-dominated. While this exercise is interesting on its own as it allows us to explore the size of the impact of a government spending shock on the business sector, we also purge for the potential and automatic link between non traded output and public spending because government purchases (to the extent that the government is the primary purchaser of goods from this industry) account for a significant part of non traded value added.[61]

Figures 17-19 report the effects of an exogenous increase in government consumption by 1% of GDP for the whole economy (baseline) together with the responses on the business sector (i.e., the public sector is excluded). In each case, the blue line reports the point estimate for the whole economy (with its 90% confidence interval) while the black line shows the point estimate for the business sector (i.e., the industry "Community Social and Personal Services" is excluded). Figure 17 shows the results of a rise in government consumption on GDP, hours worked, investment, the current account and the real consumption wage. We can notice that the dynamic adjustment of hours worked to an exogenous increase in government consumption is somewhat sensitive to the exclusion of the public sector. More precisely, when the public sector is excluded, hours worked increase less in Fig. 17(e) or even may decline on impact as displayed in Fig. 17(f). Whether we consider the whole economy or the business sector, the dynamic adjustment of hours worked displays a similar pattern whether "Community Social and Personal Services" is included or omitted: hours worked decline gradually before starting to recover after 5 years.

Figure 18 shows the results of a rise in government consumption by 1% of GDP on sectoral quantities, on sectoral labor and sectoral output shares, along with real consumption sectoral wages. In each panel, the blue solid line shows the results for the whole economy while the black solid line reports responses for the business sector. When excluding the public sector, we can notice that the contraction in hours worked and output of tradables is somewhat mitigated while the expansionary effect on non tradables is moderated. By and large, the shape of the dynamic adjustment of sectoral variables are similar and mostly lie within the confidence bounds of the baseline specification (i.e., for the whole economy). The third and fourth columns report the dynamic adjustment of output and labor shares of tradables and non tradables. As for sectoral output and sectoral labor in levels, the responses of sectoral output relative to GDP (in real terms) are mitigated when excluding the public sector. However, the conclusions we reach in the main text remain valid. In all instances, whether we use labor or output, the share of tradables falls while the share of non tradables rises. It is worthwhile mentioning that the differences in quantitative adjustments for output shares can be mostly attributed to the modifications of the initial share of each sector in terms of labor or total output. Technically, the responses of sectoral shares are measured as percentage deviation from trend in total output units for sectoral output shares or alternatively as percentage deviation from trend in total hours worked units for sectoral labor shares. Thus, percentage deviations from trend are multiplied by the corresponding share of sector j in the whole economy (for the baseline scenario) or alternatively in the business sector (for the alternative scenario where the industry "Community Social and Personal Services" is excluded). Since the initial share of non tradables is reduced when "Community Social and Personal Services" is excluded, the magnitude of the responses of labor and output share of non tradables are mitigated as well. In the baseline, non traded output and traded output as a share of GDP are 0.60 and 0.40 respectively, while in the alternative scenario where "Community Social and Personal Services" is excluded, the corresponding shares are 0.30 and 0.70. Results without these corrections (not shown) reveal that the differences in the responses of Y^T/Y and Y^N/Y across the two scenarios turn out to be substantially smaller. In the light of this result, it is unlikely that the omitted

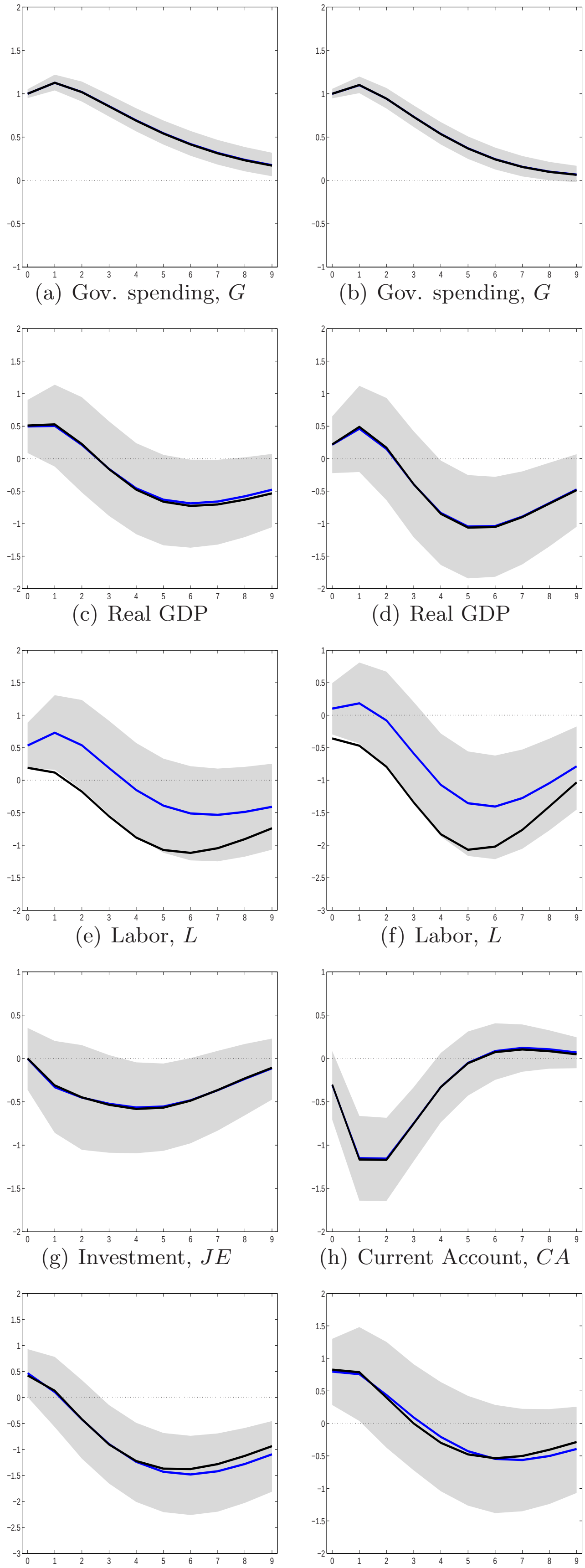
[61] This exercise has been conducted by Benetrix and Lane [2010] and Beetsma, Giuliodori, and Klaassen [2008], among others, in order to deal with the potential endogeneity of government purchases with respect to output.

industry plays a major role in explaining the responses of the output shares of tradables and non tradables to an increase in government spending.

Finally, Figure 19 compares the responses with and without the industry "Community Social and Personal Services" for the ratio of sectoral quantities (i.e., Y^T/Y^N, L^T/L^N), labor reallocation (LR), the relative price (P) and the relative wage (Ω). When excluding "Community Social and Personal Services", we find that the positive responses of the relative price of non tradables and the relative wage to an exogenous increase in government consumption are more pronounced and display more persistence over time. Because prices and wages are not really determined by the interplay of supply and demand in the public sector, it is not surprising that excluding this sector tends to magnify the responses of the relative wage and the relative price to a fiscal shock. While the ratio of hours worked of tradables relative to non tradables displays a similar magnitude, we may notice that the shift in the ratio of sectoral output is much more pronounced on impact and along the adjustment when we exclude "Community Social and Personal Services". As mentioned above, this behavior is mostly driven by the initial share of tradables which increases sharply.[62] Otherwise, the difference between the two instances would have been much smaller.

To conclude, the results presented in Figures 17-19 show that the conclusions which are drawn in the main text on the basis of the responses to an exogenous fiscal shock when we consider the whole economy remain valid when the industry "Community Social and Personal Services" is excluded.

[62] Recall that the percentage deviation from trend of Y^T/Y^N is multiplied by $\frac{P^T Y^T}{P^N Y^N}$ in order to express the result in percentage points and in the same units. For the baseline scenario (whole economy), the ratio Y^T/Y^N averages to 0.68. When "Community Social and Personal Services" is excluded, the ratio goes up to 2.40.



(a) Gov. spending, G (b) Gov. spending, G

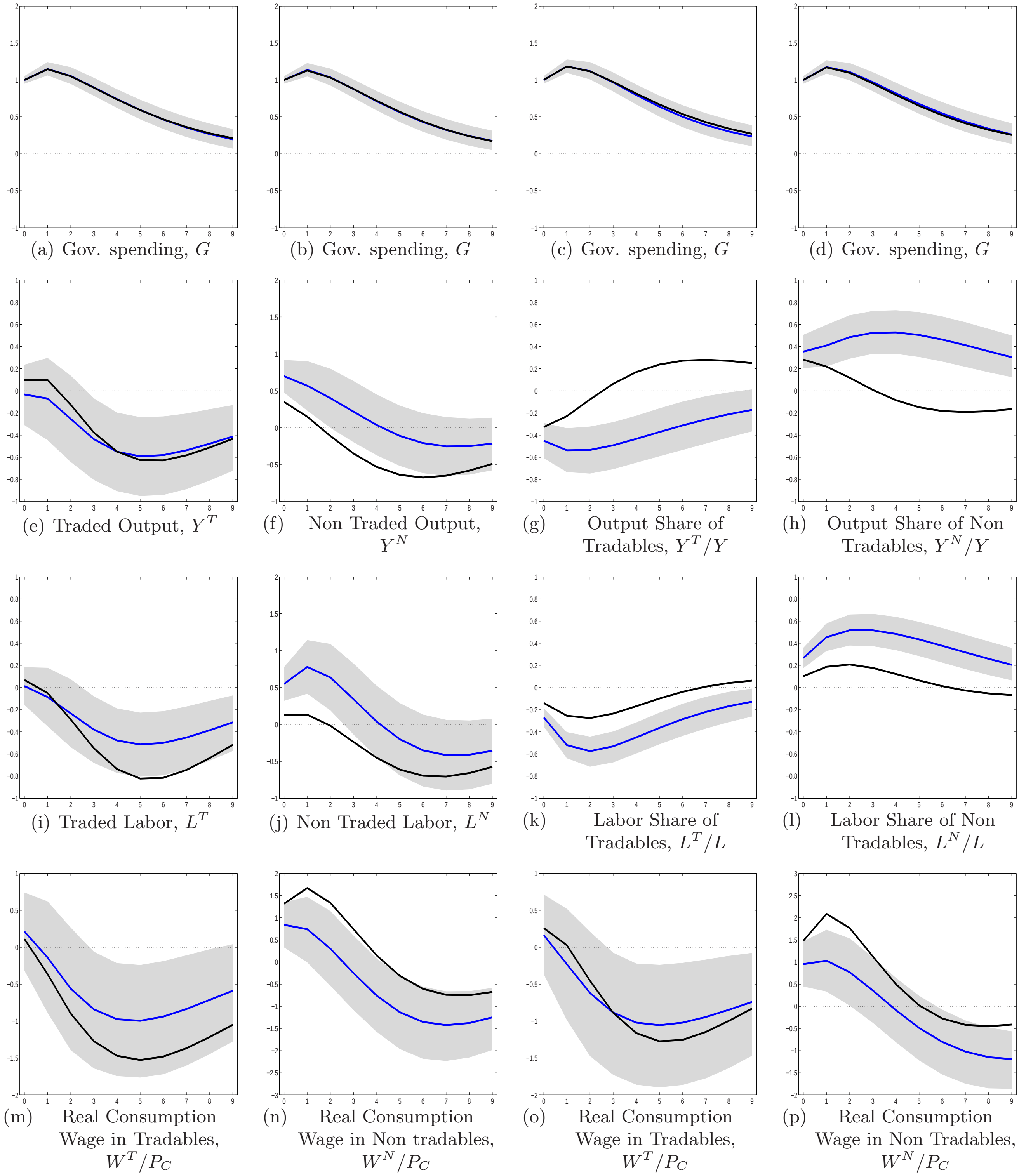
(c) Real GDP (d) Real GDP

(e) Labor, L (f) Labor, L

(g) Investment, JE (h) Current Account, CA

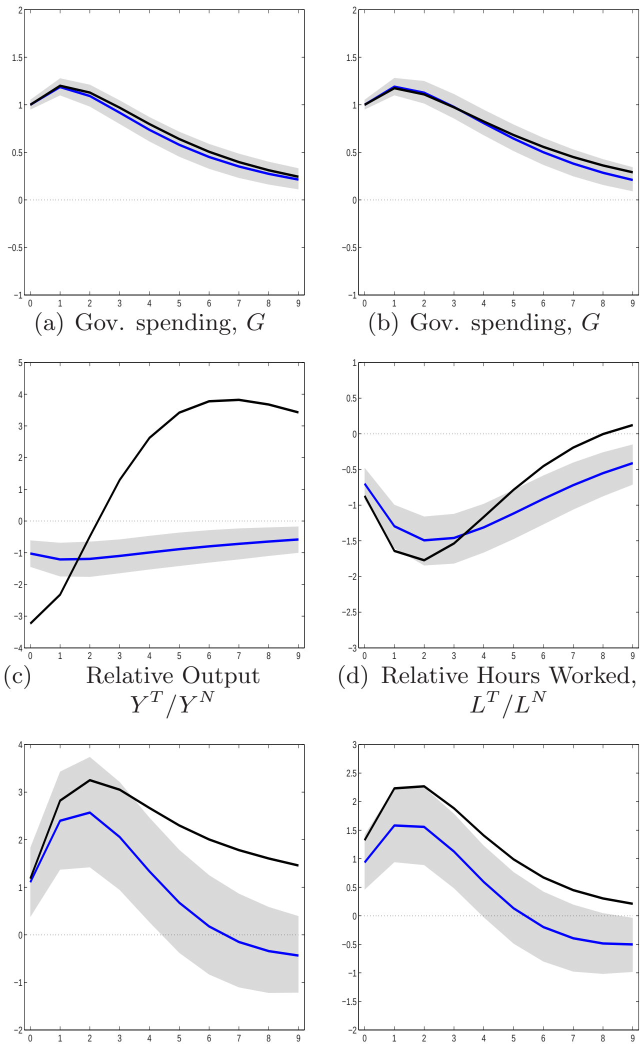
(i) Real Consumption Wage, W/P_C (j) Real Consumption Wage, W/P_C

Figure 17: Sensitivity of the Effects of Unanticipated Government Spending Shock on Aggregate Variables to Exclusion of the Public Sector. Notes: Impulse response functions to an exogenous increase in real government spending by one percent of GDP. Blue line: all sectors; shaded areas: 90 percent confidence intervals; black line: without "Community Social and Personal Services".



(a) Gov. spending, G
(b) Gov. spending, G
(c) Gov. spending, G
(d) Gov. spending, G
(e) Traded Output, Y^T
(f) Non Traded Output, Y^N
(g) Output Share of Tradables, Y^T/Y
(h) Output Share of Non Tradables, Y^N/Y
(i) Traded Labor, L^T
(j) Non Traded Labor, L^N
(k) Labor Share of Tradables, L^T/L
(l) Labor Share of Non Tradables, L^N/L
(m) Real Consumption Wage in Tradables, W^T/P_C
(n) Real Consumption Wage in Non tradables, W^N/P_C
(o) Real Consumption Wage in Tradables, W^T/P_C
(p) Real Consumption Wage in Non Tradables, W^N/P_C

Figure 18: Sensitivity of the Effects of Unanticipated Government Spending Shock on Sectoral Variables to Exclusion of the Public Sector. Notes: Impulse response functions to an exogenous increase in real government spending by one percent of GDP. Blue line: all sectors; shaded areas: 90 percent confidence intervals; black line: without "Community Social and Personal Services".



(a) Gov. spending, G

(b) Gov. spending, G

(c) Relative Output Y^T/Y^N

(d) Relative Hours Worked, L^T/L^N

(e) Relative Price of Non Tradables, $P = P^N/P^T$

(f) Relative Wage, $\Omega = W^N/W^T$

Figure 19: Sensitivity of the Effects of Unanticipated Government Spending Shock on Relative Price and Relative Wage to Exclusion of the Public Sector. Notes: Impulse response functions to an exogenous increase in real government spending by one percent of GDP. Blue line: all sectors; shaded areas: 90 percent confidence intervals; black line: without "Community Social and Personal Services".

B.4 Robustness Check: Identifying Assumption of Government Spending Shocks

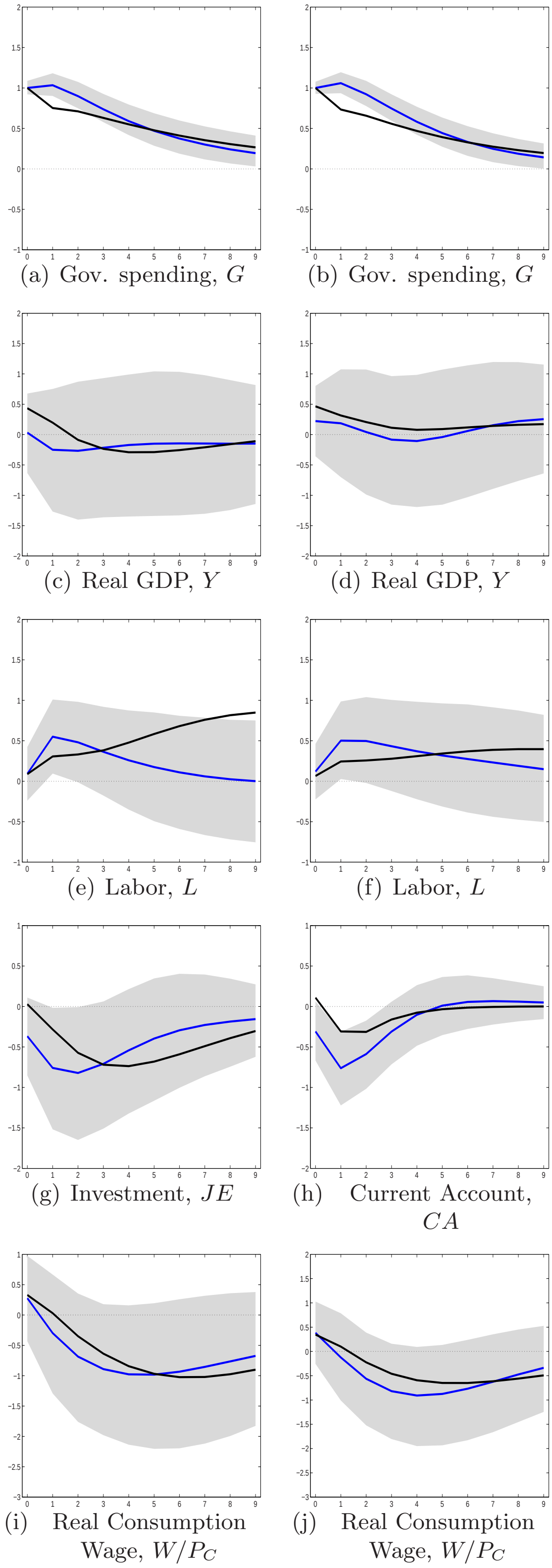
Like earlier studies, we adopt the identifying assumption of government spending shocks proposed by Blanchard and Perotti [2002] who assume that there is no contemporaneous response of government spending to macroeconomic aggregates, i.e. that government spending is predetermined. As summarized by Born and Müller [2012]: 'This requires that government spending does i) neither respond automatically to the economy, ii) nor that it is adjusted in a discretionary manner within the period. The first requirement is likely to be satisfied if government spending does not include transfers, but only government consumption and investment (a commonly used definition of government spending). Whether the second requirement is satisfied depends on the extent of decision lags in the policy process and thus on the data frequency'. While the identifying assumption is expected to hold for quarterly data, its fulfilment is less compelling when imposed at annual frequency. Recently, Beetsma, Giuliodori and Klaassen [2008] and Born and Muller [2012] provide evidence that imposing a zero within-year response of government spending to output to identify an annual SVAR is a reasonable identifying restriction for a panel of seven OECD countries and the US, respectively. While these conclusions are reassuring, we provide below additional support for our identifying assumption in annual data. We thus ask whether the assumption that government spending is predetermined within the year by using the largest available subset of the countries in our dataset for which we have sufficient quarterly data. For this purpose, we compare the annualized impulse responses from the quarterly VAR model in panel format with those obtained from a VAR model estimated in panel formal on annual data. Because sectoral data are only available at an annual frequency. we restrict the exercise to the VAR models including aggregate variables such as government spending, aggregate GDP, total hours worked, investment, the current account and the real consumption wage. We proceed below in two stages. First, we briefly discuss our data. Second, we compare results obtained on the basis of annual with those obtained with quarterly data.

Data are taken from the OECD Economic Outlook database. The country sample is Australia (AUS), Austria (AUT), Canada (CAN), France (FRA), Italy (ITA), Japan (JPN), the Netherlands (NLD), Sweden (SWE), the United Kingdom (GBR), and the United States (USA), for which quarterly and annual macroeconomic data are available. Given OECD quarterly statistics data, the country and period coverage (identical for the quarterly and annual data sets) is: AUS (1979Q1-2007Q4), AUT (1990Q1-2007Q4), CAN (1981Q1-2007Q4), FRA (1973Q1-2007Q4), ITA (1970Q1-2007Q4), JPN (1970Q1-2007Q4), NLD (1970Q1-2007Q4), SWE (1975Q1-2007Q4), GBR (1972Q1-2007Q4) and USA (1970Q1-2007Q4). Sources and data construction at a quarterly frequency are as follows:

- **Government spending**: real government final consumption expenditure (CGV). Source: OECD Economic Outlook Database.
- **Gross domestic product**: real gross domestic product (GDPV). Source: OECD Economic Outlook Database.
- **Labor**: hours worked per employee, total economy. Source: OECD Economic Outlook Database.
- **Private fixed investment**: real private non-residential gross fixed capital formation (IBV). Source: OECD Economic Outlook Database.
- **Current account**: current account balance (in % of GDP). Source: OECD Economic Outlook Database.
- **Real Consumption wage**: nominal wage rate (total economy) divided by the consumer price index (CPI). Sources: OECD Economic Outlook Database for the nominal wage and OECD Prices and Purchasing Power Parities for the consumer price index.

All data are seasonally adjusted and divided by the population, except for the current account balance and the real consumption wage. We consider per capita variables, and thus divide quantities by the working age population (15-64 years old) provided by OECD Economic Outlook Database (data for the population at quarterly frequency were interpolated from annual data). For government spending, GDP and investment, we directly use the volumes as reported by the OECD (the series are deflated with their own deflators).

In estimating the VAR models on quarterly data, we allow for four lags while the number of lags is set to two when data are at an annual frequency. In order to investigate consistently whether the assumption that government spending is predetermined within the year, we impose the restriction that government spending is predetermined with the year (the quarter) to identify government spending shocks when the model is estimated in panel format on annual (quarterly) data. Figure 20 reports the responses for the variables of interest from the VAR model estimated on annual data shown in the blue solid line and on quarterly data shown in the black solid line. The blue and the black solid lines display the point estimate with shaded areas indicating 90% confidence bounds obtained when the VAR model is estimated on annual data. We take the panel VAR model on annual data as the baseline model. For purposes of comparability, we annualize the responses of the quarterly baseline models. While some differences can be observed, the annualized responses obtained from the quarterly model are fairly close to those obtained from the baseline model as responses lie within the confidence interval of the baseline model for almost all time horizons. It is worthwhile mentioning that following an exogenous increase in government consumption, total hours worked displays much more persistence when the panel VAR model is estimated on quarterly data than on annual data. Note that hours worked revert to its inial level after several decades. We can notice that investment and the current account do not respond to the fiscal shock on impact with quarterly data while they both gradually decline and stay below trend for several years. While the responses somewhat display some minor quantitative differences, the panel VAR evidence is similar whether we assume that government spending does not respond to the other variables included in the VAR model within the year or alternatively within the quarter. In sum, we can conclude that the assumption according to which the fiscal shock is exogenous within the year is not as restrictive as one might think.



(a) Gov. spending, G (b) Gov. spending, G

(c) Real GDP, Y (d) Real GDP, Y

(e) Labor, L (f) Labor, L

(g) Investment, JE (h) Current Account, CA

(i) Real Consumption Wage, W/P_C (j) Real Consumption Wage, W/P_C

Figure 20: Impulse Response Functions from the Panel VAR Model on Annual Data vs. Quarterly Data. Notes: Exogenous increase of government consumption by 1% of GDP. Aggregate variables include GDP (constant prices), total hours worked, private fixed investment, the current account and the real consumption wage. Horizontal axes indicate years. Vertical axes measure percentage deviation from trend in output units (government spending, GDP, investment, current account), percentage deviation from trend in labor units (total hours worked), percentage deviations from trend (real consumption wage). Results for baseline specification are displayed by blue lines with shaded area indicating 90 percent confidence bounds obtained by bootstrap sampling; sample: 16 OECD countries, 1970-2007, annual data. Blue line: response from the panel VAR model on annual data; black line: annualized impulse responses from the panel VAR model on quarterly data.

C Condition for the Government Spending Shock to be Biased toward Non Tradables

In this section, we provide more details about the interpretation of our empirical results.

C.1 Standard Definition of Government Spending Shocks Biased toward Non Tradables

In subsection 2.3, we interpret the rise in non traded output relative to traded output that we document empirically as the result of government spending shocks biased toward non tradables. In this subsection, we provide more details about our interpretation and the assumptions underlying this conjecture. The traded good is the numeraire and its price, P^T, is normalized to 1.

To begin with, we write down the market clearing conditions:

$$Y^N(t) = C^N(t) + J^N(t) + G^N(t), \tag{86a}$$

$$Y^T(t) = C^T(t) + J^T(t) + G^T(t) + NX(t), \tag{86b}$$

where Y^j is value added at constant prices in sector $j = N, T$, C^j and G^j stand for private and public consumption of good $j = N, T$, respectively, J^j corresponds to private investment in sector $j = N, T$, and NX is net exports. Summing value added at constant prices across sectors gives real GDP which we denote by Y_R:

$$Y_R(t) = Y^T(t) + PY^N(t), \tag{87}$$

where P is the price of non traded goods in terms of traded goods that is kept fixed in order to evaluate non traded value added at constant prices. Note that at the initial steady-state, real GDP and nominal GDP coincide, i.e., $Y_R = Y$.

Government spending, G, is the sum of public purchases on non traded goods, G^N, and traded goods, G^T:

$$G(t) = PG^N(t) + G^T(t). \tag{88}$$

We denote by $\omega_{G^N} = \frac{PG^N}{G}$ and $\omega_{G^T} = \frac{G^T}{G} = 1 - \omega_{G^N}$ the non tradable and tradable content of government spending. Assuming that the share ω_{G^j} is constant over time, eq. (88) can be rewritten as follows:

$$G(t) = \omega_{G^N} G(t) + \omega_{G^T} G(t), \tag{89}$$

with $\omega_{G^N} + \omega_{G^T} = 1$.

Below, we note by a hat the deviation of variable $X(t)$ relative to its initial level, X, in percentage:

$$\hat{X}(t) = \frac{X(t) - X}{X}. \tag{90}$$

Totally differentiating (89) and dividing by initial GDP, a rise in government spending is split into non tradadables and tradables in accordance with their respective shares:

$$\frac{dG(t)}{Y} = \omega_{G^N} \frac{dG(t)}{Y} + \omega_{G^T} \frac{dG(t)}{Y}. \tag{91}$$

A government spending shock is said to be biased toward non tradables if

$$\omega_{G^N} > \omega_{G^T}. \tag{92}$$

As will be useful later, we totally differentiate (88) and divide the resulting expression by initial GDP:

$$\frac{dG(t)}{Y} = \omega_G \omega_{G^N} \hat{G}^N(t) + \omega_G \omega_{G^T} \hat{G}^T(t). \tag{93}$$

where $\omega_G = \frac{G}{Y}$ stands for government consumption-to-GDP ratio. Combining eq. (91) and (93), we thus have:

$$\omega_G \omega_{G^j} \hat{G}^j(t) = \omega_{G^j} \frac{dG(t)}{Y}, \quad j = N, T. \tag{94}$$

Before investigating the impact of higher government spending on sectoral value added, it is convenient to denote by $\nu_Y^N = \frac{PY^N}{Y}$ the share of non tradables in GDP and $\nu^{Y,T} = \frac{Y^T}{Y}$ the share of tradables in GDP. Keeping private consumption, C^j, private investment, J^j, and net exports, NX, constant, totally differentiating market clearing conditions for non tradables and tradables described by (86a) and (86b), respectively, leads to:

$$\nu^{Y,N}\hat{Y}^N(t) = \omega_G \omega_{G^N} G^N(t), \tag{95a}$$

$$\nu^{Y,T}\hat{Y}^T(t) = \omega_G \omega_{G^T} G^T(t), \tag{95b}$$

where $\nu^{Y,T} = 1 - \nu^{Y,N}$. The LHS of eqs. (95), $\nu^{Y,j}\hat{Y}^j(t)$, corresponds to the deviation of value added in sector j relative to its initial steady-state value in percentage of initial GDP. Subtracting (95b) from (95a) allows us to relate the change in output of non tradables relative to tradables, both expressed in percentage points of GDP, to changes in sectoral government consumption:

$$\begin{aligned} \nu^{Y,N}\hat{Y}^N(t) - \nu^{Y,T}\hat{Y}^T(t) &= \omega_G \omega_{G^N} G^N(t) - \omega_G \omega_{G^T} G^T(t), \\ &= \left(\omega_{G^N} - \omega_{G^T}\right) \frac{dG(t)}{Y}, \end{aligned} \tag{96}$$

where use has been made of (94) to obtain the second line of eq. (96). In accordance with the definition (92), eq. (96) implies that non traded output increases relative to traded output when government spending is biased toward non tradables, i.e.,

$$\nu^{Y,N}\hat{Y}^N(t) - \nu^{Y,T}\hat{Y}^T(t) > 0, \quad \text{if} \quad \omega_{G^N} > \omega_{G^T}. \tag{97}$$

C.2 Stricter Definition of Government Spending Shocks Biased toward Non Tradables

In subsection 2.3 we document a second empirical fact which reveals that the share of non tradables in GDP (in real terms) increases while the share of tradables in GDP (in real terms) falls following a rise in government consumption. In this subsection, we relate the responses of sectoral output shares to changes in sectoral government spending.

To begin with, summing value added at constant prices across sectors, i.e., (86a) and (86a), and using the definition (87) leads to the standard accounting identity according to which GDP is equal to final expenditure:

$$Y_R(t) = P_C C(t) + P_J J(t) + G(t) + NX(t), \tag{98}$$

where P_C and P_J are the consumption and investment price index, respectively, C and J stand for private consumption and private investment in volume.

Keeping consumption and investment expenditure along with net exports fixed, totally differentiating (98) leads to:

$$\hat{Y}_R(t) = \omega_G \hat{G}(t) = \frac{dG(t)}{Y}. \tag{99}$$

Totally differentiating (87) leads to:

$$\hat{Y}_R(t) = \nu_Y^N \hat{Y}^N(t) + \nu_Y^T \hat{Y}^T(t), \tag{100}$$

where $\nu^{Y,j} = \frac{P^j Y^j}{Y}$, remembering that $P^T = 1$. Subtracting $\hat{Y}_R(t)$ from both sides of eq. (100) and using the fact that $\nu^{Y,T} = 1 - \nu_Y^N$ leads to:

$$\nu^{Y,N}\left(\hat{Y}^N(t) - \hat{Y}_R(t)\right) + \nu^{Y,T}\left(\hat{Y}^T(t) - \hat{Y}_R(t)\right) = 0. \tag{101}$$

The term $\nu^{Y,j}\left(\hat{Y}^j(t) - \hat{Y}_R(t)\right)$ corresponds to the deviation of sectoral output share in GDP relative to its initial value:

$$\nu^{Y,j}\left(\hat{Y}^j(t) - \hat{Y}_R(t)\right) = \nu^{Y,j}\hat{\nu}_Y^j(t). \tag{102}$$

To relate the response of the share of non tradables in GDP to changes in sectoral government consumption, we make use of eq. (95a) and eq. (99) which relate the change in output to changes in government spending:

$$\begin{aligned}\nu^{Y,N}\left(\hat{Y}^N - \hat{Y}_R\right) &= \omega_G \omega_{G^N} G^N(t) - \nu^{Y,N}\omega_G \hat{G}(t), \\ &= \omega_{G^N}\frac{dG(t)}{Y} - \nu^{Y,N}\frac{dG(t)}{Y}, \\ &= \left(\omega_{G^N} - \nu^{Y,N}\right)\frac{dG(t)}{Y}, \end{aligned} \quad (103)$$

where we use eq. (94) to obtain the second line of eq. (103). According to (103), the share of non tradables in GDP increases following a fiscal shock as long as the fraction of government expenditure spent on non traded goods, ω_{G^N}, is higher than that the share of non tradables in GDP, ν^N. Thus, a government spending shock is biased toward non tradables if:

$$\omega_{G^N} > \nu^{Y,N}. \quad (104)$$

Building on (92) and (104), there exists two definitions of government spending biased toward non traded goods. The first definition establishes that government spending is biased toward non traded goods if a larger fraction of public spending is spent on non traded traded goods than on traded goods. Such a definition implies that non traded output increases relative to traded output, as documented in Figure 2(c), as long as $\omega_{G^N} > \omega_{G^T}$. However, this definition does not take into account that non traded output accounts for a larger fraction of GDP. Thus, for the share of non tradables in GDP to increase, inequality (92) is a necessary but not sufficient condition. For the share of non tradables in GDP to increase, as documented in Figure 2(b), the fraction of government spending spent on non traded goods must exceed the share of non tradables in GDP, in line with the stricter inequality (104).

It is worth noting that for the increase in the GDP share of non tradables to materialize, resources must be reallocated away from the traded sector to the non traded sector. In other words, the fact that government spending is biased toward non tradables in accordance with the stricter definition (104) is sufficient as long as labor and/or capital can shift toward the non traded sector.

So far, we have investigated the response of the share of non tradables in real GDP to a rise in government spending by keeping the private sector's demand components fixed. We now investigate how much the responses of the private sector's demand components influence our results. To avoid unnecessary complications, we assume that the elasticity of substitution between tradables and non tradables is equal to one for both consumption and investment. Thus, consumption (investment) in non tradables is a fixed fraction α_C (α_J) of consumption (investment) expenditure, i.e., $P_C C$ ($P_J J$). First, log-linearizing (98) leads to the deviation from initial steady-state in percentage for real GDP, Y_R:

$$\hat{Y}_R(t) = \omega_C \hat{C}(t) + \omega_J \hat{J}(t) + \frac{dG(t)}{Y} + \frac{dNX(t)}{Y}, \quad (105)$$

where Y is initial real GDP. Totally differentiating (86a) leads to the deviation from initial steady-state in percentage for real GDP, Y^N:

$$\nu^{Y,N}\hat{Y}_N(t) = \alpha_C \omega_C \hat{C}(t) + \alpha_J \omega_J \hat{J}(t) + \omega_{G^N}\frac{dG(t)}{Y}. \quad (106)$$

Pre-multiplying (105) by $\nu^{Y,N}$, the initial response of the share of non tradables in real GDP to a government spending shock is:

$$\begin{aligned}\nu^{Y,N}\left(\hat{Y}^N(0) - \hat{Y}_R(0)\right) &= -\left(\nu^{Y,N} - \alpha_C\right)\omega_C \hat{C} - \left(\nu^{Y,N} - \alpha_J\right)\omega_J \hat{J} \\ &+ \left(\omega_{G^N} - \nu^{Y,N}\right)\frac{dG(0)}{Y} - \nu^{Y,N}\frac{dNX(0)}{Y}. \end{aligned} \quad (107)$$

Since $\nu^{Y,N}$ takes values which are close to both α_J and α_C, the response of the share of non tradables in real GDP is mostly affected by $\left(\omega_{G^N} - \nu^{Y,N}\right)$ along with the deficit in the balance of trade on impact. In sum, when taking into account the reaction of the private sector's demand components, the current account deficit triggered by the rise in government spending tends to reinforce the fact that the government spending shock is biased toward non tradables.

D More VAR Results and Robustness Check

In this section, we provide more details about the empirical and calibration strategy in the main text and we conduct several robustness checks:

- In subsection D.1, we provide evidence on the composition of government consumption and quantify the contribution shocks to government consumption on non traded goods to unanticipated changes in total government consumption. We also detail the source and construction of time series for sectoral government consumption. The conclusion that emerges is that shocks to public purchases of non traded goods account on average for about 90 percent of the forecast error variance of total government spending for horizons of 1 to 8 years for the whole sample and the US as well. This finding thus corroborates our conjecture that government spending shocks are strongly biased toward non traded goods. To calibrate our model, we estimate the first VAR model that includes government final consumption expenditure, real GDP, total hours worked, private investment, the real consumption wage, in order to identify unanticipated government spending shocks. Then, we estimate a VAR model in panel format on annual data that includes unanticipated government spending shocks ordered first, government final consumption expenditure, government consumption on non tradables, and government consumption on tradables. Impulse response functions for the two components of government final consumption expenditure we generate following a rise in government spending by 1% of GDP reveal that government consumption expenditure on non tradables accounts on average for 90% of increases in government consumption. This evidence thus indicates that the sectoral components of government final consumption expenditure increase roughly by the same amount than their share in government spending. Because data for government consumption by function are available over 1970-2007 for the U.S., we also estimate the same VAR models as in the main text and contrast dynamic effects on sectoral variables after an aggregate spending shock with those following a shock to government consumption of non tradables. We find empirically that the dynamic responses are very similar in terms of shape and magnitude.

- In subsection D.2, we conduct an elaborate investigation of the responses of components of government final consumption expenditure. Because a large part of unanticipated changes in government final consumption expenditure are due to an changes in public purchases of non tradables, we investigate the responses of its components as well. In the first part, following the existing literature, we consider two components in total government expenditure: the purchase of goods and services from the private sector, and the purchases of goods and services from the government sector which accounts for 60% of government final consumption expenditure. To investigate how these two components react to a government spending shock, we identify the unanticipated shock to total government expenditure and then estimate a VAR model that includes the identified shock ordered first and its two components. Estimated responses of the sub-components of government final consumption expenditure to our identified government spending shock reveal that government purchases of goods and services from the private sector is a major part of the variation in government spending over the first five years. More precisely, while the two components react positively to the fiscal shock, the increase in government purchases from the private sector accounts for 80% of the spending shock on impact. Conversely, the contribution of government purchases of government output to the spending shock increases over time and averages 55%. Then, we identify the shocks to the two components of government spending using Blanchard and Perotti's [2002] approach and estimate the sectoral effects of each identified shock. Whether we consider a wage or a non-wage government consumption shock, our main conclusions hold. Both shocks appreciate the relative price of non tradables and reallocate resources toward the non traded sector which increases its relative size. We may nevertheless note some differences quantitatively. The magnitude of the reallocation of labor across sectors along with changes in relative sector size are more pronounced following a wage government consumption shock. When we turn to components of government consumption non non tradables, we find that the identified government spending shock increases substantially individual government final consumption expenditure. The contribution of this component to the increase in government consumption of non tradables averages 77%. When we distinguish between defense and non-defense spending, we find that the former accounts for a small fraction (6% on average) of the increase in government consumption of non tradables.

- In subsection D.3, we contrast our results related to the sectoral effects of a government spending shock when differentiating between a traded and a non traded sector with those documented by earlier empirical studies. In particular, we conduct an elaborate analysis of the causes of the discrepancy in our results and those documented by Benetrix and Lane [2010] related to the response of traded output. Our empirical study reveals that the causes are twofold. First, when we restrict the set of countries to those we have in common with the authors' sample, we find that traded output increases on impact. Second, our analysis also indicates that when quantities are not scaled by the population, as in Benetrix and Lane [2010], then the rise in traded output becomes more persistent over time. The classification of industries between tradables or non tradables along with the VAR specification does not play any noticeable role in driving the discrepancy.

- In subsection D.4, we contrast our empirical results on aggregate effects of government spending shocks with those documented in the empirical literature.

- In subsection D.5, we conduct an investigation of the potential presence of anticipation effects, using alternative measures of forecasts for government spending. The former measure was provided by Born, Juessen and Müller [2013] and stems from the OECD, while the latter measure is taken from a dataset constructed by Fioramanti et al. [2016] where forecasts are performed by the European Commission. We use two alternative datasets as the former contains observations from 1986 to 2007 for all countries, while the latter provides a longer time horizon for a restricted set of countries. As is common in the literature, we alternatively include a forward-looking variable such as stock prices into the VAR model in order to control for potential fiscal foresight. First, we run Granger-causality tests and do not find that fiscal forecasts have any predictive power for our identified government spending shocks. Second, our main results are not altered by the inclusion of forecasts for government spending. We detect some differences quantitatively, however, when we include the OECD forecast for spending growth in the VAR model. More precisely, when we control for anticipation effects, the responses of sectoral output shares are more pronounced, while the appreciation in the relative price and the relative wage of non tradables are somewhat more muted.

- In subsection D.6, we address a potential concern related to the fact that the government spending shock may display noticeable differences across alternative VAR specifications. Such differences could potentially make the comparison of the effects of a government shock across sectors difficult. Because in the quantitative analysis we base our calibration on one unique government spending shock, such differences could potentially undermine the comparison of theoretical with empirical responses. Before summarizing the main conclusions of robustness exercises, it is worth mentioning that, in line with the current practice, to facilitate the interpretation of our results, we normalize the impulse responses so that government consumption rises by one percentage point of GDP on impact. Such a normalization thus makes the responses of economic variables directly comparable quantitatively across VAR models. Since we base the greatest part of our analysis and discussion on impact effects, potential problems caused by differences in the government spending shock could be mitigated. A straightforward check of the extent of differences of the government spending shock across VAR specifications is performed by contrasting impulse response functions for G. All of the empirical impulse response functions for G, and to a lesser extent the response of G we generate from estimates of the VAR model that includes the current account, lie within the 90% confidence bounds of the first IRF for G for all horizons. Moreover, the test we perform indicates that assumption that the point estimate for the response of G in the first VAR model is significantly different from that for alternative VAR models is strongly rejected. However, even if the magnitude and the shape of the government spending shock is similar across VAR specifications, different VAR models could pickup different structural government spending shocks. In order to investigate the extent of the discrepancy in the estimated government spending shock across VAR specifications, we perform several robustness exercises. In the first robustness exercise, we augment each VAR specification with the government spending shock identified in the first VAR model which is taken as the baseline in our quantitative analysis. Because the identification scheme is based on the assumption of delays between current output observation and the implementation of fiscal measures and we consider annual rather than quarterly data, we also identify the 'baseline' government spending shock on a quarterly basis. In the latter case, the set of countries is restricted to eight. It turns out that differences with baseline results are rather moderate when the shock is identified on annual data. Some differences are nevertheless noticeable. To some extent, the relative wage increases less in the short-run while total hours worked rise more when anticipation effects are controlled for. The differences are also moderate when our baseline results with a set of countries restricted to eight are contrasted with those for the VAR models augmented with the shock identified on quarterly data. Yet, the rise in government spending following a fiscal shock identified on quarterly data tends to be more pronounced and displays more persistence over time than in the baseline case. As a result, the response of sectoral shares are more pronounced than those in the baseline case. In the last robustness exercise, we provide an attempt to answer the following question numerically: to what extent the dynamic responses of economic variables are affected quantitatively by the differences in the government spending shocks. Reassuringly, we find that the differences are quantitatively small, if not insignificant, when we contrast theoretical IRF that we generate following the baseline government spending shock with theoretical IRF that we generate following a government spending shock that is allowed to vary across VAR specifications.

- The main obstacle in empirical fiscal policy analysis is to identify exogenous and unexpected fiscal events. In subsection D.5, we have addressed the potential effects of fiscal foresight. We now deal with the potential endogeneity problem. We tackle this issue in Appendix B.4 by identifying the spending shock on quarterly instead of annual data; empirical results show that the dynamic effects are rather similar whether the fiscal shock is identified on a quarterly or yearly basis. In order to investigate the extent of the potential endogeneity problem, in subsection D.7, we allow government expenditure series to react to all VAR variables contemporaneously and contrast the IRF for G in the baseline case in which G is ordered first with that when G is ordered last. Results show that differences are rather small and thus our results should not be affected by an endogeneity problem. We nevertheless conduct an empirical investigation by adopting an alternative identification scheme that would enable us to identify 'truly' exogenous government spending shocks. The solution suggested by the empirical literature to identify exogenous fiscal shocks is to adopt a narrative approach. In contrast to Blanchard and Perotti's [2002] identification scheme, the methodology is based on identifying changes in government spending directly from historical events or official documents. Ramey and Shapiro [1998] consider a small number of events which led to large military buildups. While such an analysis is not feasible for a large panel of countries, Guajardo, Leigh, and Pescatori [2014] use historical documents to construct a dataset that contains 173 fiscal policy changes for 17 OECD countries over the period 1978-2009. Following Ramey [2011], we augment each VAR model with the 'spending-based' events variable constructed by the authors, ordered first, and uses shocks to the 'spending-based' events variable (identified with the Cholesky decomposition) as the shock. Estimates show that whether changes in government spending are identified by using a narrative approach or by applying Blanchard and Perotti's [2002] assumption, the main conclusions reached in this paper hold, except for investment which is found to be significantly increasing instead of decreasing in the short-run. We may also note some interesting differences for the sectoral effects which suggest that the fiscal shock events identified by Guajardo, Leigh, and Pescatori [2014] are somewhat less biased toward non traded goods than those identified in this paper. More precisely, the responses of sectoral output shares are somewhat less pronounced in the 'event' study while the relative wage of non tradables increases less. We believe that more work needs to be done in order to understand the cause(s) of the quantitative differences between the two approaches.

D.1 Government Spending Shocks Biased Toward Non Traded Goods

Before discussing in details our calibration strategy, it is useful to explain how our panel VAR evidence can be related to the sector intensity in the aggregate government spending shock. In the main text, we run three alternative VAR specifications:

- The first VAR specification aims at exploring empirically the size the aggregate fiscal multiplier by using annual data. Like Corsetti et al. [2012], our panel VAR evidence indicates that the aggregate fiscal multiplier is smaller than 1. All else equal, if the fraction of the rise in government consumption spent on non tradables and tradables are equal, i.e., if $\omega_{G^N} = \omega_{G^T}$, then increases in value added expressed in percentage points of GDP are identical across sectors.

- In the second VAR specification, we explore empirically the size of the sectoral fiscal multiplier and estimate effects of an aggregate spending shock on non traded and traded value added at constant prices. Like Benetrix and Lane [2010], our panel VAR evidence shows that the rise in government spending increase non traded output relative to traded output. All else equal, a fall in Y^T/Y^N indicates that government spending shocks are biased toward the non traded sector. More precisely, as shown in section C.2, we have $\nu^{Y,N}\hat{Y}^N(t) - \nu^{Y,T}\hat{Y}^T(t) > 0$ as long as $\omega_{G^N} > \omega_{G^T}$ (see eq. (97)). This result reveals that the rise in government consumption is concentrated on non traded goods. However, it does not tell us anything about the reallocation of resources across sectors since it does not take into account that the share of non tradables is approximately two-third over 1990-2007. Thus, if $1/2 < \omega_{G^N} < 2/3$, non traded output increases more than traded output in percentage points of GDP but the share of non tradables in real GDP declines as the fraction of the rise in government spending spent on non tradables is smaller than the share of non tradables in GDP.

- The third VAR specification explores empirically the responses of the share of tradables and non tradables to a government spending shock. Such a response tells us how much sectoral output would increase if real GDP remained constant. Hence, for the sectoral output share in real GDP to increase, resources must be reallocated toward this sector. And the incentives to reallocate resources toward this sector depend on the extent of the rise in demand for non tradables. More precisely, as shown in section C.2, the share of non tradables in real GDP increases as long as the fraction of the rise in government spending spent on non tradables is higher than the share of non tradables in GDP. More precisely, keeping private sector's demand components fixed, we have $\nu^{Y,N}\left(\hat{Y}^N(0) - \hat{Y}_R(0)\right) = \left(\omega_{G^N} - \nu^{Y,N}\right)\frac{dG(t)}{Y}$. Since our panel VAR evidence indicates that the share of non tradables in real GDP, i.e., $\nu^{Y,N}\left(\hat{Y}^N(0) - \hat{Y}_R(0)\right)$, rises by 0.35 percentage points of GDP, using the fact that the non tradable content of GDP averages 60% over 70-07, the above formula gives us a non tradable content of the government spending shock $dG(0)/Y = 1\%$, i.e., $\omega_{G^N} = \nu^{Y,N}\left(\hat{Y}^N(0) - \hat{Y}_R(0)\right) + \nu^{Y,N} = 0.35\% + 0.6\% = 0.95\%$. This calculus does not take into account that the private sector's demand components respond endogenously to the government spending shock. Using eq. (107) and taking into account the reactions of consumption and investment (which merely influence the response of the share of non tradables) along with the decline in net exports, we have (in percentage points of GDP):

$$\omega_{G^N} = \underbrace{\nu^{Y,N}\left(\hat{Y}^N(0) - \hat{Y}_R(0)\right)}_{0.35\%} + \underbrace{\nu^{Y,N}}_{0.6\%} + \underbrace{\text{Changes in demand components}}_{-0.17\%} \simeq 0.78\%.$$

Thus, our VAR evidence suggest that the non tradable content of the government spending shock is substantial but smaller than 95% due to the current account deficit which further shifts demand toward non traded goods as traded goods can be imported.

Obviously, the discussion above is only informative and enables us to give a sense of the magnitude of the non tradable content of the aggregate spending shock. We detail below our calibration strategy.

Our calibration strategy amounts to calculating the allocation of the rise in government spending between non tradables and tradables. To accomplish this task, we first determine the non tradable content of government spending. Denoting by ω_{G^j} the content of government spending in good j, we have:

$$G(t) = \omega_{G^N} G(t) + \omega_{G^T} G(t). \tag{108}$$

To split government spending into expenditure in non traded and traded goods, i.e., to choose a value ω_{G^N}, we use time series from COFOG (Classification of the Functions of Government) provided by the OECD. This database 'classifies government expenditure data from the System of National Accounts by the purpose for which the funds are used' (more details can be found in the *Manual on sources and methods for the compilation of COFOG statistics*). COFOG has three levels of detail: Divisions, Groups, and Classes. 'The ten Divisions could be seen as the broad objectives of government, while the Groups and Classes detail the means by which these broad objectives are achieved'.

Data are available over the period 1995-2007 for AUT, BEL, DNK, ESP, FRA, GBR, IRL, ITA, NLD, NOR and SWE, 1998-2007 for AUS, 1990-2007 for FIN, 2005-2007 for JPN and 1970-2007 for USA. Data are not available for CAN. The advantage of this database is twofold. First, this dataset gives time series for government expenditure net of transfers and makes the distinction between final consumption expenditure and public investment. Thus, there is an exact correspondence between the sum of government consumption on tradables and non tradables on the one hand and time series for total government consumption expenditure used to estimate the effects of a government spending shock in the main text. Second, the first-level COFOG splits expenditure data into ten divisions. While there is some degree of arbitrariness in treating certain items as non tradables and the remaining as tradables, the content of items is such that there is little doubt in treating them as tradable or non tradable. Among the ten items, "04-Economic Affairs" is treated as tradable while the remaining nine items are classified as non traded: "01-General Public Services", "02-Defense", "03-Public Order and Safety", "05-Environment Protection", "06-Housing and Community Amenities", "07-Health", "08-Recreation, Culture and Religion", "09-Education", "10-Social Protection". It is worth mentioning that "Economic Affairs" is subdivided in six categories including "Fuel and Energy", "Agriculture, Forestry, Fishing, and Hunting", "Mining, Manufacturing, and Construction", "Transport and Communications". Among the nine items treated as non tradables, only one item, namely "Defense" may display some ambiguity. While in the main text, we treat this item as non tradables, we nevertheless conduct a robustness check in order to explore the extent to which our conclusion for the non tradable content of government spending shocks is altered when we classify "Defense" as a traded item.

Heading of each item are displayed in the first row of Table 14. Capital letters 'N' and 'T' indicate whether the item is classified as non tradables or tradables. The first column of Table 14 gives the time horizon over which data are available for each economy in our sample. The second column of Table 14 reports the total government consumption expenditure in percentage point of GDP by summing expenditure on non traded and traded goods.

In the main text, we calibrate the model over the period 1990-2007 as data are not available before 1990 and to be consistent with our empirical analysis in the main text. Column 4 of Table 5 in the Appendix intended for publication gives the non tradable content of government spending over 1990-2007 which averages 90%; thus, when we calibrate the model, we set ω_{G^N} (see eq. (108)) to 0.90. Since time series for government consumption by function are not available before 1995 for most of the countries in our sample, and because our objective in this subsection is to estimate the non tradable content of the aggregate government spending shock, in an effort to have time series of a reasonable length, we consider a period running from 1995 to 2015 except for Australia (1998-2015), Japan (2005-2015). As reported in column 4, the non tradable content of government spending averages 91% and displays a low cross-country dispersion as it varies from a low in Japan (87%) to a high in DNK, FRA, GBR and SWE (94%). Together, "Education" and "Health" account for almost half (48%) of government consumption, except for the US (34%). While there is low cross-country dispersion, it is worth mentioning that the U.S. has distinct features as the share of "Health" is 5.6% of total government consumption while "Defense" accounts for nearly one quarter of G.

We also investigate the causes of the cross-country dispersion in the non tradable content of government consumption expenditure. According to "Wagner's Law", richer countries choose bigger governments. In spirit of "Wagner's Law", we investigate whether richer countries also have a greater non tradable content of government expenditure, given its components includes health and education expenditure. We thus run the regression of ω_{G^N} on GDP per capita (GDP Per head, constant prices, constant PPPs, OECD base year) in panel data (with country fixed effects). As can be seen in the first row of Table 15, there is a positive relationship between these two variables. However, the coefficient in front of GDP per capita is not statistically significant. We believe that the non tradable content of government consumption expenditure is rather explained by the government spending-GDP ratio. Figure 21 plots the non tradable content of government consumption expenditure against the relative size of the public sector measured by the ratio of government consumption expenditure to GDP. The trend line shows that countries where the relative size of the public sector is higher have a greater non tradable content of government consumption expenditure. This results is corroborated since G/Y exerts a statistically significant positive impact on ω_{G^N}, as can be seen in the second row of Table 15. Because Rodrik [1998] finds a positive correlation between an economy's exposure to international trade and the size of its government, we believe that the non tradable content of government consumption expenditure is higher in countries which are more open to international trade. This finding would not be surprising since expenditure classified as non tradables includes spending for an allocative and redistributive motive.

In order to **investigate whether government consumption of non tradables is a major part of unanticipated changes in government spending**, we estimate a variance decomposition of government final consumption expenditure using a simple VAR including the log of real government consumption on non tradables, g^N_{it}, and the log of real government spending, g_{it}.[63] The sample covers 13 OECD countries over the period 1995-2015. We choose this period as time series for government consumption by function (COFOG dataset) provided by the OECD are not available before 1995 for most of the countries in our sample while the period 1995-2007 would be too short to obtain consistent estimates.[64] Table 16 reports the share of the forecast error variance of total government

[63] One or two lags and quantities are scaled by the working age population

[64] Data to construct time series for sectoral government consumption expenditure are available for all countries in our sample except Canada. In an effort to have a balanced panel and time series of a reasonable length, Australia (1998-2015) and Japan (2005-2015) are removed from the sample which leaves us with 13 OECD countries over the period 1995-2015.

Table 14: Breaking Down Time Series for Government Consumption into Tradables and Non Tradables (1995-2015)

	Period	G/Y	G^T/G	G^N/G	Public Services	Defense	Public Order	Economic Affairs	Environment Protection	Housing	Health	Recreation	Education	Social Protection
					N	N/T	N	T	N	N	N	N	N	N
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)
AUS	1998-2015	0.172	0.110	0.890	0.088	0.081	0.082	0.110	0.009	0.015	0.297	0.032	0.186	0.100
AUT	1995-2015	0.196	0.120	0.880	0.109	0.038	0.068	0.120	0.009	0.005	0.306	0.034	0.247	0.063
BEL	1995-2015	0.224	0.105	0.895	0.121	0.049	0.069	0.105	0.014	0.003	0.286	0.024	0.251	0.078
CAN	n.a.	n.a.	n.a	n.a.	n.a.	n.a.	n.a.	n.a.	n.a.	n.a.	n.a.	n.a.	n.a.	n.a.
DNK	1995-2015	0.251	0.062	0.938	0.084	0.059	0.033	0.062	0.014	0.006	0.274	0.045	0.188	0.236
ESP	1995-2015	0.181	0.087	0.913	0.098	0.057	0.099	0.087	0.022	0.026	0.291	0.047	0.208	0.065
FIN	1995-2015	0.221	0.098	0.902	0.108	0.060	0.050	0.098	0.007	0.008	0.250	0.032	0.207	0.180
FRA	1995-2015	0.230	0.064	0.936	0.114	0.070	0.062	0.064	0.022	0.021	0.283	0.031	0.198	0.134
GBR	1995-2015	0.188	0.057	0.943	0.051	0.114	0.098	0.057	0.024	0.023	0.315	0.033	0.178	0.107
IRL	1995-2015	0.165	0.094	0.906	0.037	0.029	0.087	0.094	0.030	0.030	0.336	0.025	0.225	0.107
ITA	1995-2015	0.189	0.076	0.924	0.129	0.067	0.098	0.076	0.014	0.024	0.324	0.017	0.206	0.045
JPN	2005-2015	0.193	0.131	0.869	0.097	0.043	0.061	0.131	0.032	0.019	0.346	0.014	0.143	0.113
NLD	1995-2015	0.233	0.095	0.905	0.068	0.060	0.067	0.095	0.033	0.018	0.245	0.036	0.182	0.196
NOR	1995-2015	0.207	0.074	0.926	0.103	0.081	0.040	0.074	0.007	0.005	0.293	0.033	0.207	0.157
SWE	1995-2015	0.253	0.063	0.937	0.089	0.062	0.048	0.063	0.003	0.006	0.240	0.034	0.238	0.218
USA	1995-2015	0.151	0.118	0.882	0.093	0.238	0.134	0.118	n.a.	0.005	0.056	0.014	0.303	0.040
Mean		0.204	0.090	0.910	0.093	0.074	0.073	0.090	0.017	0.014	0.276	0.030	0.211	0.123
USA	1970-2015	0.156	0.124	0.876	0.090	0.286	0.107	0.124	n.a.	0.006	0.056	0.012	0.284	0.035

Notes: Column 1 gives the period of coverage for each country. Column 2 shows the ratio of government final consumption expenditure to GDP. Column 3 and 4 report the tradable and non tradable content of government final consumption expenditure. Column 5 though 14 disaggregates by function and provides a detailed analysis of the share of each component in government expenditure. Capital letters 'N' and 'T' from column 5 to 14 indicates whether the component is classified as tradables or non tradables. Data coverage: 1995-2015 for AUT, BEL, DNK, ESP, FRA, GBR, IRL, ITA, NLD, NOR and SWE, 1998-2015 for AUS, 1990-2015 for FIN, 2005-2015 for JPN, 1970-2015 for USA. Data are not available for CAN.

Table 15: Potential Determinants of the Non Tradable Content of Government Consumption Expenditure

Explanatory Variables	(1)	(2)
y_{it}^{PPP}	0.011 (1.503)	
$(G/Y)_{it}$		0.016^{c} (1.839)
R^2	0.861	0.860
Time period	1995-2015	1995-2015
Countries	15	15
Observations	301	301
Country fixed effects	yes	yes

Notes: in all regressions the dependent variable is G^N/G. All variables enter in regression in logarithms. ^{a}, ^{b} and ^{c} denote significance at 1%, 5% and 10% levels. Heteroskedasticity and autocorrelation consistent t-statistics are reported in parentheses.

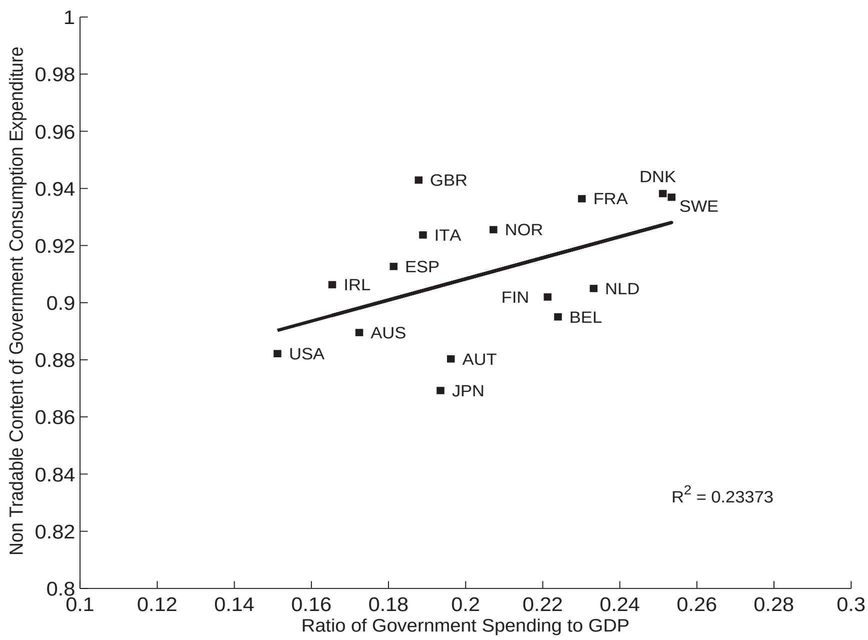


Figure 21: Non Tradable Content of Government Consumption Expenditure against the Relative Size of the Public Sector. Sample: 16 OECD countries 1995-2015; Source: OECD-COFOG database for G^N and OECD Economic Outlook for G/Y

Table 16: Variance Decomposition for Government Final Consumption Expenditure on Annual Data (1995-2015)

	Defense classified in G^N		Defense classified in G^T	
Step	$p=1$	$p=2$	$p=1$	$p=2$
1	0.902	0.874	0.801	0.825
2	0.903	0.831	0.788	0.864
3	0.905	0.831	0.809	0.892
4	0.906	0.844	0.835	0.911
5	0.907	0.858	0.855	0.924
6	0.907	0.867	0.864	0.933
7	0.908	0.872	0.868	0.940
8	0.908	0.874	0.869	0.945

Notes: To estimate a variance decomposition for total government consumption expenditure $g_{i,t}$, we use a simple VAR model that includes government consumption of non tradables and government final consumption expenditure, i.e., $z_{i,t} = [g^N_{i,t}, g_{i,t}]$. We allow for either $p = 1$ or $p = 2$ lags. Data coverage: 1995-2015 for AUT, BEL, DNK, ESP, FIN FRA, GBR, IRL, ITA, NLD, NOR, SWE and the USA (source: OECD-COFOG database).

spending attributable to shocks to g^N at various horizons. Government spending shocks on non tradables accounts for almost all of the unforeseen changes in total government spending. More precisely, irrespective of whether the item 'Defense' is classified as tradables or as non tradables, shocks to g^N account for 79%-95% of the variance of total government spending for horizons of one to eight years. It is worth mentioning that for each of the four specifications, the contribution of shocks to g^N is rather stable over time, in particular when 'Defense' is classified as non tradables. In this case, the contribution of shocks to g^N to unanticipated changes in G averages 91% with one lag and 86% with two lags.

Theoretical impulse response functions of sectoral government consumption. In order to reproduce the hump-shaped pattern of the endogenous response of government spending to an exogenous fiscal shock, we assume that the deviation of government spending relative to its initial value as a percentage of initial GDP is governed by the dynamic equation (23). Left-multiplying (23) by ω_{G^j} (with $j = N, T$) gives the dynamic adjustment of sectoral government consumption to an exogenous fiscal shock:

$$\omega_{G^j} \frac{G(t) - \tilde{G}}{Y} = \omega_{G^j} \left[e^{-\xi t} - (1 - g)\, e^{-\chi t} \right]. \tag{109}$$

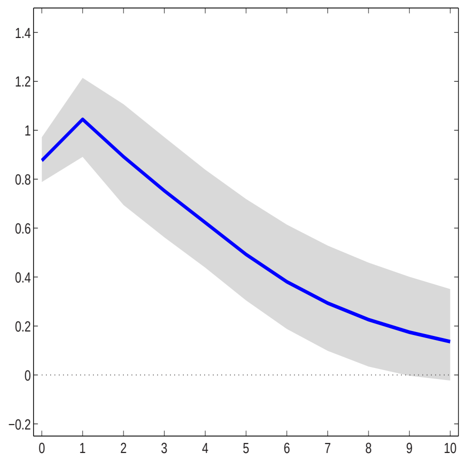
We set g to 0.01 as we consider an exogenous increase in government spending by 1% of GDP and choose values of ξ and χ in order to reproduce the hump-shaped pattern of the endogenous response of government spending to the exogenous fiscal shock. To the extent that ω_{G^j} is considered as fixed over time, we set ω_{G^j} to the share of government final consumption expenditure in good j. Thus, we set ω_{G^N} to 90% and $\omega_{G^T} = 10\%$ which corresponds to the non tradable and the tradable content of government final consumption expenditure, respectively. The derivation of the dynamic equation (43) that governs the adjustment of sectoral government consumption following an exogenous fiscal shock relies on a number of assumptions. We assume that parameters that govern the persistence and the shape of the response of sectoral government consumption are identical across sectors while sectoral intensity of the government spending shock is constant over time and thus corresponds to the share of government final consumption expenditure in good j. We investigate below the extent to which these assumptions are consistent with empirical impulse response functions we generate following a rise in government consumption by 1% of GDP.

Empirical vs. theoretical impulse response functions of sectoral government consumption. To generate impulse response functions of sectoral government consumption, we first estimate the first VAR model that includes government final consumption expenditure, real GDP, total hours worked, private investment, the real consumption wage, in order to identify unanticipated government spending shocks. Then, we estimate a VAR model in panel format on annual data that includes unanticipated government spending shocks, ϵ_{it}^G, ordered first, government spending, g_{it}, government consumption on non tradables, g_{it}^N, and government consumption on tradables, g_{it}^T, i.e., $z_{i,t}^G = [\epsilon_{it}^G, g_{it}, g_{it}^N, g_{it}^T]$. All quantities are logged, expressed in real terms and scaled by the working age population. As mentioned above, data to construct time series for sectoral government consumption expenditure are available for all countries in our sample except Canada. In an effort to have a balanced panel and time series of a reasonable length, Australia (1998-2015) and Japan (2005-2015) are removed from the sample which leaves us with 13 OECD countries over the period 1995-2015. To be consistent, we estimate the first VAR model that includes aggregate variables for these 13 OECD countries only. Table 17 reports, for various horizons, the mean responses of government consumption expenditure on non tradables and tradables to the identified government spending shock. We normalize the impulse responses so that government spending rises by one percentage point of GDP on impact. The table show that no matter what the order of the variables, a government spending shock leads to an increase in government consumption expenditure on non tradables by 0.88% on impact while the rise in public purchases of tradables accounts for the remaining share, i.e., 12%. The average contribution of the response of g^N to the government spending shock is displayed in the last line of Table 17. The contribution of government expenditure on non tradables averages 90%. We also find that its contribution is quite stable over time as it varies between 88% and 91%.

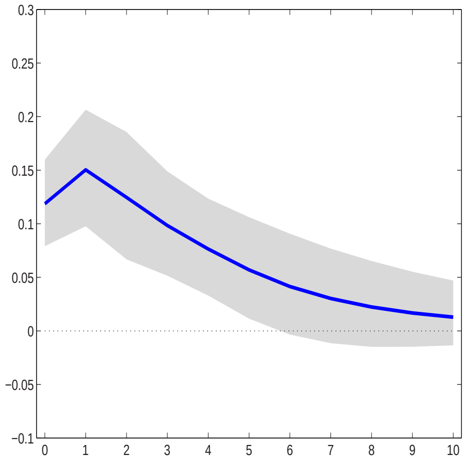
Empirical impulse response functions for the two components of government final consumption expenditure we generate following a rise in government spending by 1% of GDP are displayed in solid blue lines in Figure 22. The first and the second row show results for $z_{i,t}^G = [\epsilon_{i,t}^G, g_{it}, g_{i,t}^N, g_{i,t}^T]$ and $z_{i,t}^G = [\epsilon_{i,t}^G, g_{it}, g_{i,t}^T, g_{i,t}^N]$, respectively. No matter the ordering of variables, impulse response functions for both sectoral components of government spending display an hump-shaped pattern, like the endogenous response of total government spending, and peak after 1 year.

Empirical and theoretical impulse response functions are contrasted and displayed by solid blue lines in the right panel of Figure 23. Before discussing the results, we first focus on the response of government final consumption expenditure to the exogenous fiscal shock shown in the left panel of Figure 23. The endogenous response of government spending to an exogenous fiscal shock displayed in the solid blue line corresponds to the baseline government spending shock in the main text (see Figure 1(a)) obtained from estimates of the first VAR model. The dynamic response of government final consumption expenditure which has been computed by summing mean responses of government consumption consumption on non tradables and tradables is displayed by the solid red line. While the solid blue line displays the point estimates from a sample of 15 OECD countries over 1970-2007, the solid red line displays the point estimates from a sample of 13 OECD countries over 1995-2015. Whereas the samples are different, the discrepancy is quite moderate. Since theoretical responses of sectoral government consumption are based on the response of government spending shown in the solid blue line in the left panel while the sum of mean responses of government consumption expenditure on non tradables and tradables gives a slightly different response of government spending as show in the solid red line, we have to rescale empirical responses for G^j so that the sum of mean responses corresponds exactly to the point estimate displayed in the solid blue line. The rescaled empirical responses of sectoral government consumption are displayed by solid blue lines in the right panel of Figure 23 with dotted blue lines indicating the 90 percent confidence bounds obtained by bootstrap sampling. We contrast empirical with theoretical responses displayed by dotted black lines. It turns out that differences are quite moderate. We may notice that while the theoretical response of government consumption on non tradables (tradables) slightly overstates (understates) the estimated response, it lies within the confidence bounds for both goods. To conclude, the assumptions underlying the dynamic equation (109) which governs theoretical responses of G^j are reasonable and consistent with data.

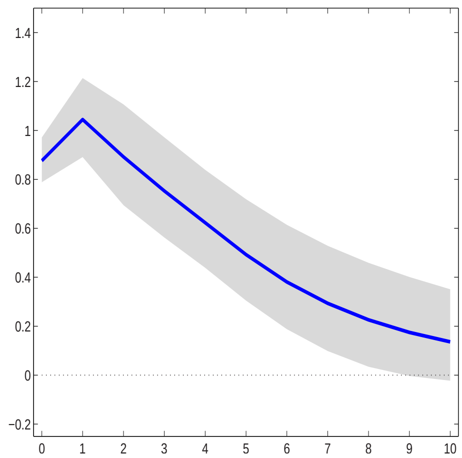
Variance decomposition for government spending: U.S. (1970-2007). So far, we have quantified the contribution of shocks to G^N to unforeseen changes in government spending. We now move a step further and investigate whether identified shocks to G^N produce similar effects to those triggered by shocks to G. Such an analysis is feasible



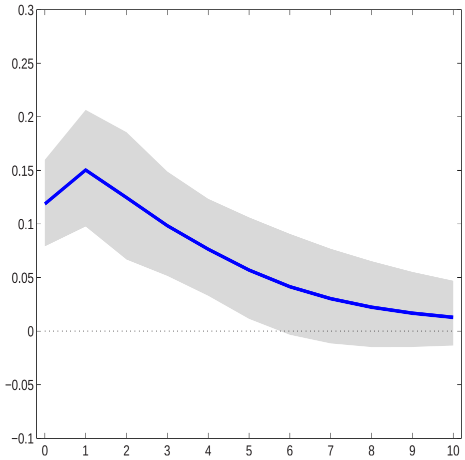
(a) Gov. Exp. on Non Tradables, G^N



(b) Gov. Exp. on Tradables, G^T



(c) Gov. Exp. on Non Tradables, G^N



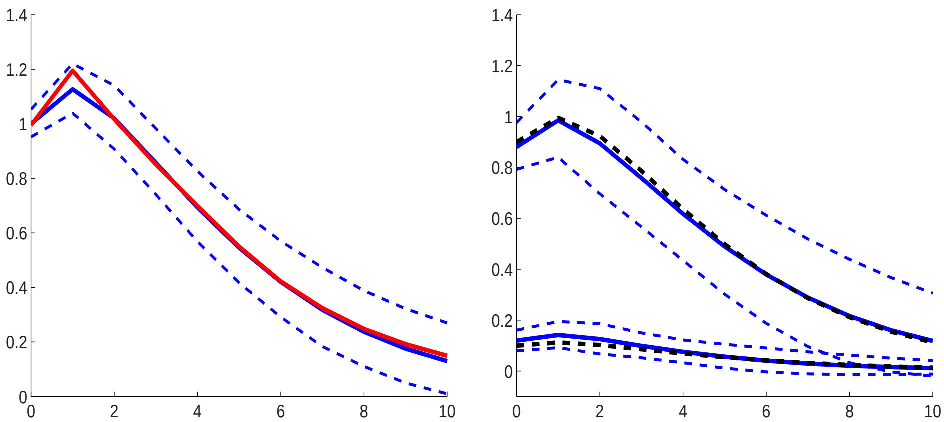
(d) Gov. Exp. on Tradables, G^T

Figure 22: Effects of an Unanticipated Government Spending Shock on Government Final Consumption Expenditure on Non Tradables and Tradables. Notes: Exogenous increase in government consumption by 1% of GDP. The government spending shock is identified by estimating a VAR model that includes real government final consumption expenditure, GDP (constant prices), total hours worked, private fixed investment, and the real consumption wage. The responses of government final consumption expenditure on non tradables (i.e., G^N) and tradables (i.e., G^T) to the identified government spending shock are displayed by solid blue lines with the shaded area indicating the 90 percent confidence bounds obtained by bootstrap sampling; sample: 13 OECD countries, 1995-2015, annual data.

Table 17: Responses of G^N and G^T to Identified Government Spending Shock: Point Estimates

Horizon	$z_{i,t}^G = [\epsilon_{i,t}^G, g_{i,t}, g_{i,t}^N, g_{i,t}^T]$		$z_{i,t}^G = [\epsilon_{i,t}^G, g_{i,t}, g_{i,t}^T, g_{i,t}^N]$	
	G^N	G^T	G^N	G^T
0	0.876	0.119	0.877	0.118
1	1.045	0.150	1.045	0.150
2	0.892	0.125	0.893	0.124
3	0.753	0.098	0.753	0.098
4	0.623	0.076	0.623	0.076
5	0.493	0.057	0.493	0.057
6	0.381	0.041	0.382	0.042
7	0.294	0.030	0.294	0.030
8	0.226	0.022	0.227	0.022
9	0.175	0.017	0.176	0.017
10	0.136	0.013	0.138	0.013
Contribution	0.895	0.104	0.895	0.104

Notes: Horizon measured in year units. We generate impulse response functions by using a simple VAR, i.e., $z_{i,t}^G = [\epsilon_{i,t}^G, g_{i,t}, g_{i,t}^N, g_{i,t}^T]$ or $z_{i,t}^G = [\epsilon_{i,t}^G, g_{i,t}, g_{i,t}^T, g_{i,t}^N]$ with 2 lags. To identify the government spending shock $\epsilon_{i,t}^G$ we estimate the VAR model that includes aggregate variables, i.e., $z_{i,t} = [g_{i,t}, y_{i,t}, l_{i,t}, je_{i,t}, w_{C,i,t}]$, and adopt a Cholesky decomposition. The last line of the table displays the average contribution of the response of each component to the government spending shock. Data coverage: 1995-2015 for AUT, BEL, DNK, ESP, FIN, FRA, GBR, IRL, ITA, NLD, NOR, SWE and the USA. All variables are real and scaled by the working age population.



(a) Government Final Consumption Expenditure, G

(b) Government Expenditure on Non Tradables, G^N, and Tradables, G^T

Figure 23: Effects of an Unanticipated Government Spending Shock on Government Final Consumption Expenditure on Non Tradables and Tradables: Empirical vs. Theoretical Impulse Response Functions. Notes: The baseline response of government final consumption expenditure is displayed by the solid blue line with the shaded area indicating the 90 percent confidence bounds obtained by bootstrap sampling; sample: 16 OECD countries, 1970-2007, annual data. The responses of government final consumption expenditure on non tradables (i.e., G^N) and tradables (i.e., G^T) to the identified government spending shock (in the baseline VAR model) are displayed by solid blue lines with dotted blue lines indicating 90 percent confidence bounds obtained by bootstrap sampling; sample: 13 OECD countries, 1995-2015, annual data. The red line in the left panel displays the dynamic response of government final consumption expenditure which has been computed by summing mean responses of government consumption expenditure on non tradables and tradables.

Table 18: Variance Decomposition for Government Final Consumption Expenditure on U.S. annual data (1970-2007)

	$z_t = [g_t^N, g_t]$		$z_t = [g_t^N, g_t, y_t]$	
Step	$p = 1$	$p = 2$	$p = 1$	$p = 2$
1	0.940	0.878	0.941	0.903
2	0.916	0.961	0.909	0.955
3	0.897	0.959	0.887	0.927
4	0.882	0.952	0.871	0.910
5	0.872	0.950	0.861	0.911
6	0.865	0.951	0.855	0.917
7	0.859	0.951	0.852	0.920
8	0.856	0.952	0.850	0.917

Notes: Decomposition of variance for government spending g_t from estimates of alternative VAR specifications $z_{i,t} = [g_t^N, g_t]$ and $z_t = [g_t^N, g_t, y_t]$, respectively, with either $p = 1$ or $p = 2$ lags. Data coverage: 1970-2007.

for the US as time series for G^N are available from 1970 to 2007. Before discussing the dynamic effects, we first estimate a variance decomposition of government spending by using a simple VAR $z_t = [g_t^N, g_t]$. We alternatively augment the VAR model with real GDP and thus consider the following specification $z_t = [g_t^N, g_t, y_t]$. The results reported in Table 18 reveal that, regardless of the VAR specification or the number of lags, shocks to G^N account for 86 to 96 percent of the forecast error variance of total government spending for horizons of 1 to 8 years.

We then estimate the baseline VAR models described in section 2 by using U.S. annual data over 1970-2007. To contrast the effects of a rise in G^N with those following an increase in G, we re-estimate VAR models in which g_t is replaced with g_t^N. The latter variable is constructed in accordance with the classification discussed above.[65] Figure 24 shows that the share of non tradables in total government consumption is rather stable after 1988 and averages 88%. We generated impulse response functions which are normalized so that government consumption increases by 1 percentage point of GDP. The solid blue line in Figures 25 and 26 shows the results following a rise in total government consumption while the solid black line shows the results following a rise in government consumption of non tradables.[66] The results are quite clear:

- First, as displayed in the first row of Figures 25-26, both the shape and the magnitude of the endogenous responses of government consumption are quite similar.
- Second, all the conclusions reached in the main text hold whether we consider a rise in G or in G^N. More precisely, we find empirically that a government spending shock gives rise to a contraction in hours worked and output in the traded sector while it has an expansionary effect on non traded output. Moreover, a rise in public purchases lowers the share of tradables and increases the relative size of the non traded sector. Finally, both the relative price and the relative wage of non tradables increase.
- Third, and most importantly, the sectoral effects are of the same magnitude whether we consider a rise in total government spending or an increase in government consumption of non traded goods. The evidence also shows that the shape of impulse response functions is quite similar. Across all VAR specifications, differences between the dynamics effects of both shocks are rather moderate. More specifically, the impulse response functions we generated after a shock to g_t^N lie within the confidence bounds of the IRF we generated after a shock to g_t.

[65] g_t is real government final consumption expenditure (source: OECD Economic Outlook Database) while g_t^N is real government final consumption expenditure on non tradables (source: OECD COFOG). Government spending on non tradables is deflated by the price of final consumption expenditure of general government (source: OECD Economic Outlook Database).

[66] Given the small number of observations ($T = 38$), VAR models are estimated by restricting the number of lags p to one in order to economize some degrees of freedom.

Figure 24: Non Tradable Content of Government Spending in the USA (source: COFOG database, OECD)

To conclude, our evidence reveal that the shocks to G^N account on average for about 88% of shocks to G for the whole sample over 1995-2015 while the variance decomposition on U.S. annual data over 1970-2007 suggests that shocks to government consumption of non traded goods accounts on average for 92% of the unforeseen changes in total government spending. Using a panel of 13 OECD countries over 1995-2015, When we estimate mean responses of government consumption expenditure on non tradables and tradables to our identified government spending shock, we find that the former contributes on average to 90% of the change in government spending while the remaining is attributed to government purchases of tradables. When we calibrate the model, we thus consider a rise in government spending which is split between non tradables and tradables in accordance with their respective contribution to the government spending shock, at 90% and 10% respectively.

D.2 An Elaborate Investigation of Responses of Government Expenditure Components to a Government Spending Shock

In this subsection, we conduct an elaborate investigation of the effects on sub-components of government final consumption expenditure and government consumption expenditure on non tradables. First, there are two main components in government consumption expenditure: the purchase of goods and services from the private sector, and the purchases of goods and services from the government sector, the latter corresponding to compensation of government employees. Second, because government consumption expenditure classified as non tradables includes nine divisions which differ from each other along a number of dimensions, such as the purpose (public versus private goods) and the type of expenditure (defense versus non-defense expenditure), in the following, we explore empirically the contribution of each broad category to shocks to government consumption of non traded goods.[67]

Wage vs. non-wage government consumption expenditure. Before going into more details in our empirical investigation, as will be useful below, we introduce a number of definitions. Since in our analysis we abstract from government investment, we denote by G government aggregate consumption expenditure. Government consumption expenditure can be subdivided into *compensation of employees* (Y_{publ}) and *non-wage government con-*

[67]Because the time horizon is too short and the number of observations are not large enough to estimate a VAR model that would enable to compute the contribution of each division of expenditure to increases in aggregate government consumption or government consumption on non traded goods for each country, we estimate a VAR model in panel format and subdivide G^N into broad categories as detailed below.

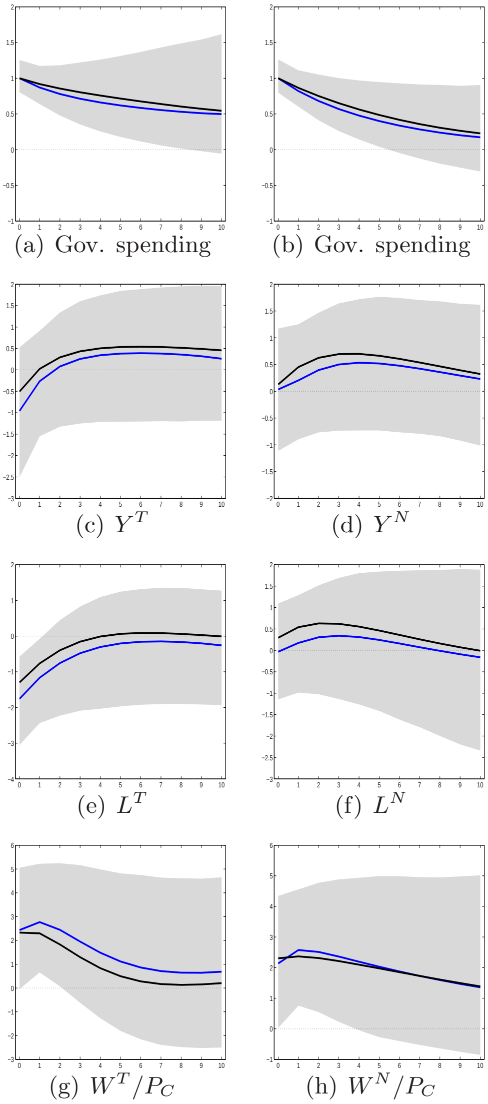


Figure 25: Sectoral Effects of Shocks to Aggregate Government Consumption and Government Consumption of Non Tradables. Notes: Exogenous increase in government consumption by 1% of GDP. Horizontal axes indicate years. Vertical axes measure percentage deviation from trend. Results for a shock to government final consumption expenditure are displayed by solid lines with the shaded area indicating the 90 percent confidence bounds obtained by bootstrap sampling; the black line displays the responses following a shock to government consumption of non tradables; sample: U.S., 1970-2007, annual data.

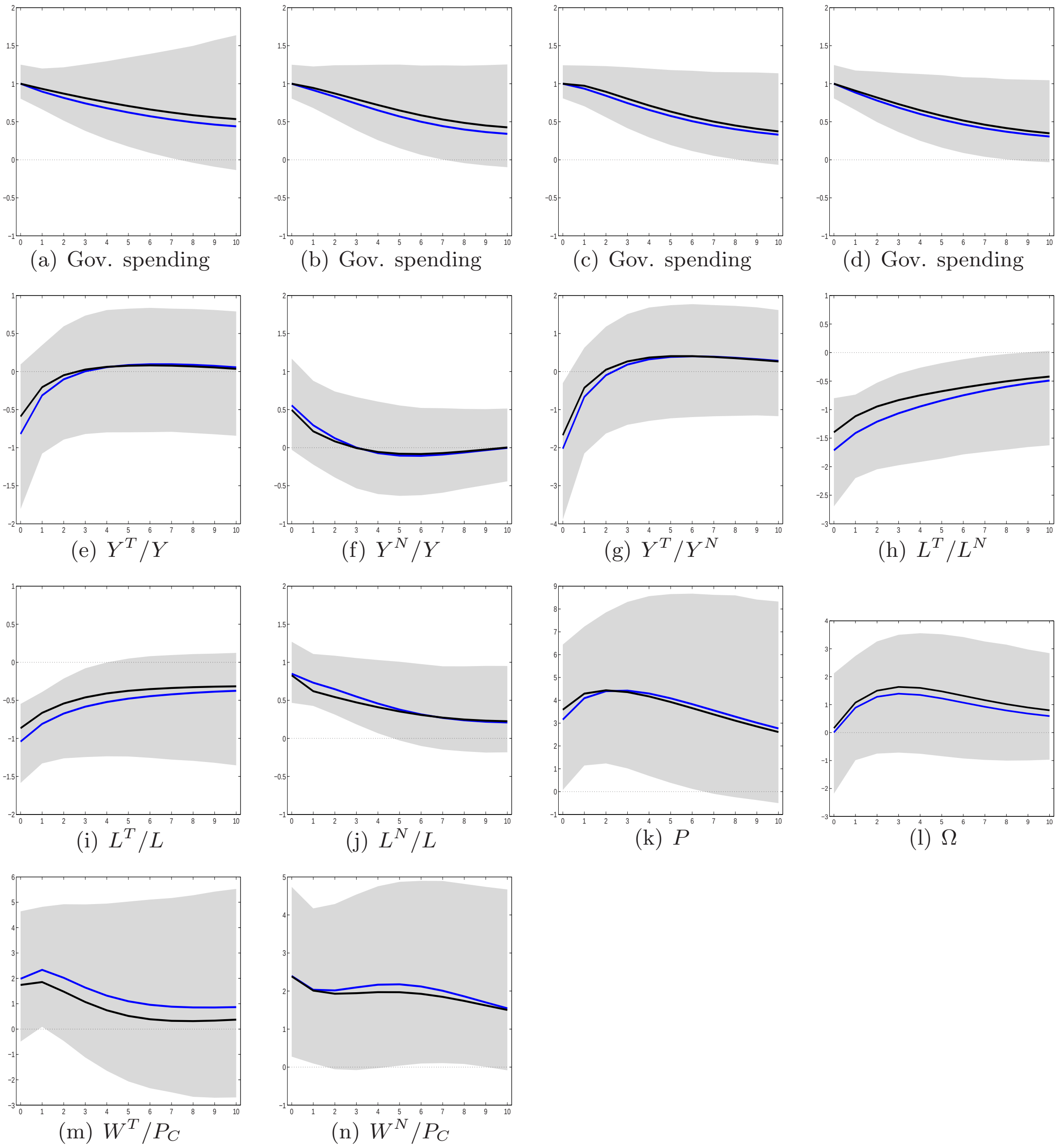


Figure 26: Sectoral Composition Effects of Shocks to Aggregate Government Consumption and Government Consumption of Non Tradables. Notes: Exogenous increase in government consumption by 1% of GDP. Horizontal axes indicate years. Vertical axes measure percentage deviation from trend. Results for a shock to government final consumption expenditure are displayed by solid lines with the shaded area indicating the 90 percent confidence bounds obtained by bootstrap sampling; the black line displays the responses following a shock to government consumption of non tradables; sample: U.S., 1970-2007, annual data.

sumption (G_{priv}). The former component covers total remuneration paid by government to its employees and relates to the services provided by the government (value added of government), whereas the latter covers public purchases of consumption goods and services from the private sector. While we could restrict our attention to G^N and differentiate between compensation of employees and non-wage government consumption within this component of G, data availability (since data start from 1995 for most of the countries) would prevent from conducting a VAR analysis.

Framework. Government purchases G consists of the value added of government, Y_G^N, which is part of the non traded sector, and government purchases of goods and services from the private sector ($G_P = G^T + PG_P^N$). Denoting the value added of the private sector by Y_P^N and the government value added by Y_G^N, the market clearing condition for non traded goods reads as:

$$Y^N = Y_P^N + Y_G^N = C^N + J^N + G^N, \tag{110}$$

where G^N consists of i) the value added which the government itself produces and sells to itself, i.e., $G_G^N = Y_G^N$, and ii) government purchases of non tradable goods and services from the private sector, G_P^N. In our study, the private and the public sector are aggregated and thus we explore the effects on non traded value added, Y^N. Conversely, if we restrict attention to the effects on value added of the private sector, using the fact that $Y_G^N = G_G^N$, eq. (110) can be rewritten as follows:

$$Y_P^N = C^N + J^N + G_P^N, \tag{111}$$

Since $L^N = L_P^N + L_G^N$ where L_P^N and L_G^N corresponds to hours worked used in the private and the public sector, in our study, we implicitly assume that hours worked can be moved costlessly between the private and the public sector. While it may be viewed as restrictive, most of the literature sets this assumption, see e.g., Cavallo [2005]. The government hires labor, L_G^N, and rents capital, K_G^N, from households, to produce government value added according to the following production function:

$$Y_G^N = \left(L_G^N\right)^{\theta^N} \left(K_G^N\right)^{1-\theta^N}. \tag{112}$$

Due to the assumption of perfect mobility of labor between the private non traded sector and the government (non traded) sector, compensation of government employees is $W^N L_G^N$. To finance compensation of government employees and rental services from capital, RK_G^N, along with purchases of goods and services from the private sector, the government levies lump-sum taxes in accordance with the following budget constraint:

$$\begin{aligned} T &= W^N L_G^N + RK_G^N + PG_P^N + G^T, \\ &= PY_G^N + PG_P^N + G^T, \\ &= PG^N + G^T = PY_G^N + G_P, \end{aligned} \tag{113}$$

where G^T is government purchases of goods and services from the traded (private) sector. The exposition of a framework that makes the distinction between the government and the private (non traded) sector has the merit to shed some light on the assumptions we set to aggregate these two sectors. First, we assume perfect mobility of labor between the government and the private (non traded) sector. Second, the traded sector is assumed to consist exclusively of private-sector firms. In other words, we assume that the government purchases goods and services from the private traded sector but does not hire traded labor.

Average government spending share of compensation of government employees. The second column of Table 19 reports the share of the compensation of employees in total government consumption expenditure for each country and for the whole sample as well. The first column indicates the time period over which data are available to re-estimate the VAR model in panel format on annual data. The time series for compensation of government employees are not available for AUS while data are available from 1970 to 2007 for all remaining countries, except BEL (1976-2007). As can be seen in the second column of Table 19, from 1970 to 2007, the average government spending share of purchases from the private sector is about 40% and the average share of the other component (i.e.,

Table 19: Subcomponents of Total Government Consumption Expenditure and Government Consumption Expenditure on Non Traded Goods

Country	Total Gov. Cons. Expend.		Gov. Cons. Expend. on N			
	(1) Period	(2) G_{publ}/G	(3) Period	(4) G^N_{publ}/G^N	(5) G^N_{coll}/G^N	(6) G^N_{def}/G^N
AUS	n.a.	n.a.	1998-2015	0.570	0.309	0.091
AUT	1970-2007	0.594	1995-2015	0.579	0.261	0.044
BEL	1976-2007	0.588	1995-2015	0.535	0.286	0.055
CAN	1970-2007	0.640	n.a.	n.a.	n.a.	n.a.
DNK	1970-2007	0.674	1995-2015	0.656	0.208	0.063
ESP	1970-2007	0.633	1995-2015	0.595	0.331	0.063
FIN	1970-2007	0.671	1990-2015	0.648	0.258	0.066
FRA	1970-2007	0.579	1995-2015	0.566	0.310	0.075
GBR	1970-2007	0.575	1995-2015	0.534	0.330	0.121
IRL	1970-2007	0.544	1995-2015	0.602	0.235	0.032
ITA	1970-2007	0.604	1995-2015	0.575	0.359	0.072
JPN	1970-2007	0.437	2005-2015	0.323	0.291	0.050
NLD	1970-2007	0.502	1995-2015	0.398	0.272	0.067
NOR	1970-2007	0.641	1995-2015	0.655	0.255	0.088
SWE	1970-2007	0.641	1995-2015	0.516	0.221	0.066
USA	1970-2007	0.637	1995-2015	0.672	0.532	0.270
Whole	1970-2007	0.597	1995-2015	0.562	0.297	0.081

Notes: G_{publ} is government final wage consumption expenditure (source: OECD Economic Outlook Database); G^N_{publ} is government final wage consumption expenditure on non tradables, G^N_{coll} collective government final consumption expenditure on non tradables, G^N_{def} government final consumption expenditure related to 'Defense' (source: OECD, COFOG database).

G_{publ}/G) is 60%. Hence, the purchases of goods and services from the government sector are a significant component in government spending. As displayed in column 4 of Table 19, the average government consumption expenditure on non tradables share of purchases from the public sector, i.e., G^N_{publ}/G^N, is a little bit lower at 56%. While the Table does not show it, the average government consumption expenditure on tradables share of purchases from the public sector, i.e., G^T_{publ}/G^T, is lower than that for non tradables, at 41%. Since G^j_{publ}/G^j is calculated over 1995-2015 and is lower than that over 1970-2007, the average government spending share of purchases from the private sector has increased significantly over time.

Wage and non-wage government consumption shocks. We re-estimate the VAR models specified in section 2 in the main text in panel format on annual data by separating the goods and services provided by the government sector (i.e., G_{publ}) from the purchase of goods and services from the private sector (i.e., G_{priv}):

- G_{publ}: **Government final wage consumption expenditure**. Source: OECD Economic Outlook Database. To express the variable in real terms, we deflate time series by the deflator of government final consumption expenditure (source: OECD Economic Outlook Database).

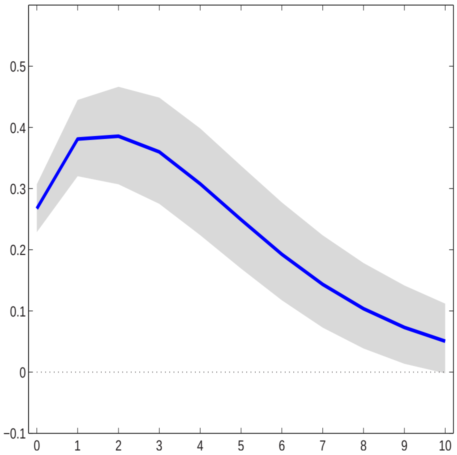
- $G_{priv} = G - G_{publ}$: **Public purchase of goods and services from the private sector**. To construct time series for variable G_{priv}, we subtract government final wage consumption expenditure from government final consumption expenditure (source: OECD, current prices, in millions of national currency). To express the variable in real terms, we deflate time series by the deflator of government final consumption expenditure (source: OECD Economic Outlook Database).

Because data are not available for AUS, the dataset covers 15 OECD countries over the period running from 1970 to 2007, except for BEL (1976-2007). In order to make our results for a wage government consumption shock comparable with those obtained for a government consumption shock, we re-estimate the VAR models for the restricted set of countries (i.e., 15). The baseline VAR model includes $G = G_{publ} + G_{priv}$ ordered first; when exploring a shock to wage or non-wage government consumption, G is replaced with G^{publ} or G^{priv} (ordered first), respectively.

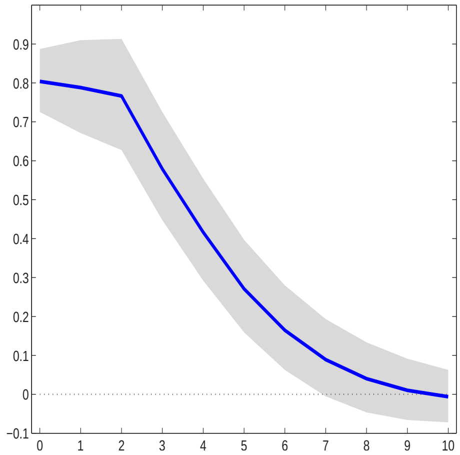
How do compensation of government employees, G_{publ}, and the purchases of goods and services from the private sector, G_{priv}, react to our identified government shock? We begin by analyzing how government purchases from the public and private sectors react to a government spending shock. We first estimate the first VAR model that includes government final consumption expenditure, real GDP, total hours worked, private investment, and the real consumption wage, in order to identify unanticipated government spending shocks. Then, we estimate a VAR model in panel format on annual data that includes unanticipated government spending shocks, ϵ^G, ordered first, government spending, g_{it}, labor compensation of government employees, G_{publ}, and government purchases of goods and services from the private sector, G_{priv}, i.e., $z^G_{i,t} = [\epsilon^G_{i,t}, g_{it}, g_{publ,i,t}, g_{priv,i,t}]$. To be consistent, we estimate the first VAR model that includes aggregate variables for 15 OECD countries only since time series for the two components are not available for AUS. Table 20 shows, at various horizons for different orderings of the variables, the mean responses of government consumption expenditure from the public and the private sector to the identified government spending shock. We normalize the impulse responses so that government spending rises by one percentage point of GDP on impact. The contribution of the response of labor compensation of government employees to the government spending shock is displayed in the third and the six column of Table 20. The table shows that, no matter what the ordering of the variables, the contribution of government purchases of goods and services from the private sector is large on impact and low after five years while we get the opposite result for compensation of government employees. In other words, a government spending shock seems to be associated first with higher purchases from the private sector and then with an increase in labor compensation. The average contribution of government purchases from the public sector shown in the last line of Table 20 is 55-63%. The contribution increases strongly over time, varying between 25% on impact and 100% after 10 years.

Impulse response functions for the two components of government final consumption expenditure that we generate following a rise in government spending by 1% of GDP are displayed in solid blue lines in Figure 27. The first and the second row show results for $z^G_{i,t} = [\epsilon^G_{i,t}, g_{it}, g_{publ,i,t}, g_{priv,i,t}]$ and $z^G_{i,t} = [\epsilon^G_{i,t}, g_{it}, g_{priv,i,t}, g_{publ,i,t}]$, respectively. No matter what the ordering of the variables, impulse response functions for the components of government spending are quite distinct. In particular, the endogenous response of government purchases from the private sector is much less persistent while the response of labor compensation is hump-shaped and persistent over time.

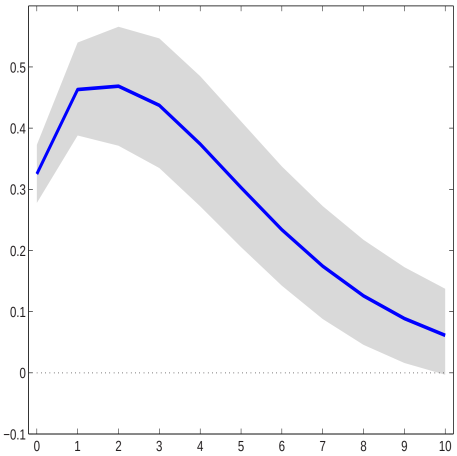
The results for a **wage government consumption shock** (solid black lines) are shown and contrasted with those for the baseline (solid blue lines) VAR model that includes total government consumption expenditure in Figures 28 and 29. To facilitate the interpretation of our results, we normalize the impulse responses so that government final (wage) consumption expenditure increases by one percentage point of GDP on impact. When we investigate the effects of a rise in government final wage consumption expenditure, we analyze the impacts on the whole economy (i.e., the private plus the public sector). The reason is that by construction, we have $Y_{publ} = G_{publ}$ where Y_{publ} is government value added and total GDP is the sum of value added of the public and the private sector, i.e., $Y = Y_{priv} + Y_{publ}$. Overall, it turns out that the effects of a wage government consumption shock are more pronounced. All our conclusions in the main text hold though. As can be seen in Figure 28, a wage government consumption shock has a strong expansionary effect on output and hours worked and leads to a greater current account deficit. Importantly, Figure 29 shows that the share of tradables declines and the relative size of the non traded sector increases, while both the relative price and the relative wage of non tradables appreciate. Nevertheless, we may notice a discrepancy in the estimated responses of sectoral real consumption wages, sectoral shares and the relative price, which are more pronounced in both the traded and the non traded sector following a wage government consumption shock. Bermperoglou, Pappa, and Vella [2016] document evidence showing that public employment and public wage (at the state and local level) shocks have expansionary ef-



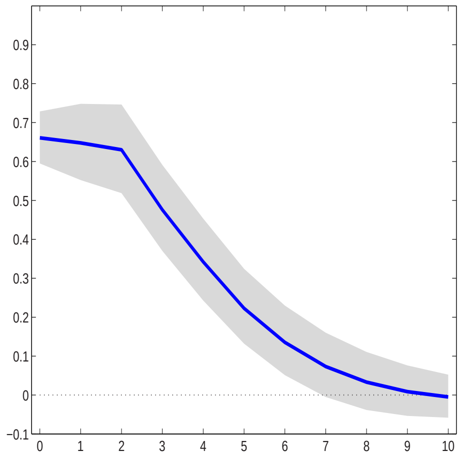
(a) Gov. Exp. in the Government Sector, G_{publ}



(b) Gov. Exp. in the Private Sector, G_{priv}



(c) Gov. Exp. in the Government Sector, G_{publ}



(d) Gov. Exp. in the Private Sector, G_{priv}

Figure 27: Effects of an Unanticipated Government Spending Shock on Purchase of Goods and Services from the Government and the Private Sector. Notes: Exogenous increase in government consumption by 1% of GDP. The government spending shock is identified by estimating a VAR model that includes real government final consumption expenditure, GDP (constant prices), total hours worked, private fixed investment, and the real consumption wage. We differentiate between government final consumption expenditure from the public sector and the private sector. The responses of the components of government final consumption expenditure to the identified government spending shock are displayed by solid blue lines with the shaded area indicating the 90 percent confidence bounds obtained by bootstrap sampling; sample: 15 OECD countries, 1970-2007 (except for BEL: 1976-2007), annual data.

Table 20: Responses of Components of Government Consumption Expenditure to Identified Government Spending Shock: Point Estimates

Horizon	$z^G_{i,t} = [\epsilon^G_{i,t}, g_{it}, g_{publ,i,t}, g_{priv,i,t}]$		Contribution	$z^G_{i,t} = [\epsilon^G_{i,t}, g_{it}, g_{priv,i,t}, g_{publ,i,t}]$		Contribution
	G_{publ}	G_{priv}	of G_{publ} in %	G_{priv}	G_{publ}	of G_{publ} in %
0	0.267	0.804	25%	0.661	0.325	33%
1	0.381	0.788	33%	0.648	0.463	42%
2	0.386	0.766	34%	0.630	0.469	43%
3	0.360	0.579	38%	0.476	0.437	48%
4	0.308	0.416	43%	0.342	0.374	52%
5	0.249	0.271	48%	0.223	0.303	58%
6	0.192	0.165	54%	0.135	0.234	63%
7	0.143	0.089	62%	0.073	0.174	70%
8	0.104	0.040	72%	0.033	0.126	79%
9	0.073	0.010	88%	0.009	0.089	91%
10	0.050	-0.006	114%	-0.005	0.061	109%
Mean	-	-	55%	-	-	63%

Notes: Horizon measured in year units. We differentiate between compensation of government employees, G_{publ} and the purchase of goods and services from the private sector, G_{priv}. We generate impulse response functions by using a simple VAR, $z^G_{i,t} = [\epsilon^G_{i,t}, g_{it}, g_{publ,i,t}, g_{priv,i,t}]$ and $z^G_{i,t} = [\epsilon^G_{i,t}, g_{it}, g_{priv,i,t}, g_{publ,i,t}]$, with 2 lags. To identify the government spending shock $\epsilon^G_{i,t}$ we estimate the VAR model that includes aggregate variables, i.e., $z_{i,t} = [g_{i,t}, y_{i,t}, l_{i,t}, je_{i,t}, w_{C,i,t}]$, and adopt a Cholesky decomposition. The third and the sixth column of the table displays the contribution of the response of labor compensation of government employees to the change in government final consumption expenditure while the last line shows the average contribution of this component. Data coverage: 1970-2007 for AUT, CAN, DNK, ESP, FIN, FRA, GBR, IRL, ITA, JPN, NLD, NOR, SWE, USA, except BEL (1976-2007). In all specifications, all variables are real and scaled by the working age population.

fects by crowding-in consumption and private-sector employment. The expansionary effect triggered by public employment shocks can be rationalized by assuming a complementarity of the public good with private consumption in the aggregate consumption bundle of the household. This complementarity overturns the negative wealth effect of the shock and leads to an increase in consumption. Public wage shocks stimulate the production of the public good, which thus raises consumption given the complementarity of the latter with the public good. Because a wage government consumption shock produces an increase in government value added, which is biased toward non traded goods, along with an increase in private consumption that leads to a current account deficit, which further biases the government spending shock toward non tradables (since traded goods can be imported while non tradables must be produced by the home country), the non traded sector should be highly intensive in a shock to compensation of government employees. The relative price of non tradables thus appreciates significantly, which provides strong incentives to shift resources toward the non traded sector. Consequently, the share of non tradables increases sharply while the relative size of the traded sector declines substantially.

The results for a **non-wage government consumption shock** (solid black lines) are shown and contrasted with those for the baseline (solid blue lines) VAR model that includes total government consumption expenditure in Figures 30 and 31. To facilitate the interpretation of our results, we normalize the impulse responses so that government purchases of goods and services from the private sector or government consumption expenditure increases by one percentage point of GDP on impact. When we investigate the effects of a rise in government purchases of goods and services from the private sector, we estimate the effects on private activity. As can be seen in Figure 30, we find that a non-wage government consumption shock has a contractionary effect on economic activity as real GDP and total hours worked decline. To further understand the underlying mechanism leading to a contraction in private activity, we estimate a VAR model that includes non-wage government consumption expenditure, compensation of government employees, real GDP, hours worked, private investment and the real consumption wage; we find that an exogenous non-wage government consumption shock lowers compensation of government employees significantly. Thus the production of public goods falls. As long as private consumption and public goods are complements, the decline in the production of public goods along with the negative wealth effect imply that a non-wage government spending shock has a contractionary effect on economy activity. Because government purchases of goods and services from the private sector are biased toward non traded goods, the relative price of non tradables appreciates and the share of non tradables increases. However, as shown in Figure 31, the share of non tradables increases less following a non-wage government consumption shock than after a rise in compensation of government employees. One potential interpretation of this finding is that the non traded sector is relatively less intensive in non-wage government consumption shocks. As can be seen in Figure 31, it might explain the smaller appreciation in the relative wage of non tradables. An additional explanation is that the combined effect of the decline in the production of public goods and the complementarity between private and public goods crowds-out consumption which mitigates the current account deficit and thus makes the government spending shock less biased toward non tradables.

There is a growing literature exploring the impact of a government spending shock on private activity and contrasting the effects of a rise in government final wage consumption expenditure with those caused by an increase in government purchases of goods and services from the private sector. In particular, Cavallo [2005] and Li [2014] study the effects of shocks to different components in government spending, such as more money spent in the private sector or more expenditure in the government sector, by using a neoclassical and a new-keynesian model, respectively. In our paper, we are interested rather in the reallocation effects between a traded and non traded sector of a government spending shock in an open economy and merge the (non traded) private and government (non traded) sectors which form the non traded sector. A government spending shock can be viewed as the result of shocks to government consumption of non tradables and tradables or alternatively as the result of shocks to wage and non-wage government consumption. In our paper, we adopt the first view and shed some light on the role of imperfect mobility of labor between the traded and non traded sectors. As exemplified by the paper by Bermperoglou, Pappa, and Vella [2016], the objective of the literature which investigates the effects of a rise in compensation of government employees is very different from ours, as the authors aim at exploring the impacts on private activity, while we are interested in the reallocation effects across sectors.

Using data from COFOG (source: OECD), government consumption expenditure can be split between expenditure non traded goods (G^N) and expenditure on traded goods (G^T). In subsection D.1, we provide some evidence which reveal that government consumption on non traded goods contributes substantially to unforeseen changes in government consumption expenditure. We now investigate the contribution of sub-components of government consumption expenditure on non tradables following a government spending shock.

Collective vs. individual consumption expenditure on non tradables by the government. Government final consumption expenditure on non tradables can be divided into individual consumption expenditure and collective consumption expenditure. The split between individual and collective consumption is straightforward. In accordance with the COFOG classification, 'Health', 'Recreation and culture', 'Education', and 'Social protection' are provided for allocative and/or distributive motive and can be aggregated under the general heading *Individual consumption expenditure of the Government* which we denote by G_{ind}. As pointed out by the manual of COFOG, *Individual consumption expenditure of the Government* is close to the definition of private and semi-public goods. The remaining functions are classified as *Collective consumption expenditure of the Government* which we denote by G_{coll}. In terms of the economic theory, collective consumption expenditure by the government includes expenditure on National Defense, Public Order, *R&D*, ... and thus approximates the definition of pure public goods. As can be seen in column 5 of Table 19, the average government consumption expenditure on non tradables share of collective consumption expenditure by the government, i.e., G^N_{coll}/G^N, is almost 30%. It varies from a low of 21% in Denmark to a high of 53% in the US.

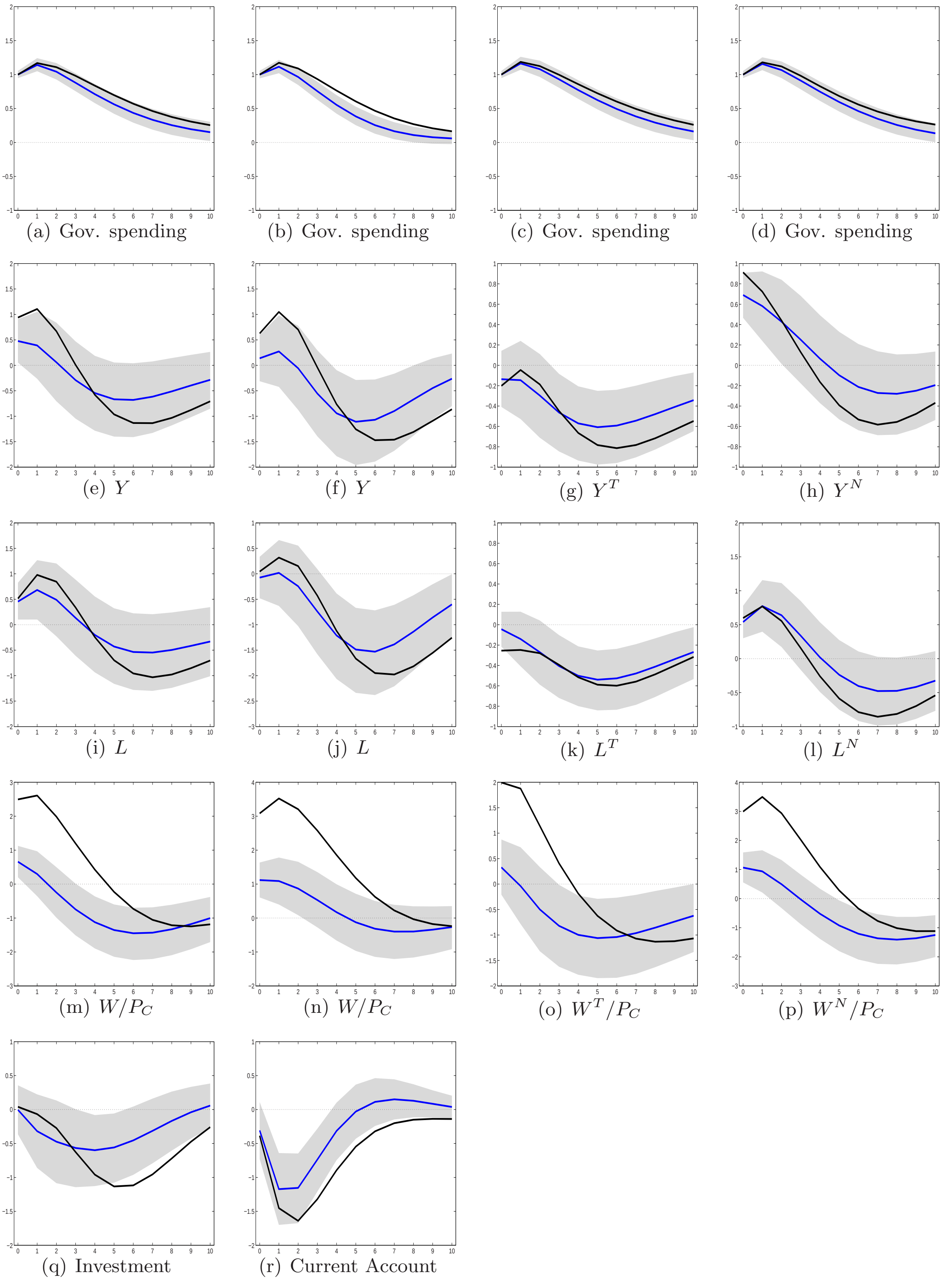


Figure 28: Aggregate and Sectoral Effects of an Unanticipated Government Final Wage Consumption Shock. Notes: Exogenous increase in government final (wage) consumption expenditure by 1% of GDP. VAR models include government final consumption expenditure (baseline) or government final wage consumption expenditure ordered first. Results for the baseline specification are displayed by solid blue lines with the shaded area indicating the 90 percent confidence bounds obtained by bootstrap sampling; the solid black line displays the results following a wage government consumption shock; sample: 15 OECD countries, 1970-2007 (except for BEL: 1976-2007), annual data.

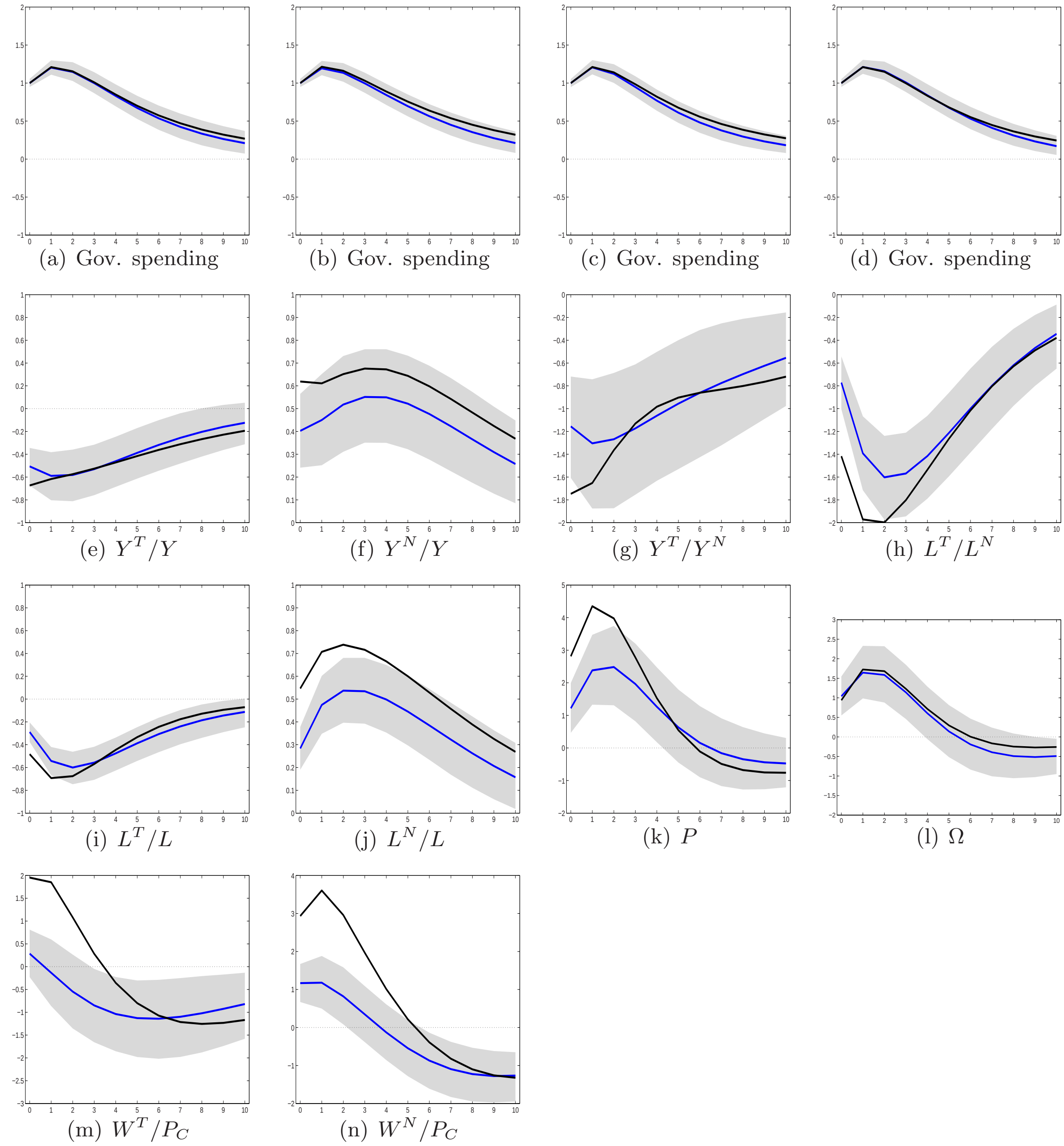


Figure 29: Effects of an Unanticipated Government Final Wage Consumption Shock on Sectoral Composition. Notes: Exogenous increase in government final (wage) consumption expenditure by 1% of GDP. VAR models include government final consumption expenditure (baseline) or government final wage consumption expenditure ordered first. Results for the baseline specification are displayed by solid blue lines with the shaded area indicating the 90 percent confidence bounds obtained by bootstrap sampling; the solid black line displays the results following a wage government consumption shock; sample: 15 OECD countries, 1970-2007 (except for BEL: 1976-2007), annual data.

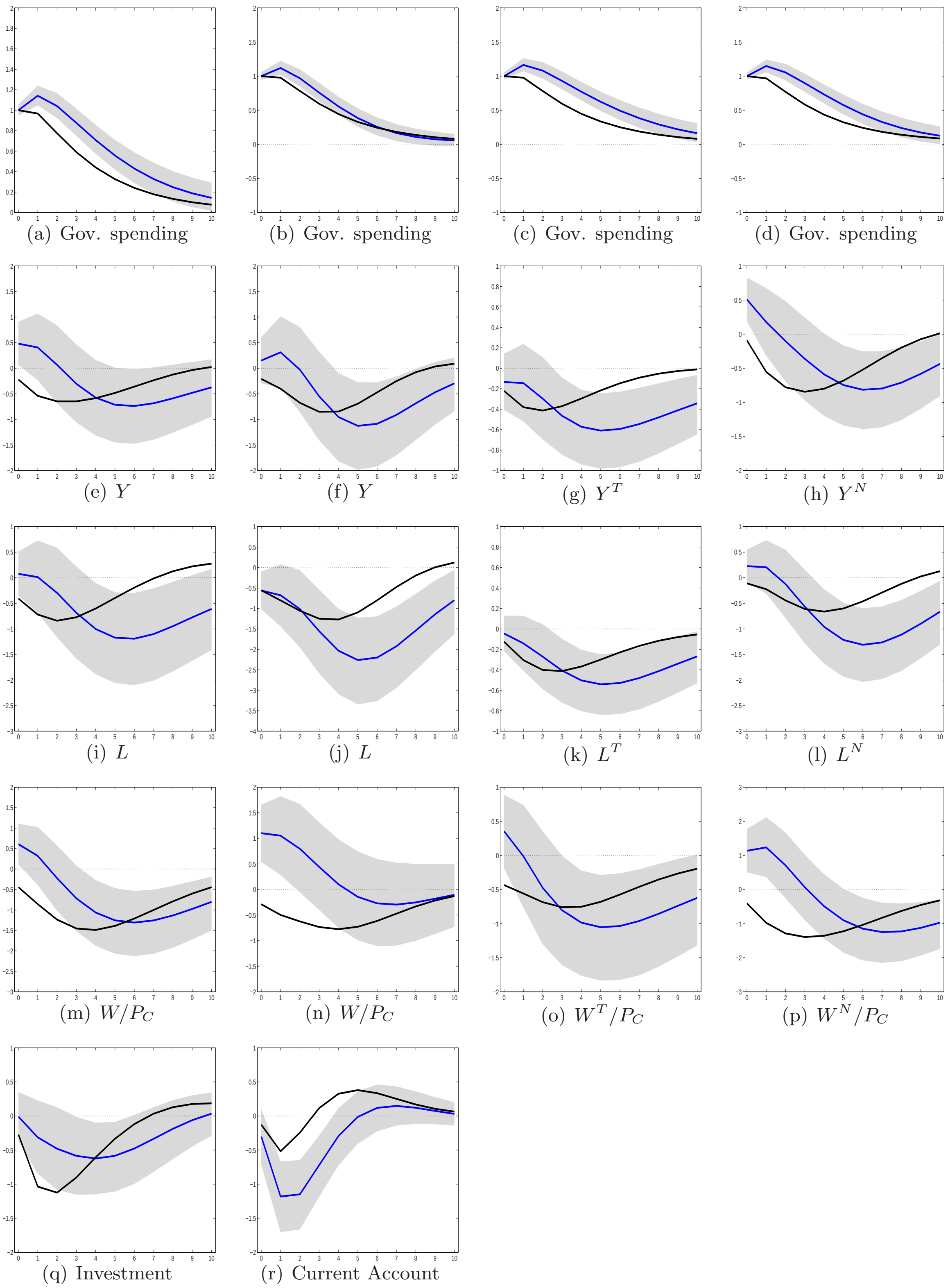
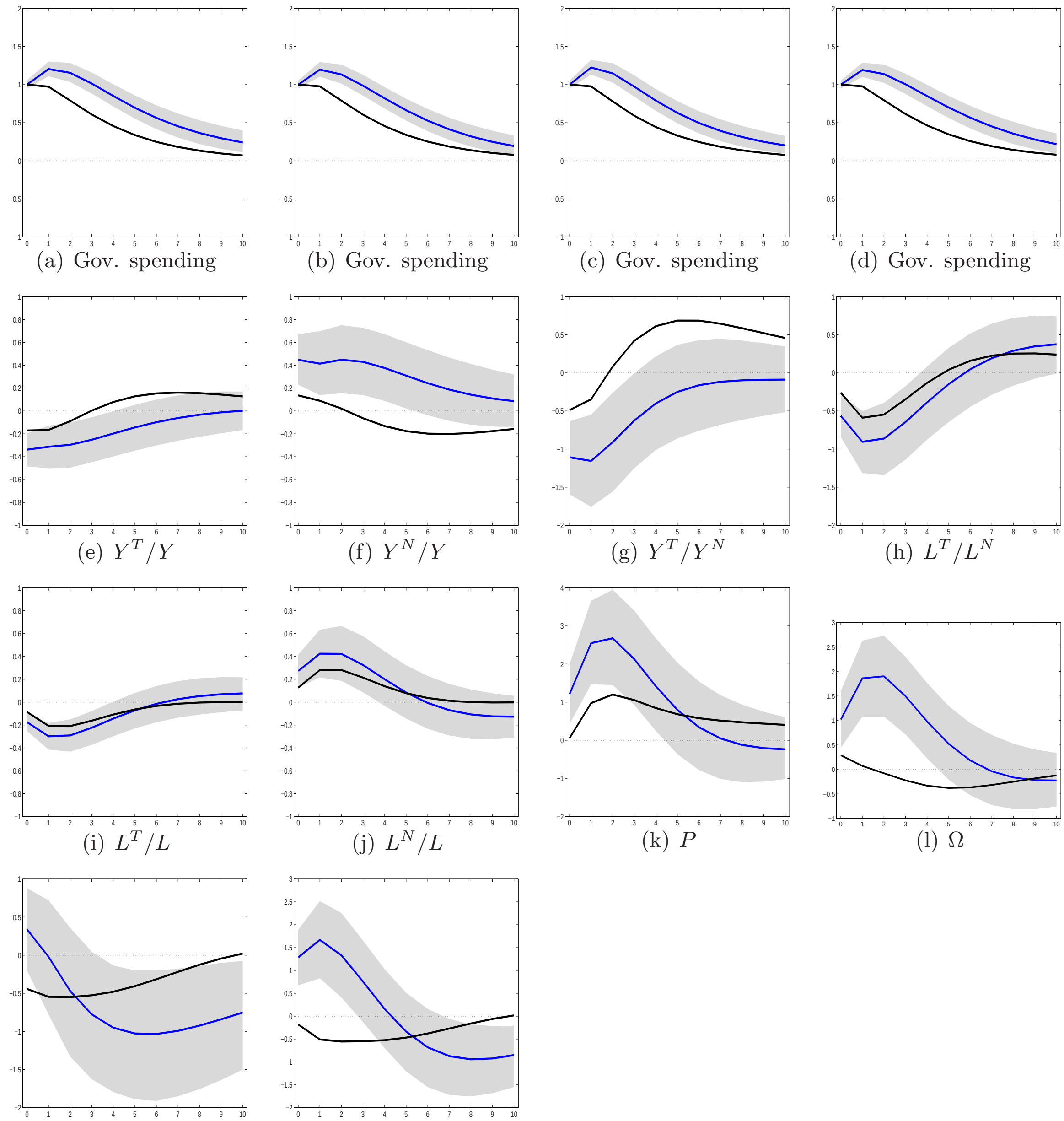


Figure 30: Aggregate and Sectoral Effects of an Unanticipated Shock to Government Purchases on Goods and Services from the Private Sector. Notes: Exogenous increase in government final (non-wage) consumption expenditure by 1% of GDP. VAR models include government final consumption expenditure (baseline) or government final consumption expenditure from the private sector ordered first. Results for the baseline specification are displayed by solid blue lines with the shaded area indicating the 90 percent confidence bounds obtained by bootstrap sampling; the solid black line displays the results following a non-wage government consumption shock; sample: 15 OECD countries, 1970-2007 (except for BEL: 1976-2007), annual data.



(a) Gov. spending (b) Gov. spending (c) Gov. spending (d) Gov. spending

(e) Y^T/Y (f) Y^N/Y (g) Y^T/Y^N (h) L^T/L^N

(i) L^T/L (j) L^N/L (k) P (l) Ω

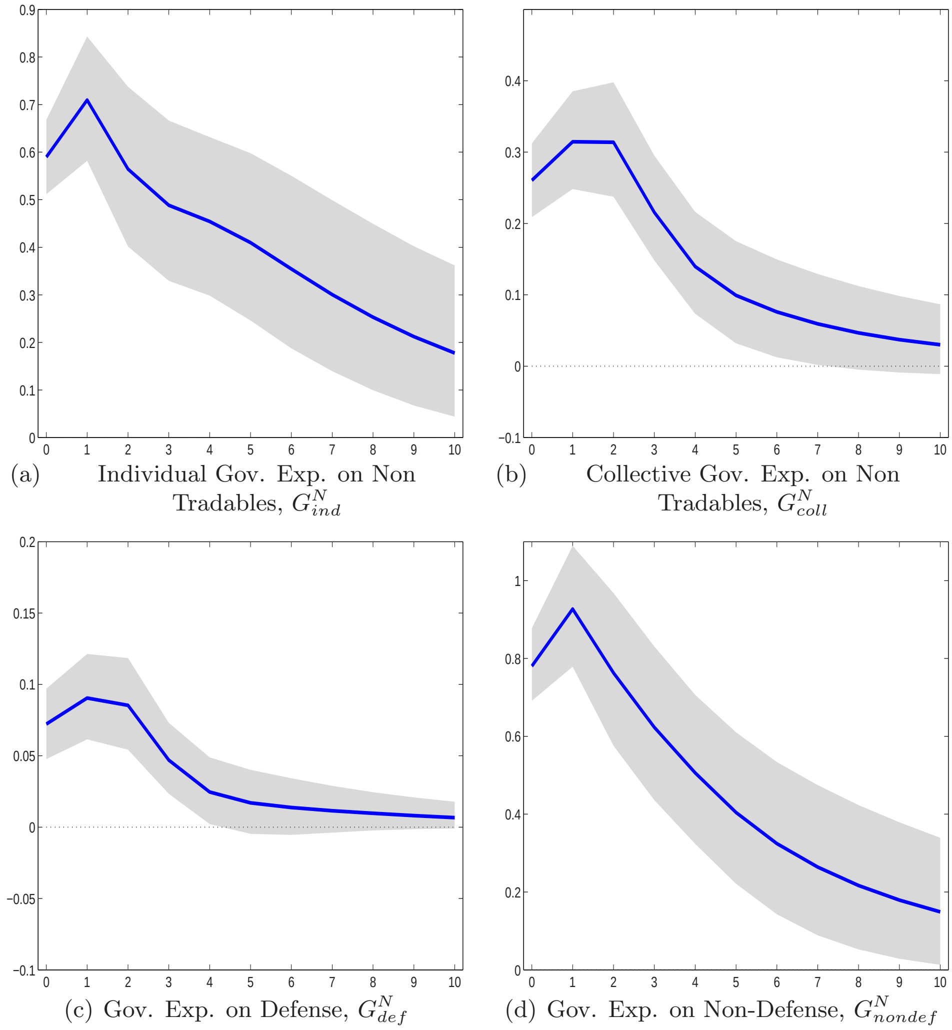
(m) W^T/P_C (n) W^N/P_C

Figure 31: Effects of an Unanticipated Shock to Government Purchases on Goods and Services from the Private Sector on Sectoral Composition. Notes: Exogenous increase in government final (non-wage) consumption expenditure by 1% of GDP. VAR models include government final consumption expenditure (baseline) or government final consumption expenditure from the private sector ordered first. Results for the baseline specification are displayed by solid blue lines with the shaded area indicating the 90 percent confidence bounds obtained by bootstrap sampling; the solid black line displays the results following a non-wage government consumption shock; sample: 15 OECD countries, 1970-2007 (except for BEL: 1976-2007), annual data.

Defense vs. non-defense consumption expenditure on non tradables by the government. A potential alternative breakdown can be performed on the basis of evidence provided by the empirical literature adopting a (Ramey-Shapiro) narrative approach that considers major political events leading to large military buildups, see e.g., Ramey and Shapiro [1998], Ramey [2011]. One key finding documented by Ramey [2011] in an older version (2007) of the paper published in QJE is that shocks to defense spending account for a substantial share of the forecast error variance of total government spending. We thus conduct a robustness check by differentiating between defense spending, G_{def}, and non-defense spending, G_{nondef}. As can be seen in column 6 of Table 19, the average government consumption expenditure on non tradables share of defense expenditure by the government, i.e., G^N_{def}/G^N, is 8% only. While the share of defense expenditure in G^N is lower than 10% for most of the countries in our sample, it averages 12% and 27% for the UK and the US, respectively.

How components of government final consumption expenditure on non tradables react to our identified government shock? We first estimate the first VAR model that includes government final consumption expenditure, real GDP, total hours worked, private investment, the real consumption wage, in order to identify unanticipated government spending shocks. Then, we estimate a VAR model in panel format on annual data that includes unanticipated government spending shocks, ϵ^G, ordered first, government spending,, g, individual, g^N_{ind} (defense, g^N_{def}), and collective (non-defense, g^N_{nondef}), g^N_{coll}, government final consumption expenditure on non tradables, i.e., $z^{G^N}_{i,t} = [\epsilon^G_{i,t}, g_{it}, g^N_{k,i,t}, g^N_{-k,i,t}]$ where $k = ind, def$ and $-k = col, nondef$. Table 21 reports at various horizons the mean responses of the two components to the identified government spending shock for two alternative breakdowns. We normalize the impulse responses so that government spending rises by one percentage point of GDP on impact. Since the ordering of variables does not matter, we do not present the results for different orderings. Focusing first on the first two columns of Table 21, a government spending shock by 1 percentage point of GDP increases individual government final consumption expenditure on non tradables by 0.59 percentage point of GDP on impact (i.e., 'Health', 'Recreation and culture', 'Education', and 'Social protection'). The spending shock also raises collective expenditure by 0.26 percentage point of GDP. The contribution of the response of individual expenditure to the rise in government expenditure on non tradables is displayed in the third column of Table 21 while the average contribution of this component is shown in the last line. The average contribution of individual expenditure to the rise in government final consumption expenditure on non tradables is 77% approximately and thus the contribution of collective expenditure is 23% only. Hence, while the rise in government consumption of non tradables is a major part of the government spending shock, the increase in individual expenditure accounts for more than three-quarters of increases in government consumption of non tradables. Impulse response functions for the two components of government final consumption expenditure on non tradables we generate following a rise in government spending by 1% of GDP are displayed in solid blue lines in the first row of Figure 32. The responses of both components are hump-shaped. We may notice that the rise in individual expenditure is more persistent.

Turning to the last two columns of Table 21, a government spending shock by 1 percentage point of GDP increases spending related to "Defense" by 0.07 percentage point of GDP, in line with its average share in government expenditure on non tradables shown in Table 19. As can be seen in the last line of Table 21, the average contribution of military spending to the rise in government final consumption expenditure on non tradables is 6% while the contribution of other expenditure is 94%. Impulse response functions for the two components of government final consumption expenditure on non tradables we generate following a rise in government spending by 1% of GDP are displayed in solid blue lines in the second row of Figure 32. The responses of both components are hump-shaped. We may notice that the increase in defense spending is much less persistent.



(a) Individual Gov. Exp. on Non Tradables, G^N_{ind}

(b) Collective Gov. Exp. on Non Tradables, G^N_{coll}

(c) Gov. Exp. on Defense, G^N_{def}

(d) Gov. Exp. on Non-Defense, G^N_{nondef}

Figure 32: Effects of an Unanticipated Government Spending Shock on Components of Government Final Consumption Expenditure on Non Tradables and Tradables. Notes: Exogenous increase in government consumption by 1% of GDP. The government spending shock is identified by estimating a VAR model that includes real government final consumption expenditure, GDP (constant prices), total hours worked, private fixed investment, and the real consumption wage. We differentiate between collective and individual government final consumption expenditure on non tradables in the first row, and we distinguish between government final consumption expenditure on defense and non-defense in the second row (both classified as non tradables). The responses of components of government final consumption expenditure on non tradables to the identified government spending shock are displayed by solid blue lines with the shaded area indicating the 90 percent confidence bounds obtained by bootstrap sampling; sample: 13 OECD countries, 1995-2015, annual data.

Table 21: Responses of Components of Government Consumption Expenditure on Non Tradables to Identified Government Spending Shock: Point Estimates

Horizon	$z^{G^N} = [\epsilon^G, g, g^N_{ind}, g^N_{coll}]$		Contribution	$z^{G^N} = [\epsilon^G, g, g^N_{def}, g^N_{nondef}]$		Contribution
	G^N_{ind}	G^N_{coll}	of G^N_{ind}	G^N_{def}	G^N_{nondef}	of G^N_{def}
0	0.590	0.260	69%	0.072	0.780	8%
1	0.710	0.315	69%	0.090	0.927	9%
2	0.564	0.314	64%	0.085	0.763	10%
3	0.488	0.216	69%	0.047	0.623	7%
4	0.454	0.140	76%	0.025	0.506	5%
5	0.410	0.099	81%	0.017	0.404	4%
6	0.354	0.076	82%	0.014	0.324	4%
7	0.301	0.059	84%	0.011	0.264	4%
8	0.253	0.047	84%	0.010	0.217	4%
9	0.212	0.037	85%	0.008	0.179	4%
10	0.178	0.030	86%	0.007	0.149	4%
Mean	-	-	77%	-	-	6%

Notes: Horizon measured in year units. We generate impulse response functions by using a simple VAR with 2 lags, $z^{G^N}_{i,t} = [\epsilon^G_{i,t}, g_{it}, g^N_{k,i,t}, g^N_{-k,i,t}]$ where $k = ind, def$ and $-k = col, nondef$. To identify the government spending shock $\epsilon^G_{i,t}$ we estimate the VAR model that includes aggregate variables, i.e., $z_{i,t} = [g_{i,t}, y_{i,t}, l_{i,t}, je_{i,t}, w_{C,i,t}]$, and adopt a Cholesky decomposition. The third and the sixth column of the table displays the contribution of the responses of individual government final consumption expenditure on non tradables and defense expenditure to the change in government consumption of non tradables while the last line displays the average contribution of the response of each component to the change in government consumption expenditure on non tradables. Data coverage: 1995-2015 for AUT, BEL, DNK, ESP, FIN, FRA, GBR, IRL, ITA, NLD, NOR, SWE and the USA. In all specifications, all variables are real and scaled by the working age population, and a linear trend is included.

D.3 Comparison of our Estimated Sectoral Effects with those Documented by Earlier Empirical Studies

Monacelli and Perotti (MP henceforth) [2008] and Benetrix and Lane [2010] (BL henceforth) conduct an empirical investigation of the sectoral output effect of a government spending shock by differentiating the traded from the non traded sector. These earlier studies give us the opportunity to address any potential discrepancy between their results and our own VAR evidence. Both MP [2008] and BL [2010] find empirically that a government spending shock produces a much larger increase in non traded output than in traded output. Our estimates corroborate this finding. Nevertheless, we find that traded output falls slightly on impact and remains below trend while the fiscal shock is in effect. MP [2008] also reports a slight decline in traded output on impact like us whereas the authors find that the traded output adjustment is bell-shaped and thus increases significantly above its trend after about two years. BL [2010] detects a positive response of traded output on impact followed by a gradual decline.

We emphasize below the main differences with MP's [2008] and BL's [2010] analysis. Monacelli and Perotti [2008] take a different approach from ours in two respects. First, they restrict attention to the US, using quarterly data from 1954 to 2006 while we consider a sample of 16 OECD economies over 1970-2007 and estimate a VAR model in panel format on annual data. Second, Monacelli and Perotti [2008] refer to industries producing services as non tradables and thus take a different approach from ours since we treat industries 'Financial intermediation' and 'Transport and Communication' as tradables instead of non tradables. In order to investigate whether this discrepancy is attributable to the sample, we re-estimate the VAR specification that includes government consumption, sectoral value added at constant prices, sectoral hours worked and the sectoral real consumption wage, on U.S. annual data over 1970-2007, keeping our own classification for tradables and non tradables. We generate impulse response functions which are normalized so that government consumption increases by 1 percentage point of GDP. The solid blue line in Figure 25 reports the results following a rise in total government consumption while the solid black line reports results following a rise in government consumption of non tradables. The first column shows results for the traded sector while the second column shows results for the non traded sector. Like MP [2008], our evidence shows that traded output falls on impact and then increases. The adjustment in traded output displays an inverted U-shaped pattern while traded output remains above trend.

A close empirical analysis to ours is that performed by BL [2010]. Like BL [2010], we estimate a panel VAR on annual data and investigate the effects of a government spending shock (identified by adopting Blanchard and Perotti's [2002] method) on traded and non traded output. Yet, our empirical analysis differs in four respects:

- **Sample**. First, regarding the sample, we use a panel of 16 OECD economies over 1970-2007 while BL [2010] consider a sample of 11 EMU countries over 1970-2005. Since we have eight countries in common with BL [2010]: Austria (AUT), Belgium (BEL), Finland (FIN), France (FRA), Ireland (IRL), Italy (ITA), the Netherlands (NLD) and Spain (ESP), we estimate VAR models by using this sample restricted to 8 EU countries over the period 1970-2005.[68]

- **Classification T/N**. Second, BL [2010] treat 'Transport, Storage and Communication' and 'Financial Intermediation' as non traded rather than traded industries, and classify 'Electricity, Gas and Water Supply' in the traded sector while we treat this industry as non tradable.

- **VAR specification**. Third, our VAR specifications are different from those considered by BL [2010]. More specifically, to explore the size of the sectoral fiscal multiplier empirically, we consider a VAR specification $z_{it}^{j} = \left[g_{it}, y_{it}^{j}, l_{it}^{j}, w_{C,it}^{j}\right]$ with $j = T, N$, while BL's [2010] VAR model includes government consumption, traded value added, non traded value added. All variables are in real terms and logged. In terms of our own notations, the VAR specification considered by BL [2010] is: $z_{it}^{BL} = \left[g_{it}, y_{it}^{T}, y_{it}^{N}\right]$.

- **Construction of variables**. Finally, when we estimate the VAR model, all variables are measured in log, real terms and per capita (except for the current account), while prices and wages are logged, in line with the current practice. In contrast, quantities are not scaled by the working age population in BL [2010].

In the following, 'CCR' is a contraction of Cardi, Claeys and Restout while 'BL' is a contraction of Benetrix and Lane. Because BL [2010] find that traded output increases in the short-term while our VAR evidence indicates that traded output is slightly negative on impact, then declines and remains below trend while the fiscal shock is in effect, we investigate below the cause of this discrepancy in the estimated contraction in traded output. Since our empirical analysis differs along of four dimensions, namely the sample, the classification T/N, the VAR specification, and data construction, we run several experiments. While we contrast the dynamic effects of a government spending shock by 1 percentage point of GDP across the four alternative experiments in Figure 33-35, for clarity purposes, we first report the impact response of traded output in Table 22. Inspection of the first line of Table 22 shows immediately that the sample is the cause of the discrepancy, i.e., restricting the sample to 8 countries changes the response of traded output from negative to positive, regardless of the classification, VAR specification and the construction of variables. As shown below, the comparison of IRF across alternative scenarios also shows that the construction of variables plays a substantial role as the rise in traded output is more persistent when variables are not scaled by the population.

In each experiment, we focus on the responses of traded and non traded output and thus report neither IRF for sectoral hours worked nor real consumption wages to save space and for clarity purposes as BL [2010] do not consider these variables in their study.

- **Classification T/N** and **VAR specification**. First, we investigate whether the classification of industries as traded or non traded and/or the VAR specification is responsible for the differences in the short-run response of traded output to a fiscal shock. In columns 1-4 of Table 22 we consider our own sample and compare our baseline results (column 1) with those obtained when adopting BL's classification

[68] We excluded Germany, Greece, Portugal as these countries lack data for a number of aggregate variables.

Table 22: Impact Response of Traded Output to a Fiscal Shock

	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)	(15)	(16)
$dY^T(0)/dG$	-0.032	-0.135	-0.109	-0.146	0.579*	0.231	0.340	0.135	-0.020	-0.126	-0.102	-0.148	0.625*	0.299	0.380	0.192
Nb of countries	16	16	16	16	8	8	8	8	16	16	16	16	8	8	8	8
Last period	2007	2007	2007	2007	2005	2005	2005	2005	2007	2007	2007	2007	2005	2005	2005	2005
Classification	CCR	BL	CCR	BL	CCR	BL	CCR	BL	CCR	BL	CCR	BL	CCR	BL	CCR	BL
VAR specification	CCR	CCR	BL	BL	CCR	CCR	BL	BL	CCR	CCR	BL	BL	CCR	CCR	BL	BL
Population scaling	yes	yes	yes	yes	yes	yes	yes	yes	no	no	no	no	no	no	no	no

Notes: Last period refers to the last observation of the period used to estimate the VAR (both samples start in 1970). The sectoral classification CCR (BL resp.) refers to the sectoral classification used in the present (BL's resp.) paper. The CCR specification is the model with $z_{it}^j = \left[g_{it}, y_{it}^T, l_{it}^T, w_{C,it}^T\right]$ while the BL specification indicates the VAR model with $z_{it}^{BL} = \left[g_{it}, y_{it}^T, y_{it}^N\right]$. In all estimations, we include a country-fixed effect and a country-specific linear trend and two lags are specified in the VAR model. Population scaling indicates if quantities variables included in the VAR models are scaled or not by the working age population. * denotes significance at 10% level.

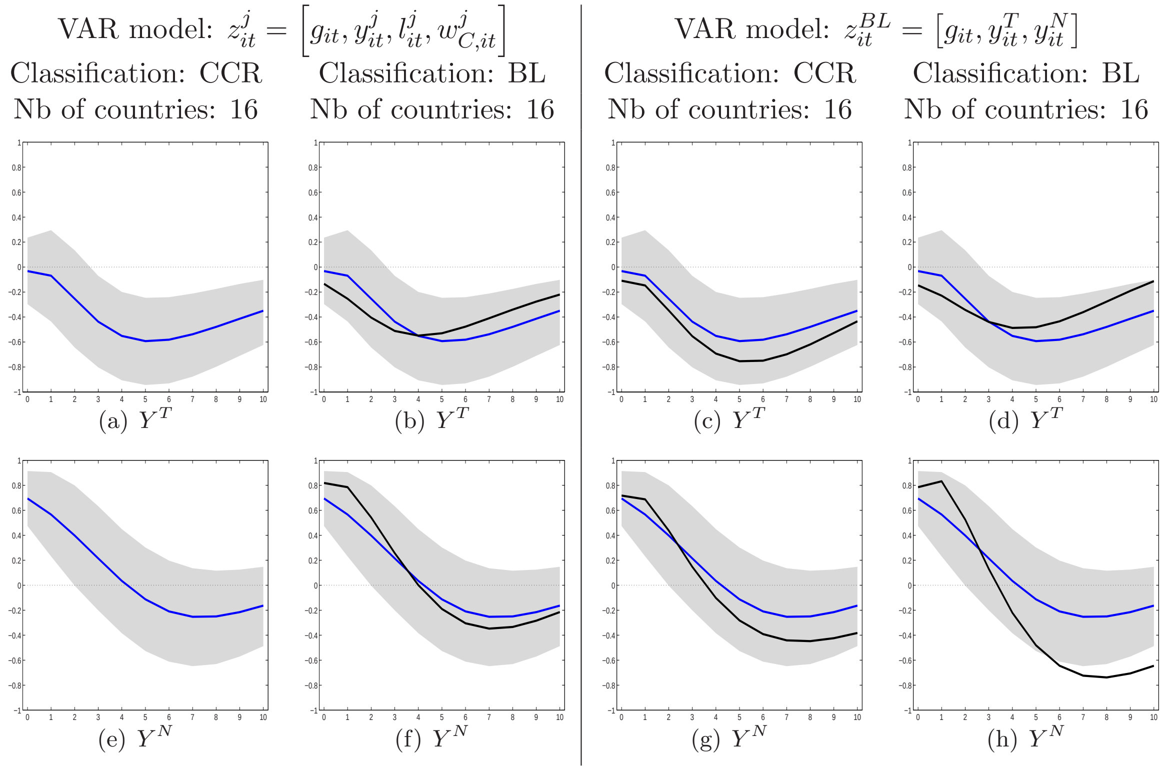


Figure 33: Effects of an Unanticipated Government Spending Shock on Sectoral Variables. Notes: Exogenous increase in government consumption by 1% of GDP. **Sample: 16 OECD Economies (1970-2007)**. The first column shows results for our classification T/N along with our VAR specification. The second, third and four columns show results when considering BL's [2010] classification, or VAR specification, or both, respectively. All quantities variables included in the VAR models are scaled by the working age population. Baseline: $N = 16$, classification CCR, VAR model $z_{it}^j = \left[g_{it}, y_{it}^j, l_{it}^j, w_{C,it}^j\right]$, $j = T, N$). Results for the baseline specification are displayed by solid blue lines with the shaded area indicating the 90 percent confidence bounds obtained by bootstrap sampling. Results for an alternative T/N classification or/and VAR specification are displayed by solid black lines.

T/N (column 2), BL's VAR specification [2010] (column 3), BL's construction of variables (column 4). The solid blue line in column 1 of Figure 33 shows our baseline results. In columns 2-4 of Figure 33, we contrast baseline results (displayed in the solid blue line) with those obtained when adopting BL's classification for T/N or their VAR specification (solid black line). Impact responses reported in columns 1-4 along with the dynamic responses show that traded output declines in the short-run and the discrepancy between the baseline scenario and alternatives is not statistically different. Thus neither the classification T/N nor the VAR specification seem to be responsible for the discrepancy in the short-term response of traded output to a fiscal shock.

- **Sample**. Second, we restrict the set of countries to those included in BL's [2010] sample. Columns 5-8 of Table 22 show the impact response of traded output when we restrict the set of countries to eight and run a number of experiments with respect to the classification T/N and VAR specification. The solid blue line in the first column of Figure 34 shows the IRF in the baseline scenario, i.e., when the sample covers 16 OECD countries, while the solid black line in columns 2-4 displays the results when the sample covers 8 countries. Columns 5-8 of Table 22 show that traded output increases in the short-run when we consider a similar set of countries as BL. As can be seen in the solid black line in Figure 34, traded output increases on impact whether we consider our own or BL's VAR specification, or whether we consider our own or BL's classification for T/N. Hence, alternative scenarios do not lead to substantially different results. While traded output increases in all cases, the expansionary effect

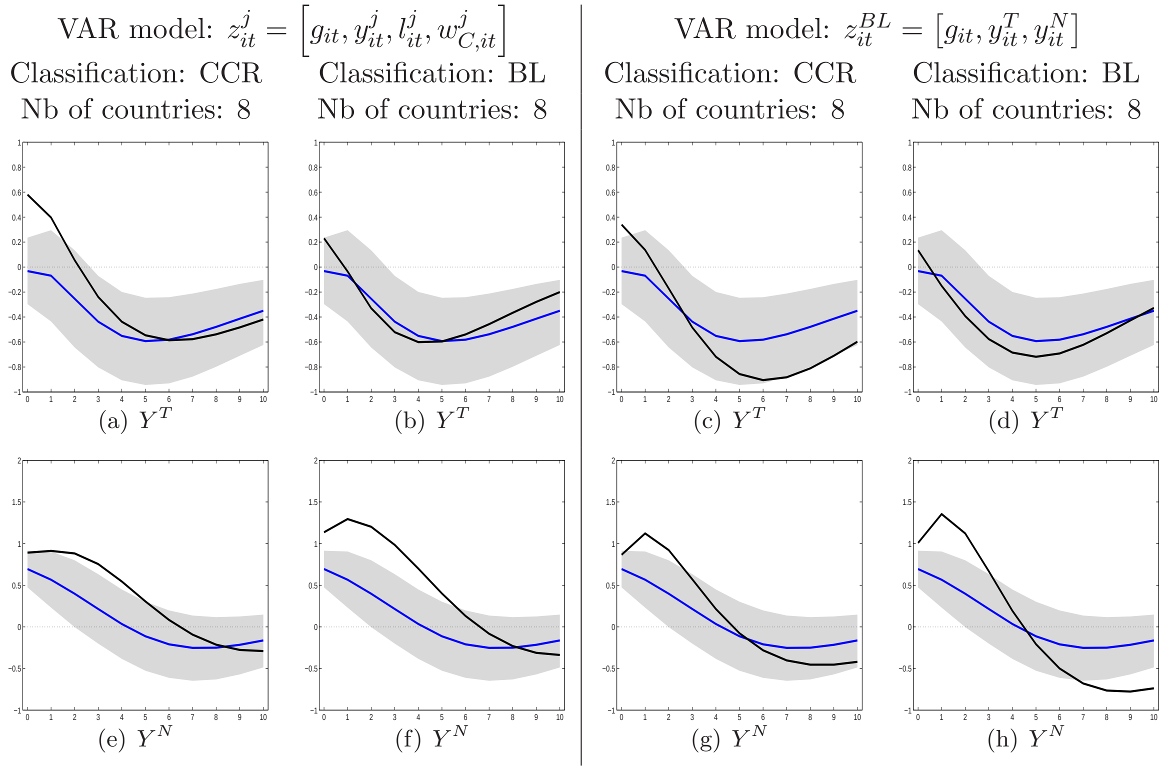


Figure 34: Effects of an Unanticipated Government Spending Shock on Sectoral Variables. Notes: Exogenous increase in government consumption by 1% of GDP. **Sample: 8 OECD Economies (1970-2005)**. The first column shows the results for our classification T/N along with our VAR specification. The second, third and four columns show results when considering BL's [2010] classification, or VAR specification, or both, respectively. All quantity variables included in the VAR models are scaled by the working age population. Baseline: $N = 16$, classification CCR, VAR model $z_{it}^{j} = \left[g_{it}, y_{it}^{j}, l_{it}^{j}, w_{C,it}^{j}\right]$, $j = T, N$). Results for the baseline specification are displayed by solid blue lines with the shaded area indicating the 90 percent confidence bounds obtained by bootstrap sampling. Results for an alternative T/N classification or/and VAR specification are displayed by solid black lines.

on traded output is not too persistent as it declines below trend after two years approximately.

- **Construction of variables**. Third, as it is common in the literature, all quantities are scaled by the working age population in order to remove trend. Since BL [2010] do not indicate whether they express quantities per capita, we run alternative experiments for both samples: our panel of 16 OECD economies over 1970-2007 and the 8 EMU countries we have in common with BL over the period 1970-2005. In all experiments, we contrast previous results when quantities are divided by the working age population with those obtained without expressing variables per capita. We consider our and BL's VAR specification, then our and BL's classification for T/N. The results for alternative scenarios are reported in columns 9-16 of Table 22. The conclusion that emerges is that when the set of countries is restricted to eight (see the last four columns), traded output increases substantially more when quantities are not scaled by the population. The dynamic effects of a government spending shock in Figure 35 reveal that the decline in traded output tends to be much less pronounced with a sample of 16 countries while the rise in traded output tends to be much more persistent when quantities are not scaled by the population and we restrict the set of countries to eight.

Since the set of countries matters for the response of traded output, we investigate the extent to which the responses of sectoral shares are modified when we restrict our sample to eight EU countries. Responses at various horizons are reported in Table 23. Reassuringly, our main conclusion holds: a government spending shock lowers significantly the share of

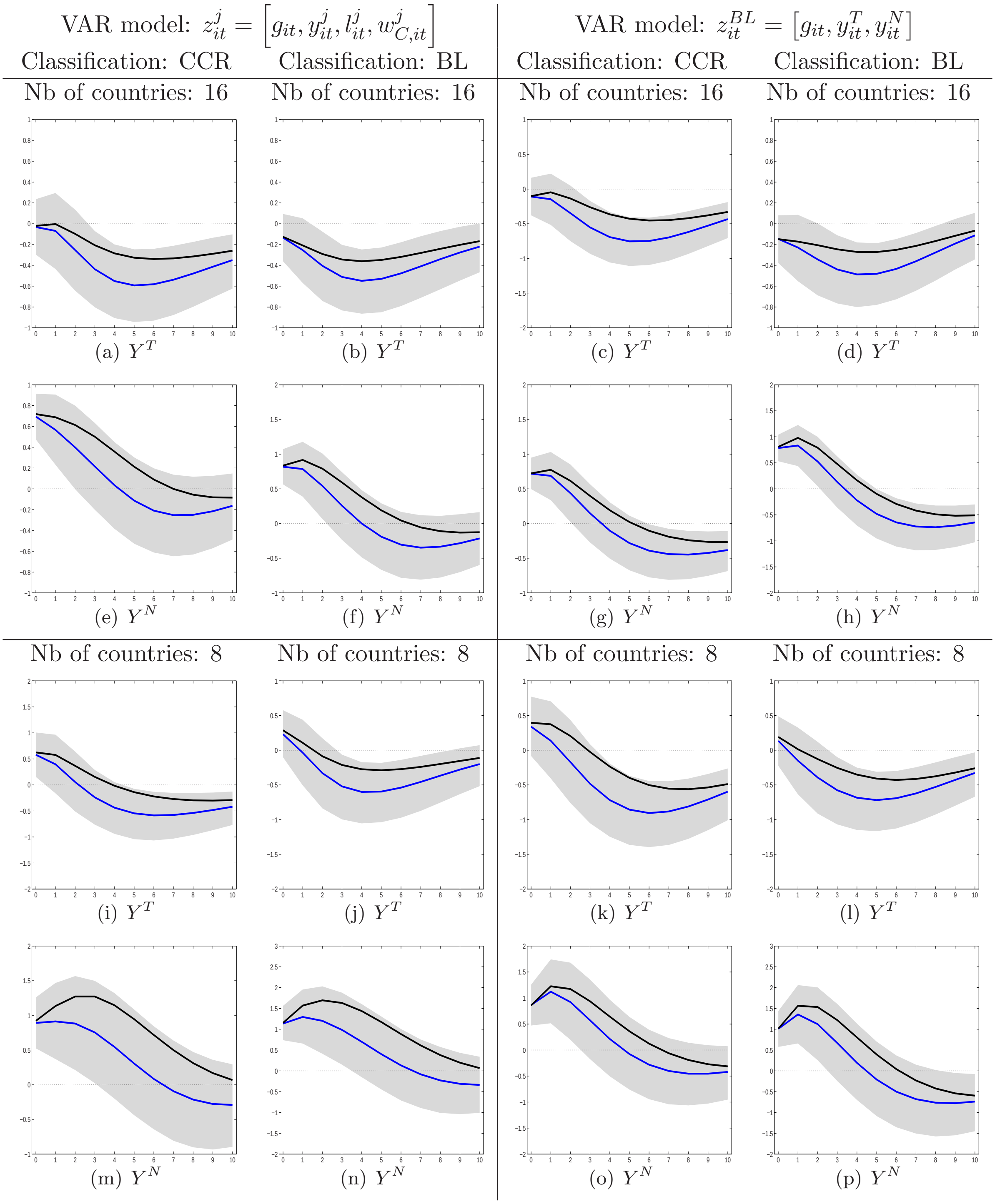


Figure 35: Effects of an Unanticipated Government Spending Shock on Sectoral Variables. Notes: Exogenous increase in government consumption by 1% of GDP. The first two rows show the results for a panel of 16 OECD countries over 1970-2007 while the last second rows show results for a panel of 8 OECD countries over 1970-2005. The first column shows the results for our T/N classification along with our VAR specification. The second, third and four columns show results when considering BL's [2010] classification, or VAR specification, or both, respectively. Blue line: the quantity variables included in the VAR models are scaled by the working age population; shaded areas: 90 percent confidence intervals; black line: quantity variables included in the VAR models are not scaled by the working age population.

Table 23: Short-run Responses of Sectoral Variables to a Fiscal Shock (1970-2007, 8 countries)

Horizon	Y^T/Y	Y^N/Y	L^T/L	L^N/L	Y^T/Y^N	L^T/L^N	P	Ω
0	-0.206	0.195	-0.150	0.151	-0.584	-0.481	1.672	1.247
1	-0.511	0.370	-0.426	0.407	-1.253	-1.301	2.764	1.853
2	-0.639	0.557	-0.553	0.527	-1.513	-1.689	2.987	1.909
3	-0.676	0.656	-0.588	0.565	-1.553	-1.805	2.697	1.485
Classification	CCR	CCR	CCR	CCR	CCR	CCR	CCR	CCR

Notes: entries report, for selected horizons, the instantaneous response of sectoral variables to an increase in government spending by 1% of GDP. Responses of Y^j/Y and L^j/L, $j = T, N$, stem from the VAR that includes $z_{it}^{S,j} = \left[g_{it}, \nu_{it}^{Y,j}, \nu_{it}^{L,j}, w_{C,it}^{j}\right]$. The response of relative labor L^T/L^N (relative output Y^T/Y^N resp.) is estimated from a 3-variable VAR that includes government spending, relative labor (relative output resp.) and the relative wage of non tradables Ω (relative price of non tradables P resp.). Sample: 1970-2005 and 8 countries (AUT, BEL, ESP, FRA, FIN, IRL, ITA and NLD). In all estimations, two lags are included in the VAR model. All quantities are scaled by the working age population.

tradables and increases the relative size of the non traded sector. Figure 36 shows the dynamic effects for a sample of eight countries. Again, all our results hold. The share of non tradables increases significantly over the first four years while the share of tradables declines substantially. We also find empirically that both the relative price and the relative wage of non tradables appreciate. We may nevertheless note some differences. In particular, the magnitude of the change in relative sector size is mitigated compared with the baseline case where we consider 16 countries.

To conclude, both the dataset and the construction of variables seem responsible for the discrepancy in the response of traded output in our empirical analysis and that documented by BL [2010]. When the set of countries is restricted to eight, traded output increases on impact, then declines rapidly below trend after two years. Keeping the same set of eight countries, when quantities are not scaled by the working age population, the increase in traded output is more pronounced and more persistent, as it takes about four years before traded output falls below trend. Whether the sample is restricted to eight or sixteen countries, non traded output increases substantially relative to traded output and thus our conclusion according to which government spending shocks are biased toward non traded goods holds. Importantly, in all scenarios, the share of non tradables in employment and real GDP rise which implies that non traded industries which are more intensive in the government spending shock experience a labor inflow.

D.4 Comparison of Aggregate Effects of Government Spending Shocks with those Documented in the Existing Literature

In the previous subsection, we address the main differences between the sectoral effects we document in our paper with those documented by past studies, in particular Benetrix and Lane [2010]. In this subsection, we contrast our empirical results on aggregate effects of government spending shocks with those documented in the empirical literature.

Overall, our panel VAR evidence for aggregate variables is well in line with that reported in earlier studies. In particular, our estimate of an aggregate output multiplier of government spending being lower than one on impact accords well with earlier findings. For example, Corsetti et al. [2012], who use a panel of 17 OECD countries for the period 1975-2008, report an increase in aggregate output by about 0.7 percentage points on impact. As documented in Corsetti et al., an increase in government spending leads to a protracted decline in private investment. The fall in the current account following a rise in public purchases is also in line with earlier findings. Although the empirical literature commonly uses net exports, replacing the current account with the trade balance leads to similar results. Beetsma, Giuliodori and Klaassen [2008] report a fall in the trade balance by 0.5% of GDP for a panel of 11 Euro Area Members while Corsetti et al. [2012] document a decline in net exports on impact which is very similar to ours.

Regarding labor market variables, our evidence reveal that a government spending shock increases hours worked, a finding that again squares well with conventional wisdom and

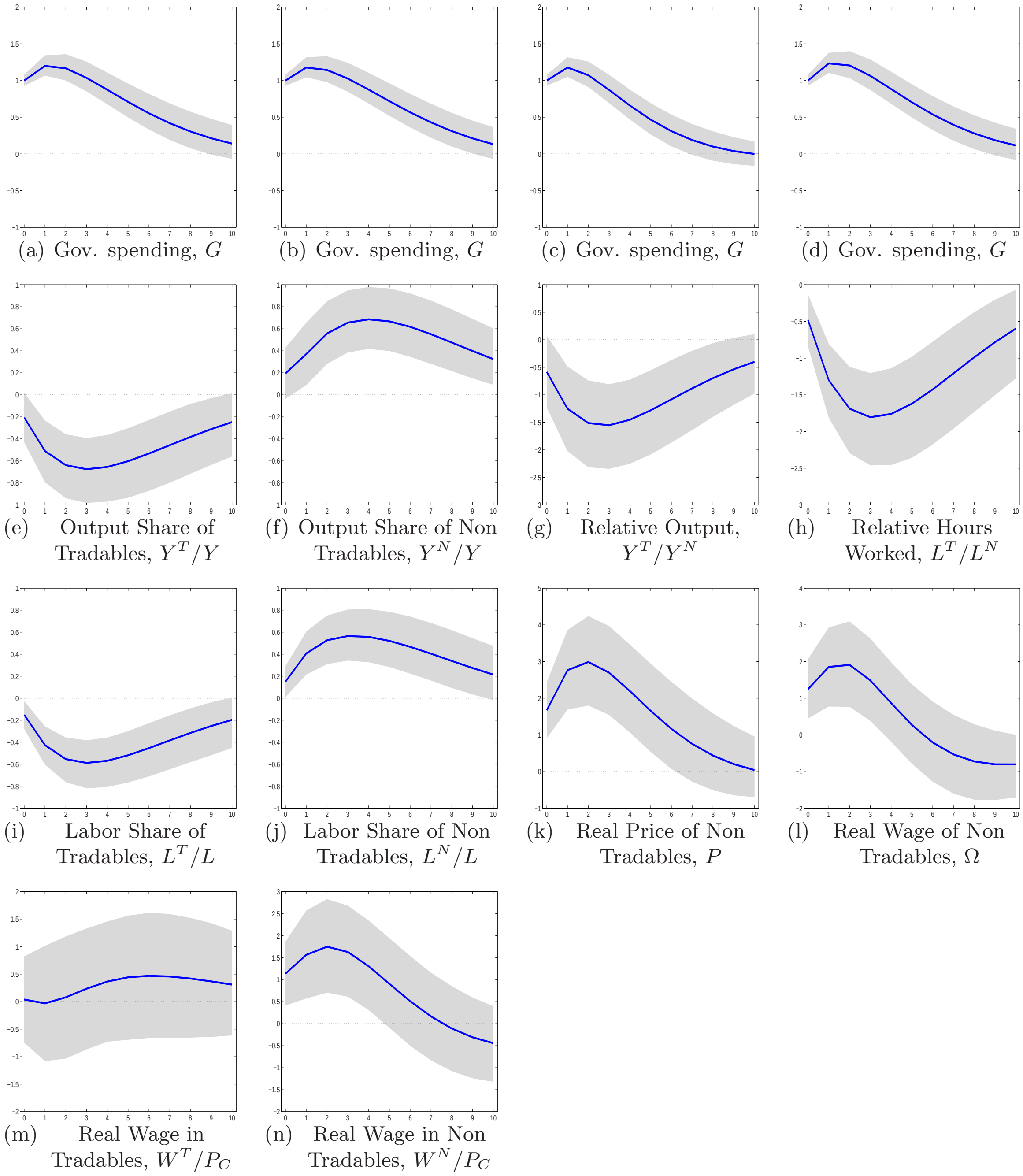


Figure 36: Effects of an Unanticipated Government Spending Shock on Sectoral Composition. **Sample: 8 EU Economies over 1970-2005**. Notes: Exogenous increase in government consumption by 1% of GDP. Results for the baseline specification are displayed by solid lines with the shaded area indicating the 90 percent confidence bounds obtained by bootstrap sampling.

earlier empirical studies, see e.g., Pappa [2009], Ramey [2011]. While there is no debate in the literature about the empirical facts mentioned above, the response of the real wage to a government spending shock is not a clear-cut result. As summarized by Nekarda and Ramey [2011], the literature adopting Blanchard and Perotti's [2002] approach to identifying fiscal shock reports an increase in the real consumption wage while application of the 'narrative' approach reveals that real consumption wages tend to fall in response to military spending shocks, see e.g., Ramey [2011]. While we find a significant rise in the real consumption wage on impact, our panel VAR evidence indicates that it is followed by a rapid decline. In this regard, our result can be viewed as halfway between these two strands of literature applying different identification schemes to U.S. data.

D.5 Anticipation Effects

In this subsection, we address a major concern regarding the evidence on fiscal transmission we document in the main text due to anticipation effects. As argued by Ramey [2011], Blanchard and Perotti's [2002] approach to identifying government spending shocks in VAR models may lead to incorrect timing of the identified fiscal shocks. If the fiscal shock is anticipated in advance, agents may have modified their decisions before the rise in government spending actually materializes. Consequently, when the fiscal shock is anticipated, and thus VAR approach captures the shocks too late, it misses the initial changes in variables that occur as soon as the news is learned. As a robustness check, we conduct below an investigation of the potential presence of anticipation effects which draws heavily on previous analysis performed by Beetsma and Giulodori [2011] and Born, Juessen and Müller [2013]. It is worth mentioning that, as argued by Beetsma and Giulodori [2011], the effects of anticipation of fiscal policy changes by market participants should be less relevant when using annual data since the fiscal shock is less likely to be anticipated one year before the rise in government spending is implemented than one quarter before it actually takes place.

Drawing on previous studies, we conduct three robustness exercises to explore the potential implications of anticipation effects:

- Like Beetsma and Giuliodori [2011], we run Granger-causality tests in order to investigate whether fiscal forecasts have any predictive power for the identified government consumption shocks.
- A second way to deal with the complications of possibly anticipated government spending shocks is to augment the VAR specification with the forecasts for government spending, see Beetsma and Giuliodori [2011], Born, Juessen and Müller [2013].
- A third route followed by Beetsma and Giuliodori [2011], Brückner and Pappa [2012] is to augment the baseline VAR specification with forward-looking variables such as short-term interest rates, the log of the GDP deflator, stock prices, or oil prices in order to control for fiscal-foresight effects.

In the following, we conduct an investigation of the potential presence of anticipation effects by performing the three robustness exercises mentioned above. To perform the first robustness exercise, we use a dataset constructed by Born, Juessen and Müller [2013] that contains time series for forecasts for government spending from the OECD.[69] Since the OECD prepares forecasts in June and December for each year, the dataset contains semi-annual observations for the period running from 1986 to 2011. To investigate the extent to which evidence on fiscal transmission can be affected by anticipation effects, we use the December forecasts. Data are available over the period 1986-2007 for CAN, FRA, GBR, ITA, JPN and USA, 1997-2007 for AUS, BEL, DNK, ESP, FIN, IRL, NLD, NOR, SWE and 1997-2004 for AUT. We denote fc_t^{t+1} the period$-t$ forecast of the growth rate of government spending for the next year $t+1$. This variable is constructed as the logarithm of real government consumption forecast minus the logarithm of real government consumption.

Before exploring empirically the VAR model augmented with forecasts for government spending, we first test whether the anticipation problem is relevant in our annual VAR.

[69]We thank Born, Juessen and Müller [2013] for providing this dataset to us.

Table 24: Granger Causality Tests (p-values)

Country	p-value	Country	p-value
AUS	0.545	GBR	0.042
AUT	0.090	IRL	0.752
BEL	0.884	ITA	0.017
CAN	0.218	JPN	0.000
DNK	0.617	NLD	0.723
ESP	0.532	NOR	0.905
FIN	0.817	SWE	0.761
FRA	0.073	USA	0.884
Whole Sample	0.258		

Notes: the null hypothesis that fc_{it}^{t+1} does not Granger-cause $\epsilon_{i,t}^{G}$ is rejected if p-value ≤ 0.05 at a 5% significance level.

We run a Granger-causality test. In particular, we test whether fiscal forecasts fc_{it}^{t+1} have any predictive power for the government spending shocks estimated from our benchmark model $z_{it} = [g_{it}, y_{it}, l_{it}, je_{it}, w_{C,it}]$. To implement the test of whether fc_{it}^{t+1} Granger-causes the VAR-based government spending shocks $\epsilon_{i,t}^{G}$, we run the following regression:

$$\epsilon_{i,t}^{G} = \alpha_i + \sum_{k=1}^{p} a_k \epsilon_{i,t-k}^{G} + \sum_{k=1}^{p} b_k fc_{i,t-k}^{t+1} + u_{i,t}, \tag{114}$$

where p is the autoregressive lag length and $u_{i,t}$ the error term. With respect to (114), in country i, the test of the null hypothesis that fc_{it}^{t+1} does not Granger cause $\epsilon_{i,t}^{G}$ is a F test of the form: $H_0 : b_1 = b_2 = \cdots = b_p = 0$. By not rejecting the null, one may conclude that VAR shocks $\epsilon_{i,t}^{G}$ are strictly exogenous to the dependent variable fc_{it}^{t+1}. Table 24 reports results.[70] The results for individual countries show that, with the exception of GBR, ITA and JPN, there is no causality running from fc_{it}^{t+1} to $\epsilon_{i,t}^{G}$ at the 5% level of significance suggesting that VAR shocks are not forecastable. For the whole sample, we find that forecasts for government spending fc_{it}^{t+1} do not Granger-cause the VAR shocks using the Cholesky decomposition to the benchmark specification $z_{it} = [g_{it}, y_{it}, l_{it}, je_{it}, w_{C,it}]$.

Following Born et al. [2013], we include the forecasts for real government spending growth within the VAR model (ordered after g_t). More specifically, we augment the four VAR specifications as follows:

- Estimating the magnitude of the aggregate fiscal multiplier: $z_{it} = \left[g_{it}, fc_{it}^{t+1}, y_{it}, l_{it}, je_{it}, w_{C,it}\right]$. In the second specification we replace private investment with the current account expressed in percentage of GDP, ca_{it}.

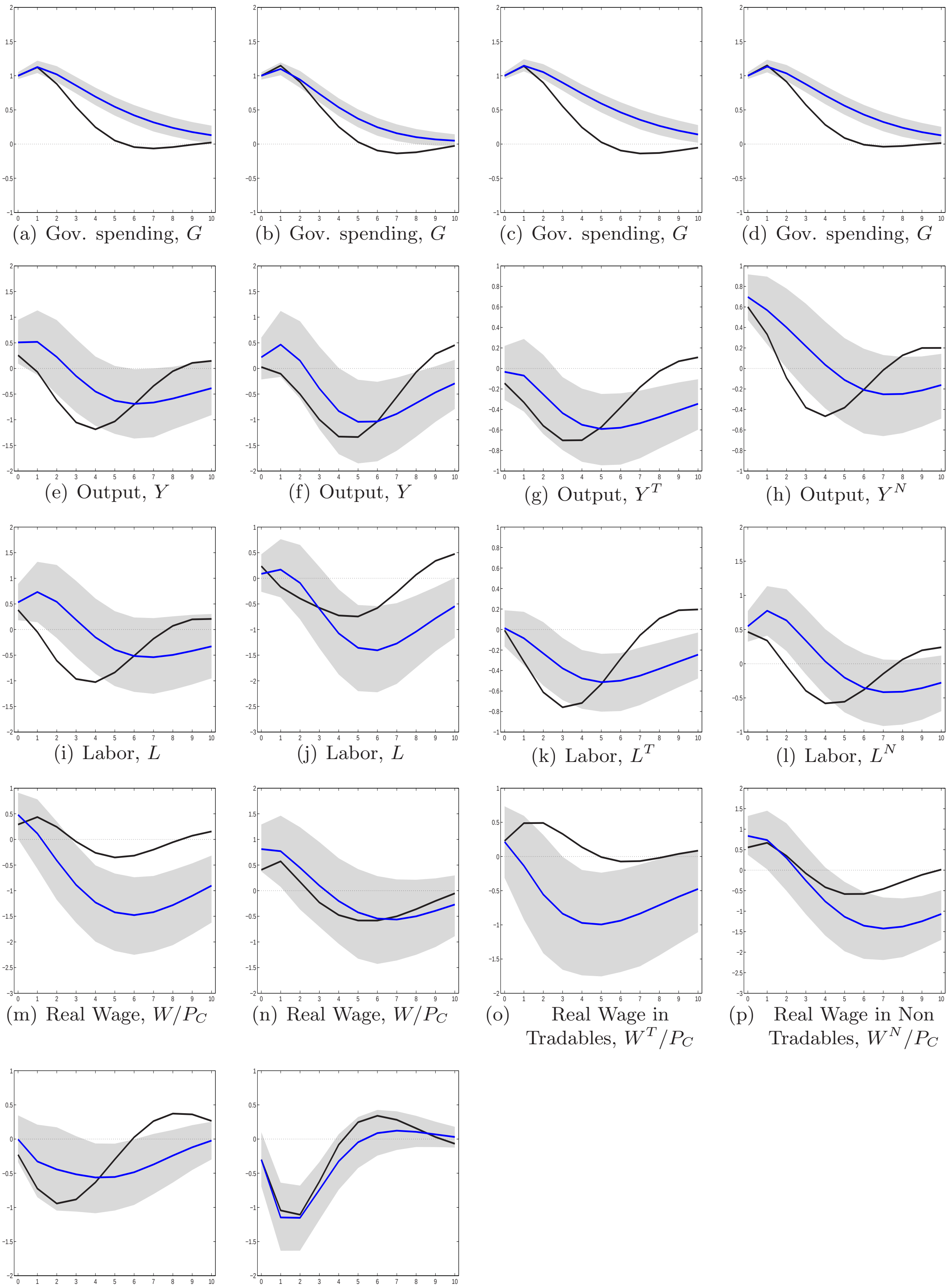
- Estimating the magnitude of the sectoral fiscal multiplier,: $z_{it}^{j} = \left[g_{it}, fc_{it}^{t+1}, y_{it}^{j}, l_{it}^{j}, w_{C,it}^{j}\right]$ with $j = T, N$.

- Estimating the change in relative sector size: $z_{it}^{S,j} = \left[g_{it}, fc_{it}^{t+1}, \nu_{it}^{Y,j}, \nu_{it}^{L,j}, w_{C,it}^{j}\right]$ with $j = T, N$.

- Estimating the relative price and relative wage effects: $z_{it}^{P} = \left[g_{it}, fc_{it}^{t+1}, y_{it}^{T} - y_{it}^{N}, p_{it}\right]$ and $z_{it}^{W} = \left[g_{it}, fc_{it}^{t+1}, l_{it}^{T} - l_{it}^{N}, \omega_{it}\right]$, respectively.

In order to make our evidence comparable with that without government spending forecasts, we estimate the four VAR specifications over the same period, i.e., from 1986 to 2007. Overall, Figures 37 and 38 show that all our results hold regardless of the period considered. We nevertheless may notice that real GDP, total hours worked and the real consumption wage increase less over the period 1986-2007 than over the period 1970-2007. Turning to sectoral variables, we find that the rise in non traded wages relative to traded

[70]Given the relatively short time horizon for the variable fc_{it}^{t+1}, regression (114) is estimated over the period 1997-2007. Therefore, we choose $p = 1$. Data limitation prevents the use of larger values for p.



(a) Gov. spending, G (b) Gov. spending, G (c) Gov. spending, G (d) Gov. spending, G

(e) Output, Y (f) Output, Y (g) Output, Y^T (h) Output, Y^N

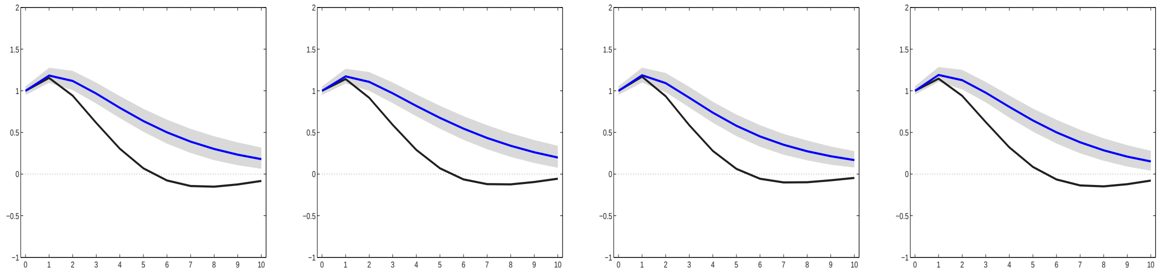
(i) Labor, L (j) Labor, L (k) Labor, L^T (l) Labor, L^N

(m) Real Wage, W/P_C (n) Real Wage, W/P_C (o) Real Wage in Tradables, W^T/P_C (p) Real Wage in Non Tradables, W^N/P_C

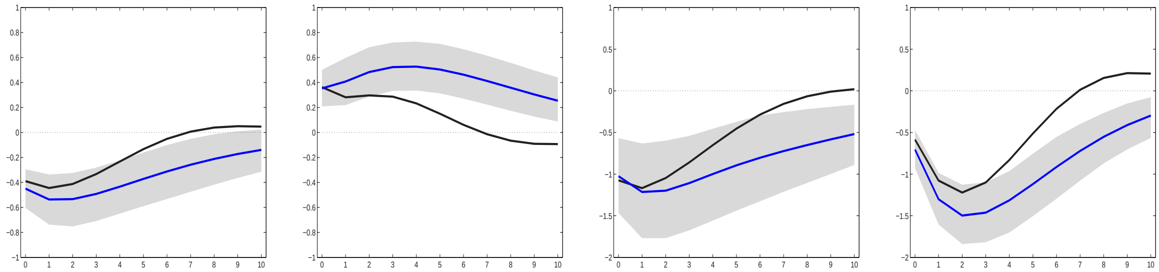
(q) Investment, JE (r) Current Account, CA

Figure 37: Aggregate and Sectoral Effects of an Unanticipated Government Spending Shock over 1986-2007. Notes: Exogenous increase in government consumption by 1% of GDP. Baseline sample: 16 OECD countries, 1970-2007; restricted sample: 17 OECD countries, 1986-2007. Results for baseline sample are displayed by solid blue lines with the shaded area indicating the 90 percent confidence bounds obtained by bootstrap sampling; the solid black line reports results for the restricted sample.

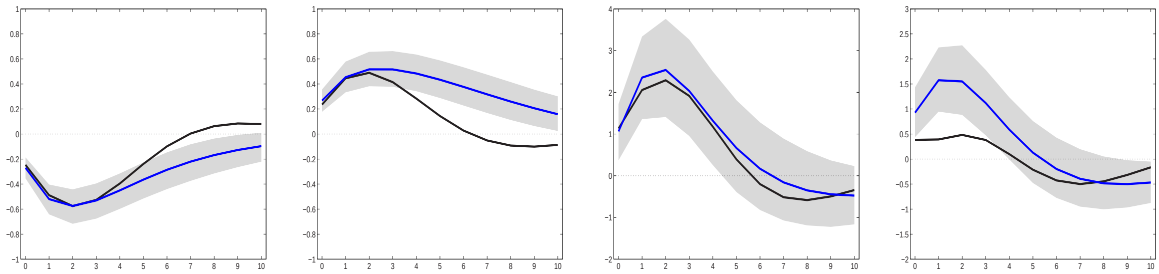
wages is slightly less pronounced than that over the baseline period 1970-2007. This result could suggest that workers' mobility costs have been reduced in 1986-2007 compared with those prevailing over 1970-1985.



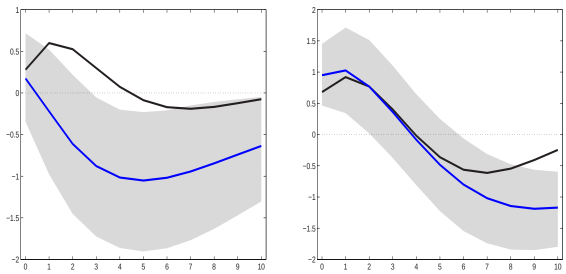
(a) Gov. spending, G (b) Gov. spending, G (c) Gov. spending, G (d) Gov. spending, G



(e) Output Share of Tradables, Y^T/Y (f) Output Share of Non Tradables, Y^N/Y (g) Relative Output, Y^T/Y^N (h) Relative Hours Worked, L^T/L^N



(i) Labor Share of Tradables, L^T/L (j) Labor Share of Non Tradables, L^N/L (k) Real Price of Non Tradables, P (l) Real Wage of Non Tradables, Ω



(m) Real Wage in Tradables, W^T/P_C (n) Real Wage in Non Tradables, W^N/P_C

Figure 38: Sectoral Composition Effects of an Unanticipated Government Spending Shock over 1986-2007. Notes: Exogenous increase in government consumption by 1% of GDP. Baseline sample: 16 OECD countries, 1970-2007; restricted sample: 17 OECD countries, 1986-2007. Results for baseline sample are displayed by solid blue lines with the shaded area indicating the 90 percent confidence bounds obtained by bootstrap sampling; the solid black line reports results for the restricted sample.

Figures 39 and 40 show IRF when augmenting each baseline VAR specification with forecasts for government spending. The solid blue line reports the results for the baseline case without forecasts for government spending growth, while the solid black line displays the results for the VAR model augmented with forecasts. In both cases, the VAR model is estimated over the period running from 1986 to 2007. Overall, it turns out that differences are rather moderate and anticipation effects thus play a limited quantitative role in the dynamic adjustment to a government spending shock. Yet, some differences can be noticed. Once anticipation effects are controlled for, the rise in hours worked displays more persistence and is more in line with what we obtained numerically. In this regard, this conclusion squares well with estimates documented by Born et al. [2013], except that the authors detect a smaller increase in real GDP when anticipation effects are not controlled for, while this finding applies to hours worked in our case as differences in the dynamic effects for real GDP are almost insignificant quantitatively. Likewise, impact responses of sectoral outputs are also very similar to impact effects computed numerically once the VAR model is augmented with forecasts for government spending. More specifically, the decline in empirically-estimated traded output is found to be more pronounced while the increase in non traded output is slightly smaller. We may also note that the reallocation effects are slightly greater as changes in sectoral shares in real GDP are somewhat more pronounced while the relative wage of non tradables increases less than in the baseline case. However, the responses of the sectoral shares in labor, L^j/L, are merely affected once the anticipation effects are controlled for.

As emphasized above, to ensure that our results are not subject to the fiscal foresight problem, we carry out a number of robustness exercises by augmenting the baseline VAR model with forward-looking variables along the lines of Beetsma and Giuliodori [2011], and Brückner and Pappa [2012]. Since one major contribution in this paper is to shed some light on the reallocation effects of a government spending shock, we restrict attention to the dynamic responses of sectoral shares. Columns 1 and 2 of Figure 41 show results when augmenting the baseline VAR model with the forecast for the budget balance-GDP ratio which we denote by bbr_t^{t+1}. The year-ahead forecasts are taken from the Commission's autumn forecasts, which are published in November.[71] In terms of VAR specifications shown above, we replace fc_t^{t+1} with bbr_t^{t+1}. It is worth mentioning that Beetsma and Giuliodori [2011] find empirically that the balance-ratio forecast has strong predictive power for g. Time series for the general government balance to GDP ratio forecast (one year ahead) are available for BEL (1971-2007), DNK (1977-2007), ESP (1987-2007), FRA (1970-2007), GBR (1974-2007), IRL (1974-2007), ITA (1970-2007), NLD (1970-2007). The impulse response functions shown in the solid black line, reported in columns 1-2 of Figure 41, are similar, if not identical, to those under the baseline shown in the solid blue line and thus do not deserve more comments. As an additional, and final, test we augment the baseline model with the log of nominal stock prices denoted by sp_t. In terms of VAR specifications, we replace fc_t^{t+1} with sp_t as this variable captures information about the future effects of fiscal shocks. Time series for stock prices are taken from OECD Main Economic Indicators. Data are available over 1970-2007 for AUS, AUT, CAN, FIN, FRA, GBR, IRL, ITA, JPN, NLD, SWE and USA, 1983-2007 for DNK, 1985-2007 for ESP and 1986-2007 for BEL and NOR. Again, the discrepancy in the estimated responses is quite moderate.

D.6 Government Spending Shock across VAR Specifications

An additional concern is related to the government spending shock which may vary across alternative VAR specifications. First, panel VAR evidence can be misleading if the spending shock significantly varies across VAR specifications which would make their interpretation difficult; for example, the sectors would not respond to the same shock and thus the comparison of sectoral output responses would become less relevant. In other words, while the responses are qualitatively the same, their magnitude might quantitatively be different with respect to an ideal configuration where we would have considered the same shock across all VAR specifications. Second, when we calibrate and simulate the model, we consider

[71] We thank Fioramanti et al. [2016] for providing this dataset to us.

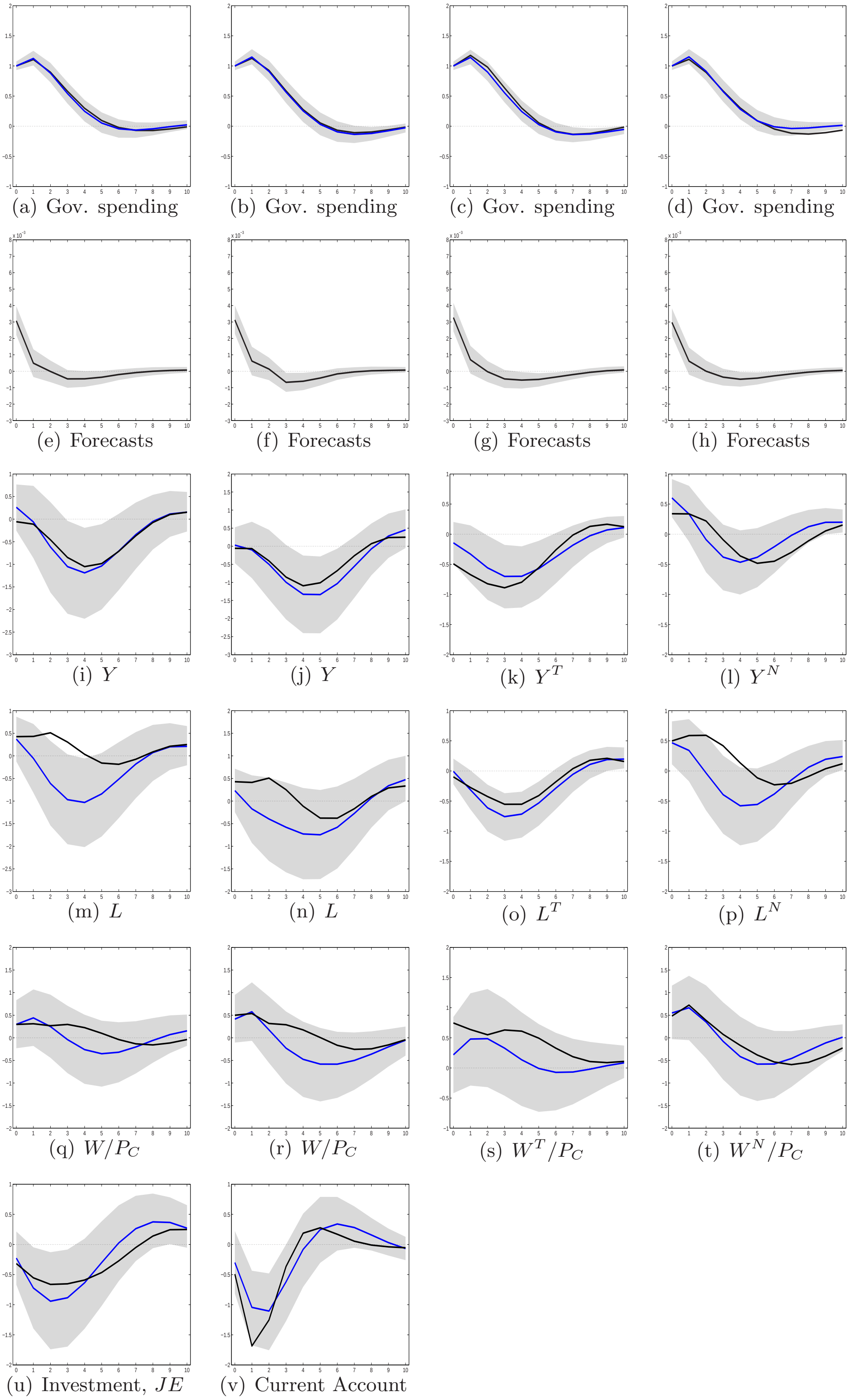


Figure 39: Aggregate and Sectoral Effects of an Unanticipated Government Spending Shock: Anticipation Effects. Notes: Exogenous increase in government consumption by 1% of GDP. Baseline sample: 16 OECD countries, 1986-2007. Solid blue line: Results for baseline case without controlling for anticipation effects; the shaded area indicates the 90 percent confidence bounds obtained by bootstrap sampling; the solid black line reports the results from estimates of VAR models with forecast of government spending growth (ordered after g_t).

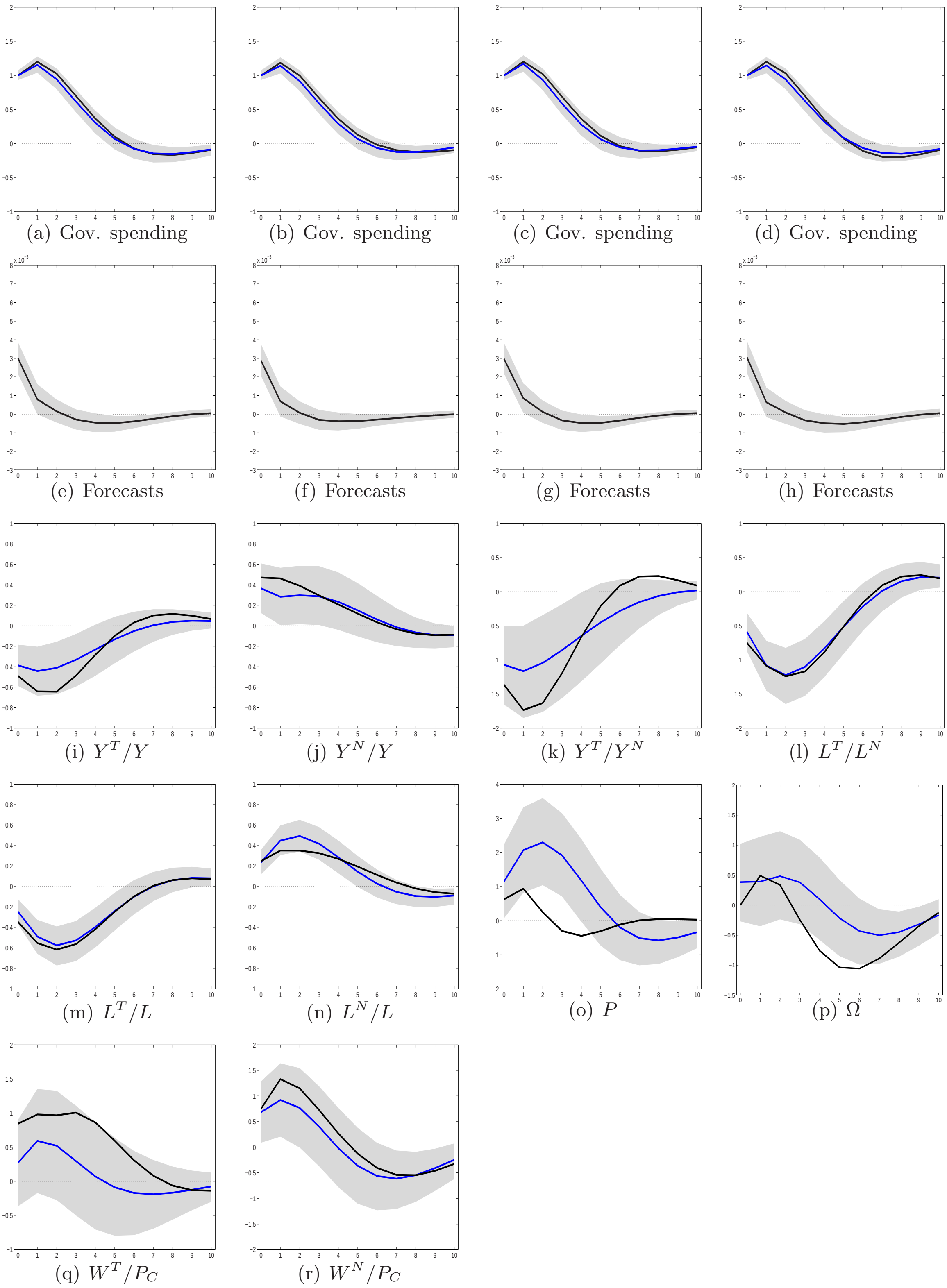


Figure 40: Sectoral Composition Effects of an Unanticipated Government Spending Shock: Anticipation Effects. Notes: Exogenous increase in government consumption by 1% of GDP. Baseline sample: 16 OECD countries, 1986-2007. Solid blue line: Results for baseline case without controlling for anticipation effects; the shaded area indicates the 90 percent confidence bounds obtained by bootstrap sampling; the solid black line reports the results from estimates of VAR models with forecast of government spending growth (ordered after g_t).

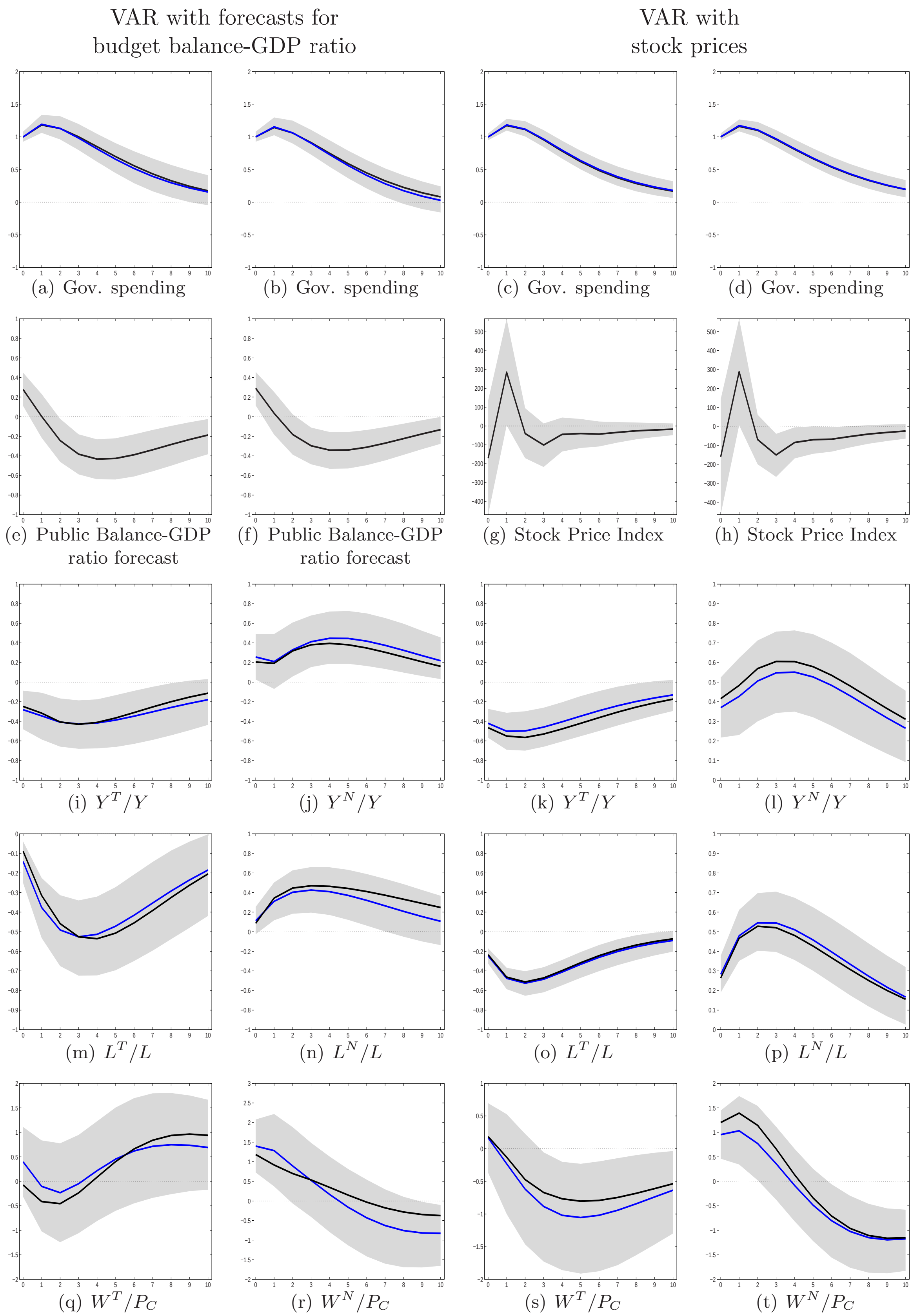


Figure 41: Sectoral Composition Effects of an Unanticipated Government Spending Shock: Alternative Forecasts Measures and Anticipation Effects. Notes: Exogenous increase in government consumption by 1% of GDP. Baseline sample: 8 OECD countries (first two columns) and 16 OECD countries (last two columns), 1970-2007. Solid blue line: Results for the baseline case without controlling for anticipation effects; the shaded area indicates the 90 percent confidence bounds obtained by bootstrap sampling; the solid black line reports the results from estimates of VAR models with balance-ratio forecast (first two columns) or stock prices (last two columns).

Table 25: Correlation Matrix between Structural Government Spending Shocks across VAR models

VAR models	Correlations							
	1-VAR	2-VAR	3-VAR	4-VAR	5-VAR	6-VAR	7-VAR	8-VAR
1-$z_{it} = [g_{it}, y_{it}, l_{it}, je_{it}, w_{C,it}]$	1.000							
2-$z_{it} = [g_{it}, y_{it}, l_{it}, ca_{it}, w_{C,it}]$	0.976	1.000						
3-$z^j_{it} = [g_{it}, y^T_{it}, l^T_{it}, w^T_{C,it}]$	0.989	0.968	1.000					
4-$z^j_{it} = [g_{it}, y^N_{it}, l^N_{it}, w^N_{C,it}]$	0.986	0.970	0.978	1.000				
5-$z^{S,T}_{it} = [g_{it}, \nu^{Y,T}_{it}, \nu^{L,T}_{it}, w^T_{C,it}]$	0.951	0.938	0.970	0.954	1.000			
6-$z^{S,N}_{it} = [g_{it}, \nu^{Y,N}_{it}, \nu^{L,N}_{it}, w^N_{C,it}]$	0.956	0.944	0.975	0.958	0.996	1.000		
7-$z^P_{it} = [g_{it}, y^T_{it} - y^N_{it}, p_{it}]$	0.958	0.948	0.974	0.955	0.982	0.982	1.000	
8-$z^W_{it} = [g_{it}, l^T_{it} - l^N_{it}, \omega_{it}]$	0.947	0.935	0.967	0.954	0.995	0.994	0.979	1.000

Notes: The first column shows that VAR model while column 2 through 9 shows the correlation between structural government spending shocks across VAR models.

the same government spending shock to compute the dynamic responses of aggregate and sectoral variables. Thus, the comparison of theoretical and empirical impulse response functions can be misleading as well. In this subsection, we assess the legitimacy of investigating aggregate and sectoral effects by identifying government spending shocks on the basis of alternative VAR specifications. A first and simple check of the discrepancy between estimated structural government spending shocks across the VAR models can be performed by estimating the correlation between structural government spending shocks. The first column of Table 25 is the most interesting as it shows the correlation between structural government spending shocks whose identification is based on the first VAR model and those identified on the basis of alternative VAR models. The correlation varies from a low of 0.947 for the VAR model z^W_{it} that includes the relative wage of non tradables to a high of 0.986 and 0.989 for the VAR model z^j_{it} that includes sectoral output. Overall, given the high value of correlation between structural government spending shocks across VAR models, one may reasonably expect the discrepancy in the estimated responses caused by slight differences in estimated structural government spending shocks to be small.

Before investigating the extent of the discrepancy in the estimated government spending shock across VAR specifications, we find it useful to begin with a quick refresher on the computation of IRF. For convenience, we repeat the structural VAR model which can be written (abstracting from the constant term) as:

$$AZ_{i,t} = \sum_{k=1}^{p} B_k Z_{i,t-k} + \epsilon_{i,t}. \tag{115}$$

In order to uniquely recover the structural form, we have to impose assumptions on matrix A. Following Blanchard and Perotti [2002], we assume that government consumption does not react on impact to other shocks in the system. We thus adopt a Cholesky decomposition in which government spending is ordered before the other variables. Technically, matrix A is thus lower-triangular. Once the restriction is imposed and A has been recovered, the structural form (115) can be written as follows:

$$Z_{i,t} = \sum_{k=1}^{p} A^{-1} B_k Z_{i,t-k} + A^{-1}\epsilon_{i,t}. \tag{116}$$

To avoid unnecessary complications, let us assume one lag so that $p = 1$. Iterating (116) backward leads to:

$$Z_{i,t} = \sum_{h=0}^{H} B_1^h A^{-1} \epsilon_{i,t-h} \tag{117}$$

Setting $\phi_h = B_1^h A^{-1}$ with elements $\phi_{lm}(h)$, the vector moving average representation of the reduced VAR form (116) now reads:

$$Z_{i,t} = \sum_{h=0}^{H} \phi_h \epsilon_{i,t-h}. \tag{118}$$

Letting $e_{i,t}$ be the vector of residuals in the reduced form, we have $e_{i,t} = A^{-1}\epsilon_{i,t}$ and $\epsilon_{1,i,t}$ is the structural government spending shock. VAR model can be estimated in its reduced form by using OLS. OLS provide estimates of elements of $A^{-1}B_1$ along with the variance-covariance matrix which allows the computation of impulse response functions. Since estimates should depend on the VAR specification, the structural government spending shock should be different across VAR specifications. However, this potential problem is mitigated as we normalize the spending shock across all VAR specifications to a rise in government spending by one percentage point of GDP. Such a normalization thus makes impact responses of economic variables directly comparable quantitatively across VAR models. In this regard, as we base the greatest part of our analysis and discussion of fiscal transmission on impact effects, potential problems caused by differences in shape and the magnitude of the fiscal shock could be mitigated. However, even if the magnitude and the shape of the government spending shock is similar across VAR specifications, different VAR models could pickup different structural government spending shocks. Moreover, the endogenous response of government spending to an exogenous fiscal shock normalized to 1% of GDP may vary across VAR specifications while in the quantitative analysis, we compute the theoretical impulse response functions by considering the same exogenous dynamic adjustment of government spending. In order to investigate the extent of the discrepancy in the estimated responses caused by potentially different government spending shocks across VAR specifications, we proceed in four stages:

- First, we compare endogenous responses of government spending across all VAR specification in Figure 42. The shaded area corresponds to the 90% confidence bound for the original VAR specification $z_{it} = [g_{it}, y_{it}, l_{it}, je_{it}, w_{C,it}]$. Then we test whether the point estimate for the response of government spending in the first VAR model is significantly different from the point estimate for other VAR models.

- Second, once we identified the government spending shock in the first VAR model that includes private investment, $z_{it} = [g_{it}, y_{it}, l_{it}, je_{it}, w_{C,it}]$, we augment each VAR model with the identified government spending shocks, ordered first, and use shocks to government spending (identified with the Cholesky decomposition) as the fiscal shock, see e.g., Ramey [2011] who adopts a similar procedure to identify military spending shocks. Then, we contrast the responses for the baseline model with those for augmented VAR models.

- Third, we identify the government spending shock by estimating the first VAR model that includes private investment, i.e., $z_{it} = [g_{it}, y_{it}, l_{it}, je_{it}, w_{C,it}]$ by using quarterly data, and we annualize the estimated shock. Then, we estimate each VAR model augmented with the same annualized identified government spending shock on annual data. Quarterly data are taken from the OECD Economic Outlook database. We apply our method for the largest available subset of the countries in our current sample for which we have sufficient quarterly fiscal data. The sample includes AUS, CAN, FRA, JPN, NLD, SWE, GBR and USA, for which quarterly and annual macroeconomic data are available: AUS (1979Q1-2007Q4), CAN (1981Q1-2007Q4), FRA (1973Q1-2007Q4), JPN (1970Q1-2007Q4), NLD (1970Q1-2007Q4), SWE (1975Q1-2007Q4), GBR (1972Q1-2007Q4) and USA (1970Q1-2007Q4).[72] We provide more details below about the data used in this analysis:

[72] Lack of data and/or short time period prevent the inclusion of others countries in the sample. In details: AUT (no data for investment), BEL (no data for government spending, output and the real wage), DNK (no data for the real wage), ESP (no data for investment and the real wage), FIN (no data for hours worked), IRL (no data for investment and quarterly series for government spending and output start in 1990Q1), ITA (no data for investment) and NOR (no data for hours worked and the real wage).

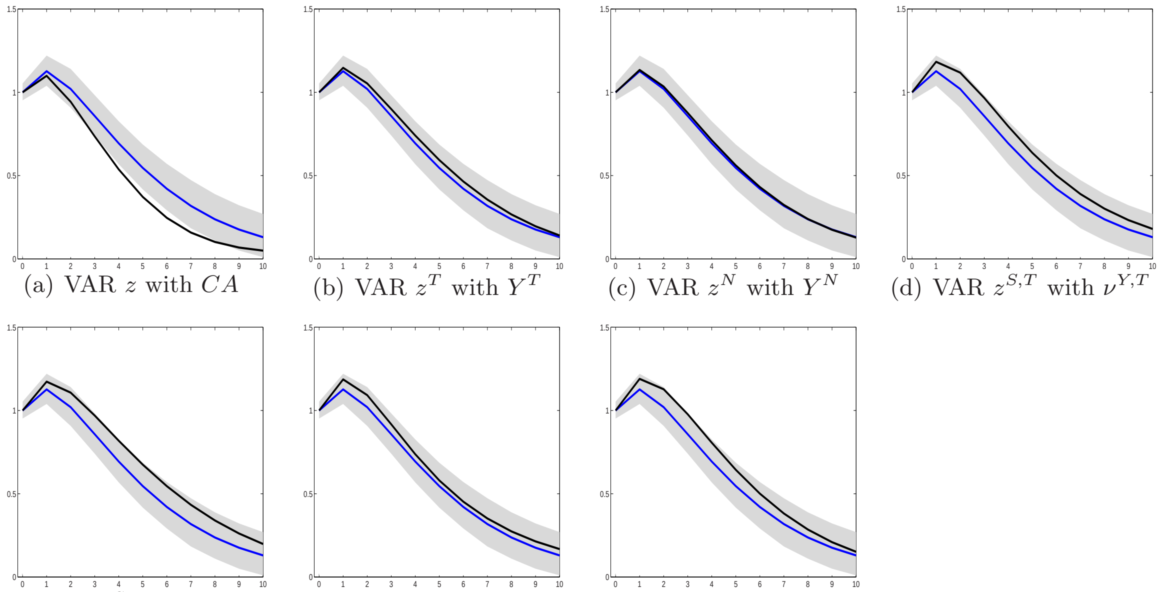
  - **Government spending**: real government final consumption expenditure (CGV). Source: OECD Economic Outlook Database.
  - **Gross domestic product**: real gross domestic product (GDPV). Source: OECD Economic Outlook Database.
  - **Labor**: hours worked per employee, total economy. Source: OECD Economic Outlook Database.
  - **Private investment**: real private non-residential gross fixed capital formation (IBV). Source: OECD Economic Outlook Database.
  - **Real wage**: nominal wage rate (total economy) divided by the consumer price index (CPI). Sources: OECD Economic Outlook Database for the nominal wage and OECD Prices and Purchasing Power Parities for the consumer price index.

  All data are seasonally adjusted and, except for the real wage, are divided by the population. To obtain variables in per capita terms we use the working age population (15-64 years old) provided by OECD Economic Outlook Database (data for the population at quarterly frequency were interpolated from annual data). For government spending, GDP and investment, we directly use the volumes as reported by the OECD (the series are deflated with their own deflators).

- Fourth, instead of taking the identified government spending shock from the estimation of the first VAR model as the baseline spending shock, we allow the government spending shock to vary in the quantitative analysis. More specifically, we compute numerically the responses of variables by calibrating the model so as to replicate the endogenous response of government spending obtained in each VAR specification. In other words, we compute the dynamic responses of economic variables to the government spending shock corresponding to the same VAR model in which this variable is included.

Figure 42 compares the dynamic response of government consumption to an exogenous fiscal shock for the first VAR model with the endogenous response of G for alternative VAR models. The solid blue line reports the point estimates for the first VAR model while the solid black line in each panel reports the point estimates for an alternative VAR model. The evidence is very clear: all responses of government spending are fairly close to the one based on the benchmark classification and remain within the confidence interval of the baseline for all of the selected horizons (10 years). We can notice only one slight difference for the specification $z_{it} = [g_{it}, y_{it}, l_{it}, ca_{it}, w_{C,it}]$. When we calculate the correlations between the IRF on government spending from the original VAR specification and the ones obtained from others VAR specifications, we find a strong homogeneity in the estimated value of the correlation coefficient, which varies from a low of 0.992 for the specification $z_{it} = [g_{it}, y_{it}, l_{it}, ca_{it}, w_{C,it}]$ to a high of 0.999 for the specification $z_{it}^N = \left[g_{it}, y_{it}^N, l_{it}^N, w_{C,it}^N\right]$, with a mean value (across specifications) of 0.997. To further explore empirically the discrepancy between government spending shocks across VAR specifications, Table 26 reports the test (p-value) of the statistical significance of the difference between the point estimate for the baseline model $z_{it} = [g_{it}, y_{it}, l_{it}, je_{it}, w_{C,it}]$ and that for an alternative VAR specification for each horizon $k = 1 \ldots 10$. As can be seen in Table 26, we fail to detect a significant difference in the responses of government spending for all horizons. Overall, the assumption that the government spending shock is similar across VAR specifications appears to be reasonable.

Figures 43 and 44 compare the results in the main text displayed in the solid blue line with those for the same VAR model augmented with the identified government spending shock in the first VAR model estimated on annual data. As shown in the first row of Figures 43 and 44, across all VAR specifications, the endogenous response of government spending is quite similar, if not identical, whether the fiscal shock is identified in the first VAR model (solid black line) or is identified in the corresponding VAR model (solid blue line). The dynamic effects displayed in Figure 43 do not deserve comments as impulse response functions are very similar. Turning to the sectoral composition effects displayed in Figure 44, while we may notice some slight differences for the responses of sectoral shares,



(a) VAR z with CA (b) VAR z^T with Y^T (c) VAR z^N with Y^N (d) VAR $z^{S,T}$ with $\nu^{Y,T}$

(e) VAR $z^{S,N}$ with $\nu^{Y,N}$ (f) VAR z^P with P (g) VAR z^W with Ω

Figure 42: Effects of an Unanticipated Fiscal Shock on Government Spending. Notes: Exogenous increase in government consumption by 1% of GDP. Blue line: baseline VAR model $z_{it} = [g_{it}, y_{it}, l_{it}, je_{it}, w_{C,it}]$; shaded areas: 90 percent confidence intervals; black line: alternative VAR specifications.

Table 26: Testing Differences Between Point Estimates of Government Spending for the First and Alternative VAR Models (p-values)

VAR Specification	Time Horizon									
	1	2	3	4	5	6	7	8	9	10
$z_{it} = [g_{it}, y_{it}, l_{it}, ca_{it}, w_{C,it}]$	0.887	0.791	0.716	0.667	0.643	0.641	0.659	0.693	0.738	0.787
$z_{it}^j = [g_{it}, y_{it}^T, l_{it}^T, w_{C,it}^T]$	0.912	0.902	0.893	0.892	0.897	0.907	0.920	0.937	0.955	0.974
$z_{it}^j = [g_{it}, y_{it}^N, l_{it}^N, w_{C,it}^N]$	0.966	0.957	0.950	0.952	0.961	0.973	0.985	0.997	0.995	0.990
$z_{it}^{S,T} = [g_{it}, \nu_{it}^{Y,T}, \nu_{it}^{L,T}, w_{C,it}^T]$	0.777	0.746	0.756	0.781	0.806	0.827	0.843	0.856	0.868	0.880
$z_{it}^{S,N} = [g_{it}, \nu_{it}^{Y,N}, \nu_{it}^{L,N}, w_{C,it}^N]$	0.804	0.767	0.753	0.754	0.763	0.776	0.793	0.814	0.838	0.865
$z_{it}^P = [g_{it}, y_{it}^T - y_{it}^N, p_{it}]$	0.754	0.812	0.872	0.918	0.940	0.945	0.938	0.928	0.918	0.913
$z_{it}^W = [g_{it} l_{it}^T - l_{it}^N, \omega_{it}]$	0.753	0.721	0.721	0.749	0.792	0.837	0.876	0.910	0.938	0.962

Notes: Each entry gives the p-value associated with the equality test between the point estimate of G at horizon k for the first VAR model, i.e., $z_{it} = [g_{it}, y_{it}, l_{it}, je_{it}, w_{C,it}]$ and alternative VAR models shown in the first column. The null hypothesis is rejected if p-value ≤ 0.05 at a 5% significance level. The differences and their standard errors are computed as follows. First, we take the point estimates of the mean responses of G in all specifications at each time horizon. Second, we compute the differences between the mean response of G for the baseline $z_{it} = [g_{it}, y_{it}, l_{it}, je_{it}, w_{C,it}]$ and the mean response of G obtained for alternative VAR specifications. Then, we test the statistical significance of these differences using the replications produced by the bootstrap sampling used to determine confidence bounds.

the real consumption wage in non tradables, and the relative wage of non tradables, the discrepancy is not statistically significant, except for the relative wage in the short-run. Overall, reassuringly, this robustness exercise shows that the government spending shock is very similar across VAR specifications and it turns out that differences are quantitatively rather moderate.

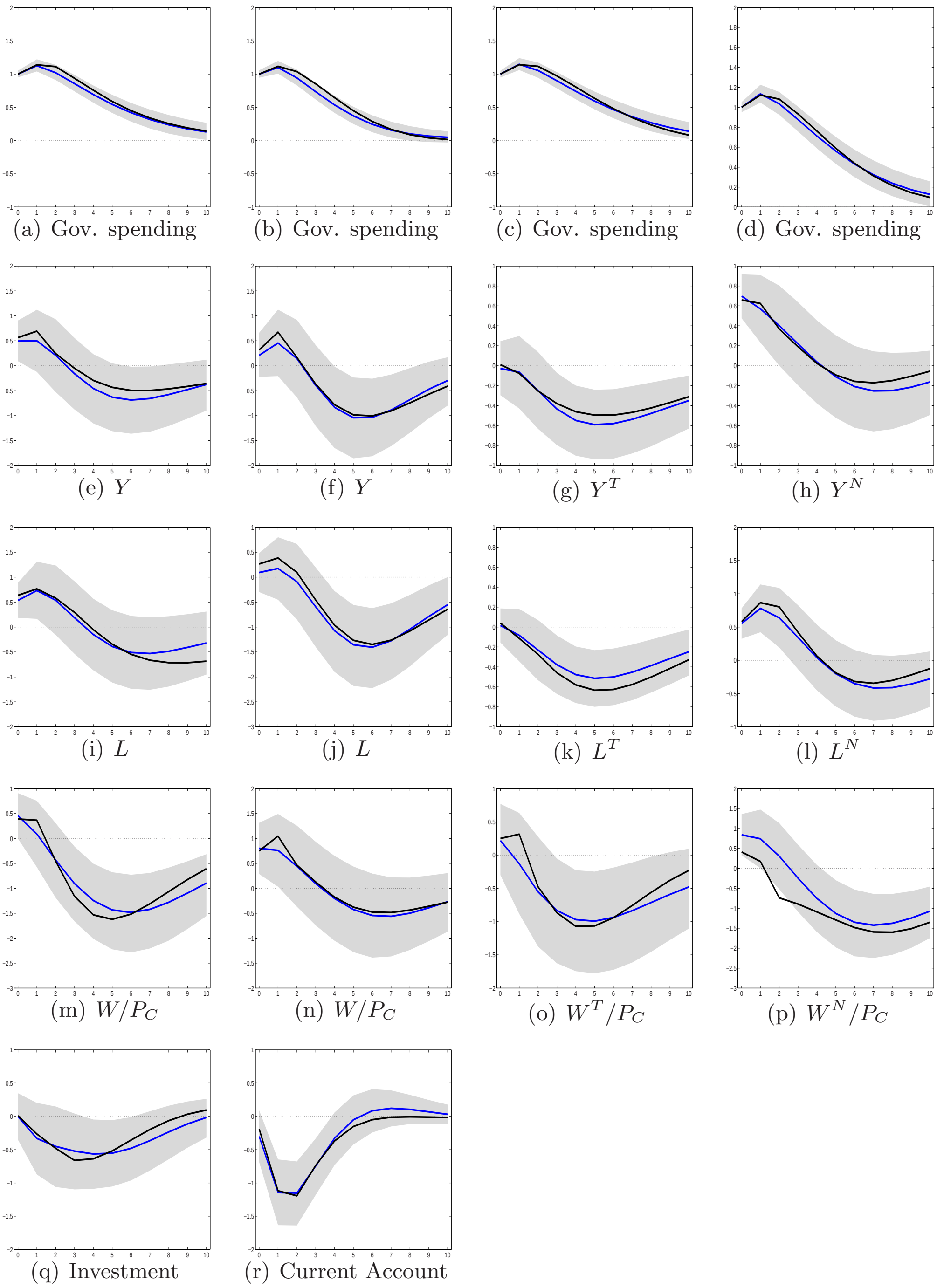
The identification scheme proposed by Blanchard and Perotti [2002] is based on the assumption that government spending does not respond contemporaneously to current output developments due to delays between current output observation and the implementation of fiscal measures. The potential problem is that Blanchard and Perotti's argument is not necessarily true when using annual data as some adjustment could be possible within the year. We use quarterly data and assume that government spending does not respond within the quarter to the other variables included in the VAR model. This assumption is in the spirit of Blanchard and Perotti [2002]. We take the identified government spending shock in the first VAR model as the baseline spending shock. Then we augment each VAR model with the baseline spending shock identified on a quarterly basis. Such a procedure should ensure that the fiscal shock is exogenous and variables respond to the same identified government spending shock. The disadvantage is that the largest available subset of the countries in our current sample for which we have sufficient quarterly fiscal data is 8 instead of 16. In order to make our baseline results comparable with those when we augment each VAR model with the spending shock identified in the first VAR model, i.e. $z_{it} = [g_{it}, y_{it}, l_{it}, je_{it}, w_{C,it}]$, we re-estimate each VAR model on annual data for the set of countries restricted to eight. In the latter case, we do not augment VAR models with the identified government spending shock in the first VAR model. The solid blue line in Figures 45 and 46 displays the baseline results for a government spending shock identified on annual data, while the solid black line displays the results when each VAR model is augmented with government spending shock identified in the first VAR model on quarterly data. As shown in the first row of Figures 45 and 46, the response of government spending to the exogenous fiscal shock identified on quarterly data displayed in the solid black line is somewhat more pronounced in the short term and the IRF of G remains above that in the baseline. In sum, the government spending shock displays more persistence and is somewhat more pronounced when identified on quarterly data. Because the government spending shock is larger in this configuration, as can be seen in Figure 45, hours worked and output fall more in the traded sector while they increase more in the non traded sector. It is thus not surprising that the responses of sectoral shares are more pronounced, as can be seen in Figure 46. Regarding the responses for the relative price and the relative wage, differences are quantitatively rather moderate.

In the last robustness exercise we perform, we normalize the exogenous fiscal shock to a rise in G by 1 percentage point of GDP in the quantitative analysis but let the endogenous response of government consumption vary across VAR specifications. Thus, when we compute the theoretical impulse response functions of one variable, we calibrate the government spending shock so as to reproduce the endogenous response of G we generate from estimates of the VAR model in which the variable is included. The objective of this exercise is to compute quantitatively the discrepancy in the estimated response of each variable caused by an identified government spending shock that potentially varies across VAR models while in the baseline quantitative analysis, we consider one unique spending shock identified in the first VAR model $z_{it} = [g_{it}, y_{it}, l_{it}, je_{it}, w_{C,it}]$. In the first row of Figures 47 and 48, the solid blue line displays the adjustment of government spending we generate from estimates of the first VAR model $z_{it} = [g_{it}, y_{it}, l_{it}, je_{it}, w_{C,it}]$ while the solid red line displays the endogenous response of G we generate from estimates of the VAR model in which the variable shown in the second row is included.

As discussed above, the differences between the government spending shock identified in the first VAR model and the government spending shock identified in alternative VAR models are quite moderate, and in most of the cases insignificant, except for the specification that includes the current account shown the first column of Figure 47. The solid blue line in the second row of Figures 47 and 48 shows empirical impulse response functions, while the solid black line displays theoretical responses when the government spending shock is calibrated on the basis of the first VAR model. The dotted black line displays the theoretical responses when the government spending shock is identified in the VAR model in which the economic variable (shown in the second row) is included. Overall, the differences between the solid and the dotted black line are quantitatively small or hardly noticeable for all variables. Thus, our quantitative analysis should not be altered by the small differences in the government spending shock across VAR specifications.

D.7 Exogeneity of Government Spending Shocks and the Narrative Approach

Following Blanchard and Perotti [2002], we have based identification on the assumption that government spending does not react contemporaneously to other variables included in the VAR model. Since there are some delays inherent to the legislative system, this is a natural assumption when using quarterly data. However, this argument may not be necessarily true when using annual data since some adjustment could be possible. We thus conduct in this subsection a robustness check by using narratively identified government



(a) Gov. spending (b) Gov. spending (c) Gov. spending (d) Gov. spending

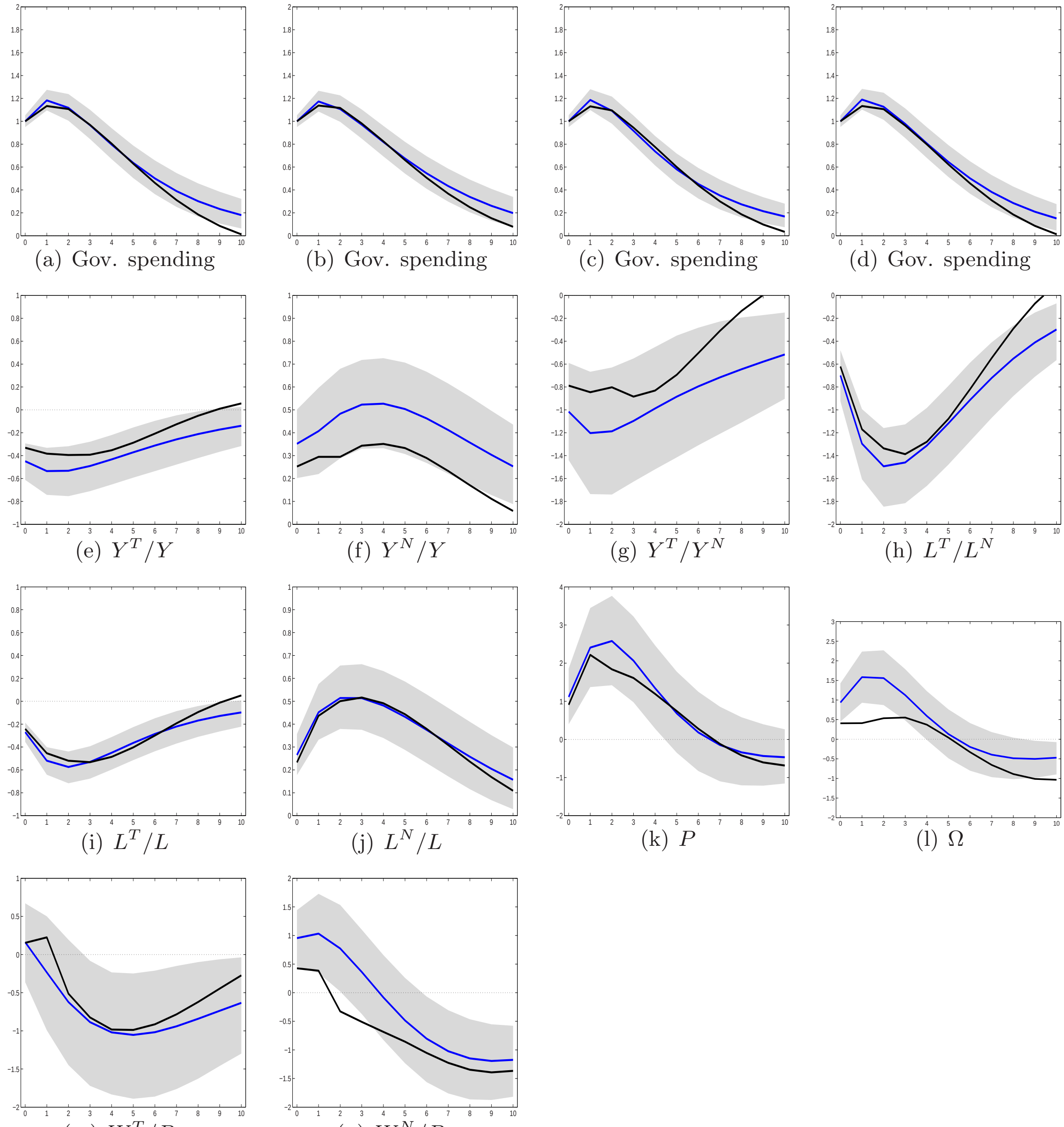
(e) Y (f) Y (g) Y^T (h) Y^N

(i) L (j) L (k) L^T (l) L^N

(m) W/P_C (n) W/P_C (o) W^T/P_C (p) W^N/P_C

(q) Investment (r) Current Account

Figure 43: Aggregate and Sectoral Effects of an Unanticipated Government Spending Shock: Assessing Differences Caused by Identifying Different Government Spending Shocks on Annual Data. Notes: Exogenous increase in government consumption by 1% of GDP. Results for the baseline specification are displayed by solid lines with the shaded area indicating the 90 percent confidence bounds obtained by bootstrap sampling; the solid black line reports the results for the same VAR model which is augmented with the identified government spending shock in the first VAR model estimated on annual data; sample: 16 OECD countries, 1970-2007, annual data.



(a) Gov. spending (b) Gov. spending (c) Gov. spending (d) Gov. spending

(e) Y^T/Y (f) Y^N/Y (g) Y^T/Y^N (h) L^T/L^N

(i) L^T/L (j) L^N/L (k) P (l) Ω

(m) W^T/P_C (n) W^N/P_C

Figure 44: Sectoral Composition Effects of an Unanticipated Government Spending Shock: Assessing Differences Caused by Identifying Different Government Spending Shocks on Annual Data. Notes: Exogenous increase in government consumption by 1% of GDP. Results for the baseline specification are displayed by solid lines with the shaded area indicating the 90 percent confidence bounds obtained by bootstrap sampling; the solid black line reports the results for the same VAR model which is augmented with the identified government spending shock in the first VAR model estimated on annual data; sample: 16 OECD countries, 1970-2007, annual data.

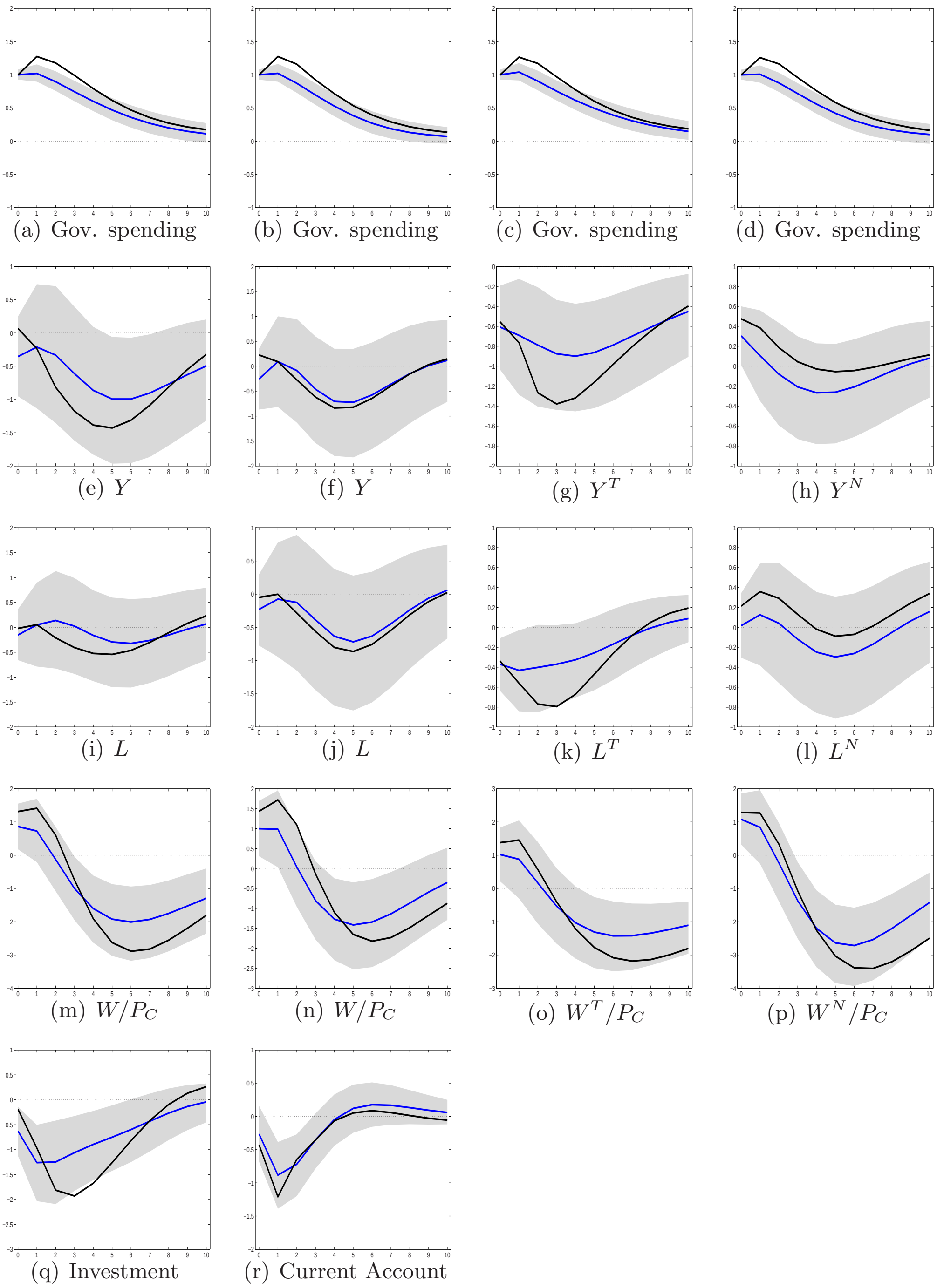


Figure 45: Aggregate and Sectoral Effects of an Unanticipated Government Spending Shock: Assessing Differences Caused by Identifying Different Government Spending Shocks. Notes: Exogenous increase in government consumption by 1% of GDP. Results for the baseline specification are displayed by solid lines with the shaded area indicating the 90 percent confidence bounds obtained by bootstrap sampling; the solid black line reports the results for the same VAR model which is augmented with the identified government spending shock in the first VAR model estimated on quarterly data; sample: 8 OECD countries, 1970-2007, annual data.

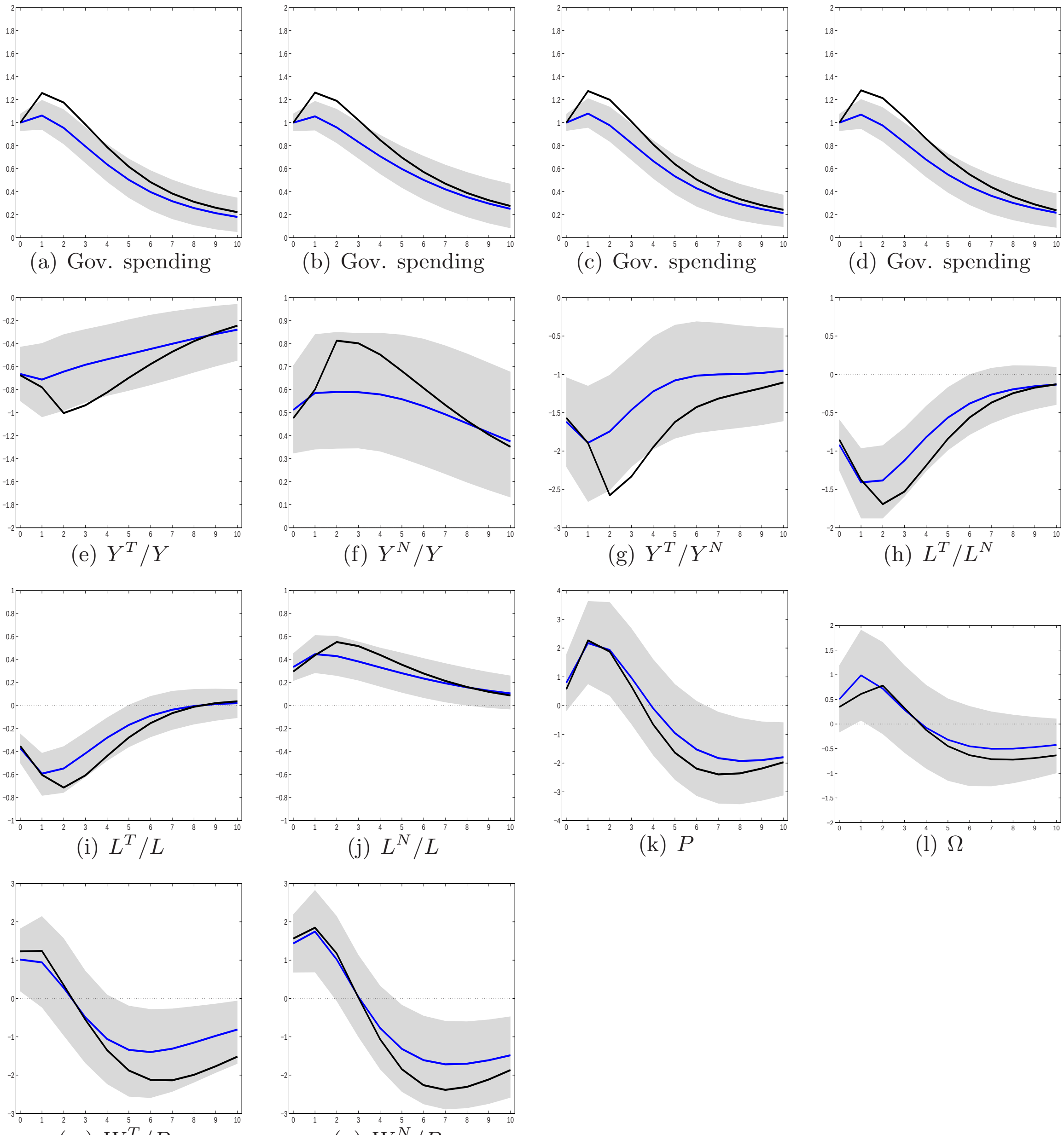
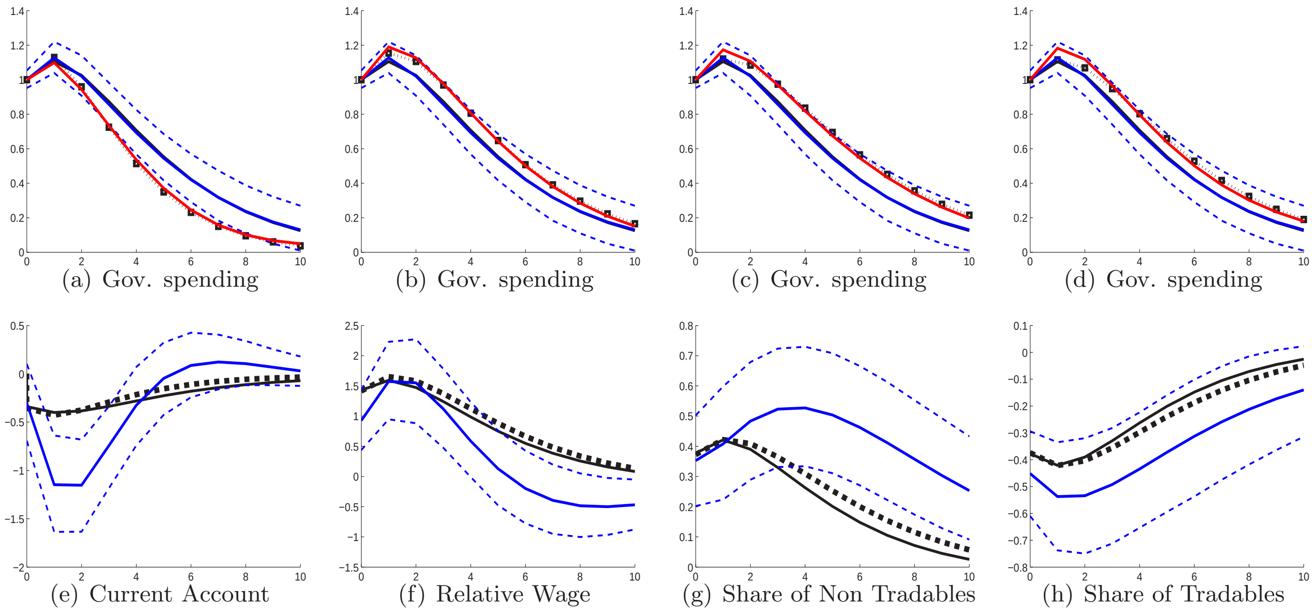


Figure 46: Sectoral Composition Effects of an Unanticipated Government Spending Shock: Assessing Differences Caused by Identifying Different Government Spending Shocks. Notes: Exogenous increase in government consumption by 1% of GDP. Results for the baseline specification are displayed by solid lines with the shaded area indicating the 90 percent confidence bounds obtained by bootstrap sampling; the solid black line reports the results for the same VAR model which is augmented with the identified government spending shock in the first VAR model estimated on quarterly data; sample: 8 OECD countries, 1970-2007, annual data.



(a) Gov. spending (b) Gov. spending (c) Gov. spending (d) Gov. spending

(e) Current Account (f) Relative Wage (g) Share of Non Tradables (h) Share of Tradables

Figure 47: Contrasting Theoretical Impulse Response Functions for Potentially Varying Government Spending Shock. Notes: Impulse response functions to an exogenous increase in real government spending by one percent of GDP. The solid blue line displays the point estimate of VAR with the dotted blue lines indicating 90% confidence bounds; the solid black line displays model predictions in the baseline scenario, i.e., when we calibrate the model on the basis of the first VAR model, $z_{it} = [g_{it}, y_{it}, l_{it}, je_{it}, w_{C,it}]$; the dotted black line displays model predictions when we calibrate the model for a government spending shock specific to the VAR specification. In the first row, the red line and the dotted black line with squares display the empirical and theoretical response of government spending specific to the VAR specification, respectively.

spending shocks from the dataset constructed by Guajardo, Leigh, and Pescatori [2014].

Before discussing the results from the narrative approach, it is worth mentioning that we conducted alternative robustness checks. In subsection B.4, following Beetsma and Giuliodori [2011], for the largest available subset of the countries in our current sample, we estimate the same VAR model on a quarterly basis, assuming that government purchases take at least one quarter to react to an output shock. We find that the dynamic responses of government spending along with the remaining aggregate variables included in the VAR model are similar to those when estimating the same VAR model on annual data. To deal further with the potential endogeneity problem, like Beetsma and Giuliodori [2011] and Brückner and Pappa [2012], we also order government purchases last in the VAR model and thus alow for G to respond to all variables included in the VAR model. If the endogenous response of G to an exogenous fiscal shock is similar to that when the VAR is estimated by ordering G first, then we can be confident that the endogenity problem is mitigated as G is not or at least little responsive to output shocks. As displayed in Figure 49, the endogenous response of G lies within the confidence bounds of the primary VAR model where G is ordered first across all VAR specifications. This finding could be explained by the fact that automatic stabilizers which operate through unemployment benefits or transfers should not pose a problem since we consider government spending net of transfers.

Finally, Born and Müller [2012] test whether annual government spending is predetermined conditional on being predetermined at the quarterly frequency for four countries, i.e., United States, United Kingdom, Canada, and Australia. Their main result is that the restriction that government spending does not respond to other variables in the VAR within a year cannot be rejected. That being said, an alternative estimation strategy is suggested by Ramey and Shapiro [1998]. Their narrative approach amounts to considering major political events which led to large military buildups associated with significant increases in government spending. The advantage of the narrative approach over alternatives

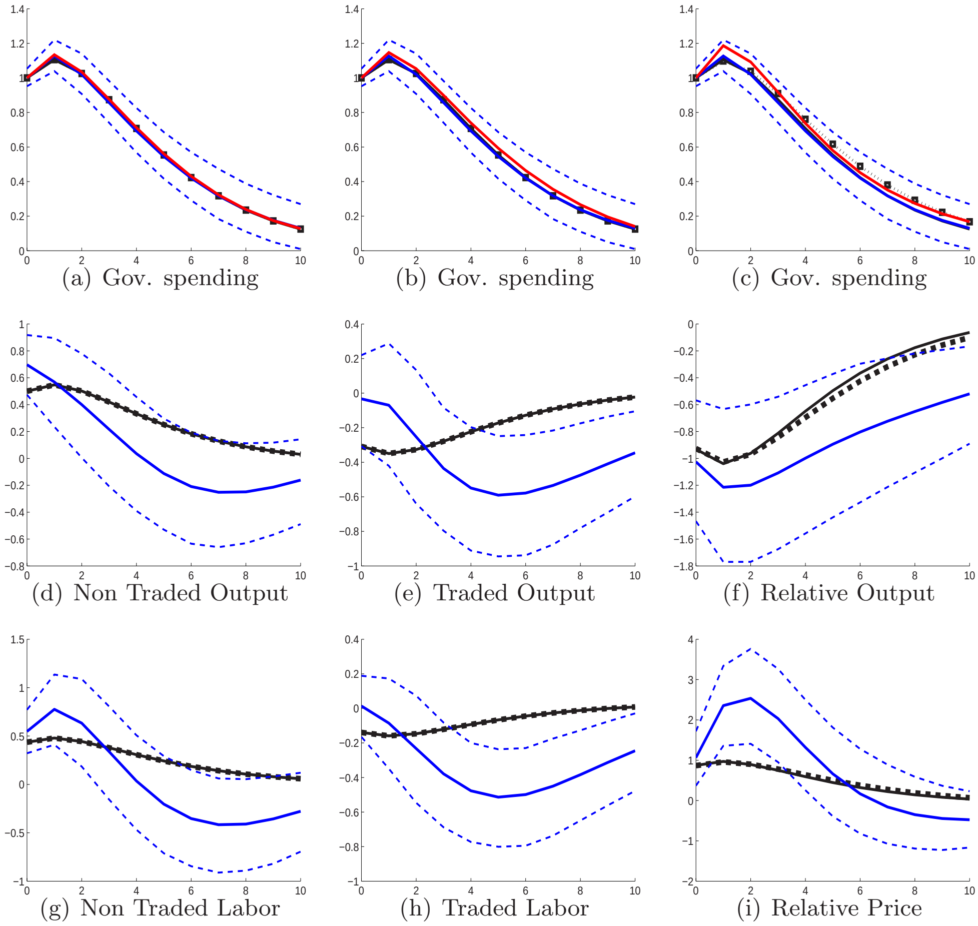
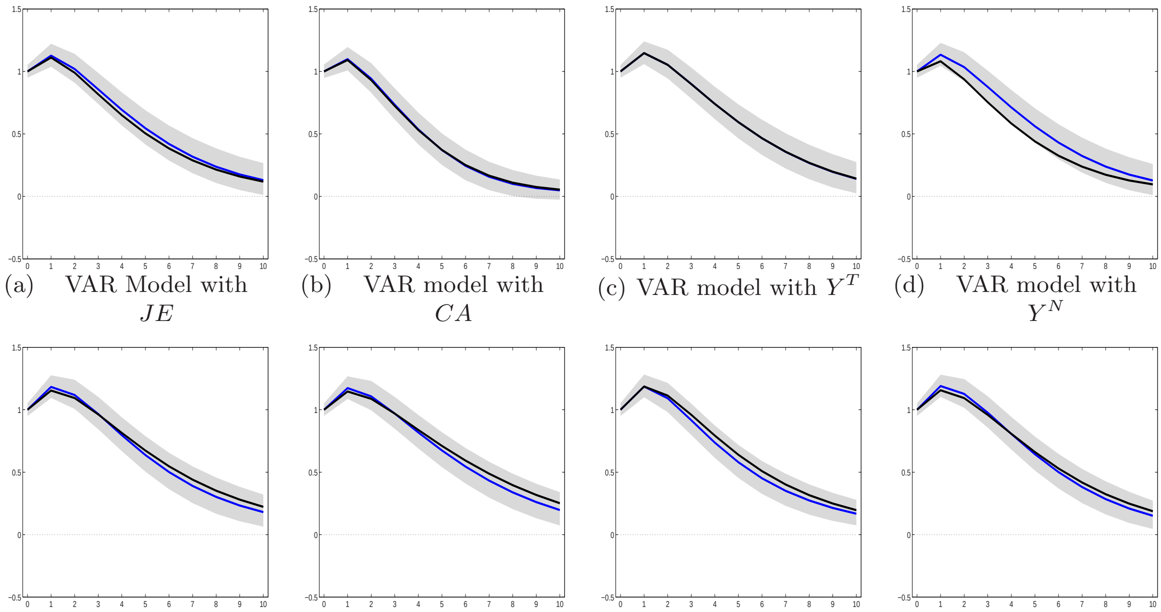


Figure 48: Contrasting Theoretical Impulse Response Functions for Potentially Varying Government Spending Shock. Notes: Impulse response functions to an exogenous increase in real government spending by one percent of GDP. The solid blue line displays the point estimate of VAR with the dotted blue lines indicating 90% confidence bounds; the solid black line displays model predictions in the baseline scenario, i.e., when we calibrate the model on the basis of the first VAR model, $z_{it} = [g_{it}, y_{it}, l_{it}, je_{it}, w_{C,it}]$; the dotted black line displays model predictions when we calibrate the model for a government spending shock specific to the VAR specification. In the first row, the red line and the dotted black line with squares display the empirical and theoretical response of government spending specific to the VAR specification, respectively.



(a) VAR Model with JE (b) VAR model with CA (c) VAR model with Y^T (d) VAR model with Y^N

(e) VAR model with ν_Y^T (f) VAR model with ν_Y^N (g) VAR model with P (h) VAR model with Ω

Figure 49: Impulse Response Functions for Government Spending across VAR specifications when G is Ordered Last in the VAR Model. Notes: Exogenous increase in government consumption by 1% of GDP. Results for baseline specification, i.e., G is ordered firt in the VAR model, are displayed by solid blue lines with the shaded area indicating the 90 percent confidence bounds obtained by bootstrap sampling; the black line reports results for a VAR model in which G is ordered last; sample: 16 OECD countries, 1970-2007, annual data.

is that political events are arguably exogenous (with respect to economic conditions) and thus identified government spending shocks are not subject to the potential endogeneity problem.

To further explore the potential endogeneity problem empirically, we use a dataset constructed by Gujardo, Leigh, and Pescatori [2014] in order to address the potential problem of endogeneity of government spending. Our objective is to investigate whether our main conclusions hold when adopting an alternative identification method. Using a narrative approach. Guajardo, Leigh, and Pescatori [2014] identify changes in fiscal policy directly from historical documents. More precisely, the dataset contains 173 fiscal policy changes for 17 OECD countries over the period 1978-2009. In order to make our results when adopting the 'event' approach comparable with our evidence obtained by adopting Blanchard and Perotti's [2002] identifying assumption, we restrict the set of countries to 15 and the period to 1978-2007. We then estimate the same VAR models described in section 2 in the main text.[73] We augment each baseline VAR model with identified fiscal events (ordered first in the VAR specification) corresponding to changes in government spending, i.e. 'spending-based' events. Figure 50 reports aggregate and sectoral effects while Figure 51 shows the sectoral composition effects.

While our results obtained by adopting Blanchard and Perotti's [2002] identifying assumption are broadly in line with those obtained with the narrative approach, we may nevertheless note some differences. Before discussing these differences, it is worth mentioning that Gujardo, Leigh, and Pescatori [2014] identify cases of fiscal consolidation motivated by a desire to reduce the budget deficit. To be consistent with the objective of our paper, we concentrate on episodes of fiscal consolidation implemented through changes in government spending rather than changes in tax rates. The authors find that fiscal consolidation through spending cuts gives rise to a contraction in GDP and investment. In order to be able to compare the effects of a government spending shock identified by applying Blanchard and Perotti's [2002] identification scheme with those following fiscal shocks identified by Guajardo, Leigh, and Pescatori [2014], we normalize the impulse response functions

[73] We exclude DEU and PRT which are not included in our empirical study. while NOR is removed from our sample.

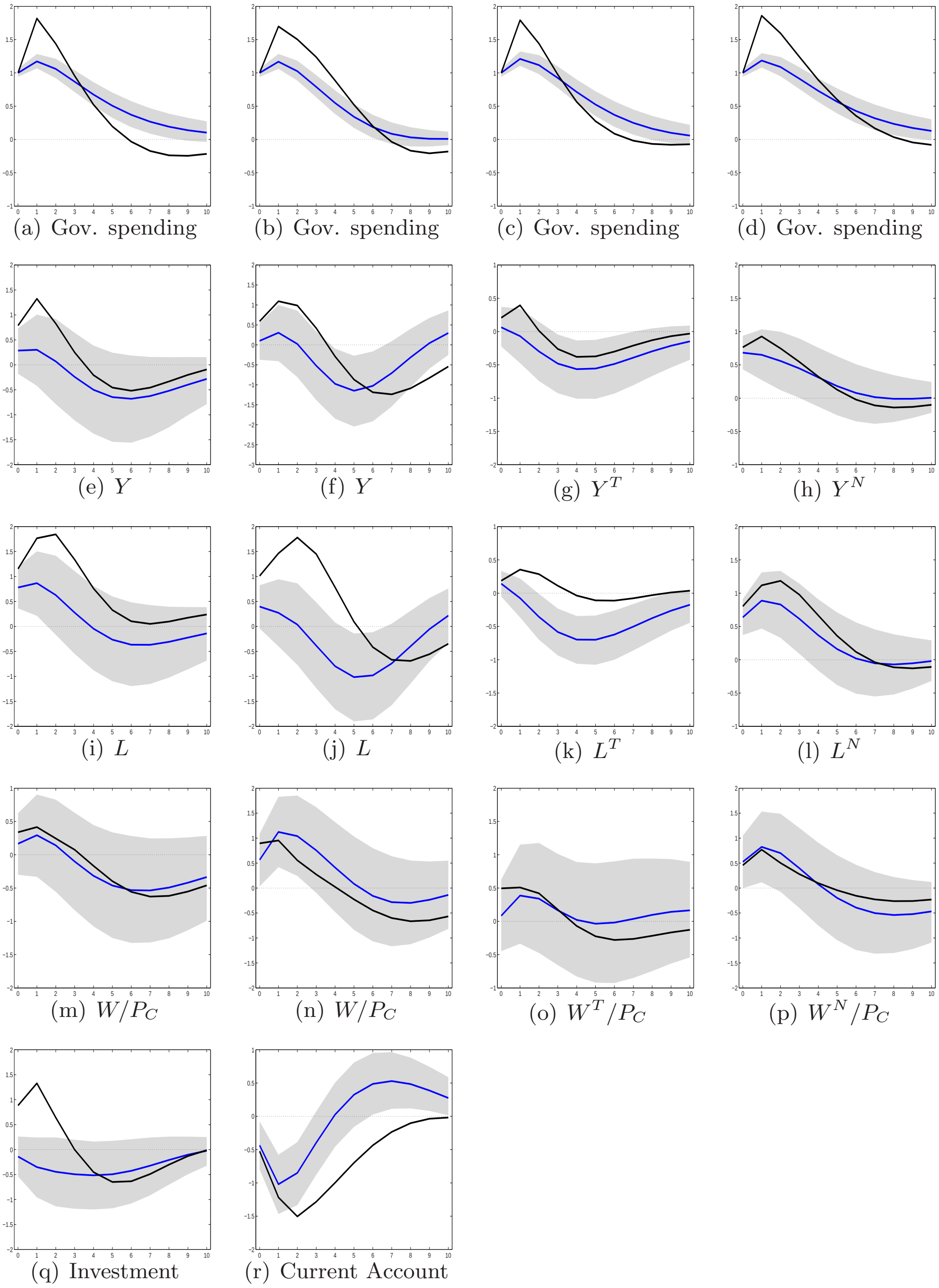


Figure 50: Contrasting Aggregate and Sectoral Effects of an Unanticipated Government Spending Shock between Alternative Identification Schemes of Government Spending Shock. Notes: Exogenous increase in government consumption by 1% of GDP. In the baseline case, government spending shocks are identified by assuming that government spending is predetermined relative to the other variables in the VAR model. Results for the baseline case are displayed by solid blue lines with the shaded area indicating 90 percent confidence bounds obtained by bootstrap sampling; the solid black line reports results for narratively identified government spending shocks from the dataset constructed by Guajardo, Leigh, and Pescatori [2014]; sample: 15 OECD countries, 1978-2007, annual data.

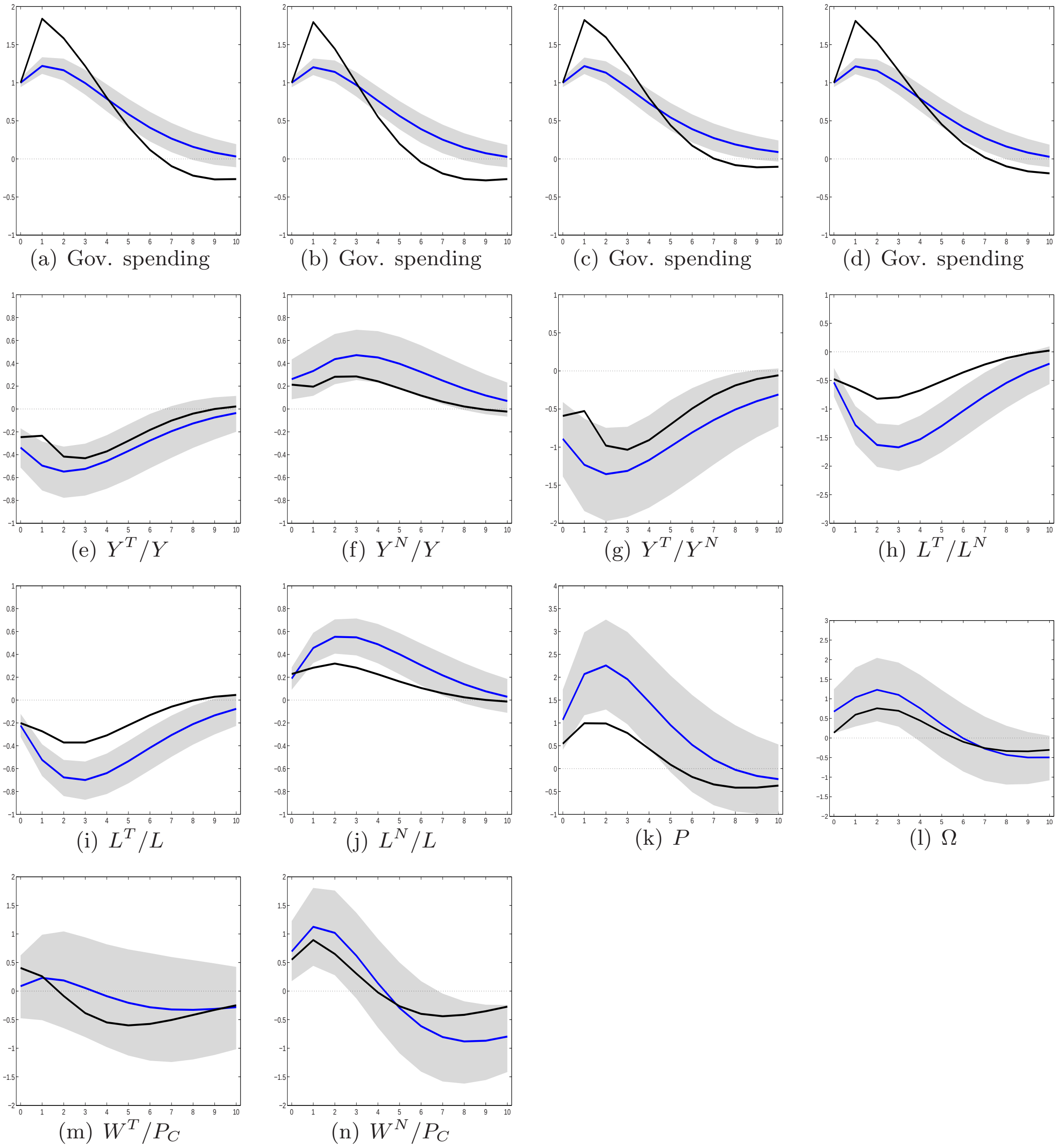


Figure 51: Contrasting the Effects of an Unanticipated Government Spending Shock on Sectoral Composition between Alternative Identification Schemes of Government Spending Shock. Notes: Exogenous increase in government consumption by 1% of GDP. In the baseline case, government spending shocks are identified by assuming that government spending is predetermined relative to the other variables in the VAR model. Results for the baseline case are displayed by solid blue lines with the shaded area indicating 90 percent confidence bounds obtained by bootstrap sampling; the solid black line reports results for narratively-identified government spending shocks from the dataset constructed by Gujardo, Leigh, and Pescatori [2014]; sample: 15 OECD countries, 1978-2007, annual data.

so that government consumption rises by 1 percentage point of GDP. In Figures 50 and 51, we report results for our four VAR specifications, augmenting each VAR model with the narrative shocks, ordered first. Results for the 'event' study are displayed in the solid black line while the solid blue line reports results in the baseline case in which government spending shocks are identified by applying Blanchard and Perotti's [2002] method.

- **Differences in responses of aggregate variables**. As displayed in the first row of Figure 50, while the shapes of the endogenous response of government spending are similar, the fiscal shock displays less persistence over time in the 'event' approach and is greater in the short-run; more precisely, we observe that increases in government spending over the first two years are more pronounced, while G is restored back toward its initial level more rapidly. In addition, in most of the cases, we observe a spending reversal which echoes Corsetti et al. [2012]; the magnitude of the cut in government spending during the reversal period (after 5 years approximately) is moderate though. Inspection of the dynamic effects of a government spending shock shows that the responses of aggregate variables are qualitatively similar whether the fiscal shock is identified by applying Blanchard and Perotti's [2002] method or by using an 'event' approach, except for investment. More precisely, while a rise in government spending increases both real GDP and hours worked and leads to a decline in the current account in either cases, we detect a significant increase in investment on impact in the 'event' approach, while investment declines gradually in the baseline case. We may also note some differences quantitatively, as real GDP and hours worked increase more in the 'event' approach than in the baseline case while the current account deficit is more pronounced. This result is not surprising since the government spending shock is more pronounced in the short-run.
- **Differences in responses of sectoral variables**. The last two columns of Figure 50 show the responses of sectoral labor and output, while Figure 51 displays the dynamic adjustment of sectoral shares along with the responses of the relative price and relative wage of non tradables. As can be seen in the last two columns of Figure 50, hours worked in the traded sector increase in the 'event' study while traded output rises in the short-run. Because the rise in government spending is more pronounced in the 'event' study, we also find empirically that labor and output in the non traded sector increase by a larger amount. While we detect a positive impact on traded output in the short run, the first column of Figure 51 shows that the share of tradables, whether measured in total employment or real GDP, declines after a fiscal shock. As can be seen in the first two columns of Figure 51, the responses of sectoral output shares are somewhat less pronounced in the 'event' study but lie within the confidence bounds of the baseline case. As displayed in the last two columns of Figure 51, hours worked and output in the traded sector falls relative to the non traded sector. Yet, the decline is much less pronounced than that in the baseline case. Moreover, both the relative price and the relative wage of non tradables appreciate by a smaller amount.

In sum, whether we consider a narrative approach or Blanchard and Perotti's [2002] identification scheme, all our results hold qualitatively, except for investment which is found to be crowded-in in the former approach. As mentioned above, we may notice some quantitative differences though. In particular, we find empirically that the rise in government spending has an expansionary effect on non traded output relative to traded output which is somewhat less pronounced in the 'event' study. In addition, the government spending shock gives rise to a positive response of traded output on impact and a contraction in the medium-run only.

How can the discrepancy between the two approaches be rationalized? Because the appreciation in the relative price of non tradables along with the responses of sectoral shares are less pronounced in the 'event' study, it seems reasonable to conjecture that changes in government spending identified by Gujardo, Leigh, and Pescatori [2014] are somewhat less biased toward non tradables than those identified by applying Blanchard and Perotti's [2002] method. The decline in hours worked in the traded sector relative to the non traded sector along with the increase in the relative wage of non tradables which are less pronounced tend to corroborate this conjecture. Furthermore, a relatively less intensive non traded sector in the government spending shock could rationalize the increase in investment expenditure in the short-run in the event approach. More precisely, the response of investment depends on the movement in Q/P_J where Q is the shadow value of capital and P_J the investment price index (which is an increasing function of the relative price of non tradables, P). Because the capital-labor ratio falls in the traded sector, the return on domestic capital and thus Q increases. Hence, the response of investment depends on the magnitude of the appreciation in the relative price of non tradables. If the government spending shock were not strongly biased toward non traded goods, the increase in Q could thus offset the rise in P_J so that investment is crowded-in. The second cause of the discrepancy in results obtained in the narrative approach with those obtained by applying Blanchard and Perotti's [2002] identification scheme could be based on the change in public investment. It may be possible that narratively identified fiscal shocks are associated with an increase in public investment.

To conclude, whether changes in government spending are identified by using a narrative approach or by applying the Blanchard and Perotti's [2002] assumption, our main conclusions hold. This result is reassuring as the Blanchard and Perotti's [2002] argument is not necessarily true when using annual data and such a robustness check tends to corroborate that government spending shocks we identify in our paper are exogenous. Such an empirical study also suggests that more work needs to be done in order to understand the cause(s) of the quantitative differences between the two approaches.

E Solving the Two-Sector Model without Physical Capital

In this section, we provide the main steps to solve the two-sector model without capital accumulation. This enables us to shed some light on the implications of a difficulty in reallocating labor across sectors for the fiscal transmission. The small open economy produces a traded and a non traded good by means of a production technology described by linearly homogenous production functions that use labor only. As previously, the output of the non traded good (Y^N) can be used for private (C^N) and public consumption (G^N). The output of the traded good (Y^T) can be consumed by households (C^T) and the government (G^T), or can be exported with $Y^T - C^T - G^T$ corresponding to net exports. To avoid technical details, the reader can jump to subsection E.13 that solves the model in a friendly way by assuming that the endogenous response of government spending to an exogenous fiscal shock decreases monotonically.

Furthermore, to ease the interpretation of analytical results, we set the following assumption:

Assumption 1 *The elasticity of labor supply across sectors, ϵ, is higher than the intertemporal elasticity of substitution for labor, σ_L.*

First, our panel data estimates for ϵ average 0.75 while empirical studies usually report estimates for the Frisch elasticity of labor supply ranging from 0.4 to 0.6. Second, as will be clear below, such an assumption guarantees that an open economy without physical capital runs a current account deficit, in line with our VAR evidence.

E.1 Households

At each instant the representative agent consumes traded goods and non-traded goods denoted by C^T and C^N, respectively, which are aggregated by a constant elasticity of substitution function:

$$C\left(C^T, C^N\right) = \left[\varphi^{\frac{1}{\phi}} \left(C^T\right)^{\frac{\phi-1}{\phi}} + (1-\varphi)^{\frac{1}{\phi}} \left(C^N\right)^{\frac{\phi-1}{\phi}}\right]^{\frac{\phi}{\phi-1}}. \tag{119}$$

The representative agent must also decide on worked hours in the traded and the non traded sector denoted by L^T and L^N at each instant of time which are aggregated by a constant elasticity of substitution function:

$$L\left(L^T, L^N\right) = \left[\vartheta^{-\frac{1}{\epsilon}} \left(L^T\right)^{\frac{\epsilon+1}{\epsilon}} + (1-\vartheta)^{-\frac{1}{\epsilon}} \left(L^N\right)^{\frac{\epsilon+1}{\epsilon}}\right]^{\frac{\epsilon}{\epsilon+1}}. \tag{120}$$

The agent is endowed with a unit of time and supplies a fraction $L(t)$ of this unit as labor, while the remainder, $1-L$, is consumed as leisure. At any instant of time, households derive utility from their consumption and experience disutility from working. Households decide on consumption and worked hours by maximizing lifetime utility:

$$U = \int_0^\infty \left\{ \frac{1}{1-\frac{1}{\sigma_C}} C(t)^{1-\frac{1}{\sigma_C}} - \frac{1}{1+\frac{1}{\sigma_L}} L(t)^{1+\frac{1}{\sigma_L}} \right\} e^{-\beta t} \mathrm{d}t, \tag{121}$$

where β is the consumer's discount rate, $\sigma_C > 0$ is the intertemporal elasticity of substitution for consumption, and $\sigma_L > 0$ is the Frisch elasticity of labor supply.

Households decide on consumption and worked hours by maximizing lifetime utility (121) subject to the flow budget constraint which states that the real disposable consisting of interest receipts from traded bonds holding plus labor income less lump sum taxes, T, can be consumed or saved by accumulating traded bonds:

$$\dot{B}(t) + P_C\left(P(t)\right) C(t) = r^\star B(t) + W\left(W^T(t), W^N(t)\right) L(t) - T(t), \tag{122}$$

where the RHS term of (122) corresponds to household's real disposable income.

Denoting the co-state variable associated with eq. (122) by λ, the first-order conditions characterizing the representative household's optimal plans are:

$$C = \left(P_C \lambda\right)^{-\sigma_C}, \tag{123a}$$

$$L = \left(\lambda W\right)^{\sigma_L}, \tag{123b}$$

$$\dot{\lambda} = \lambda\left(\beta - r^\star\right), \tag{123c}$$

and the transversality condition $\lim_{t\to\infty} \bar{\lambda} B(t) e^{-\beta t} = 0$. In an open economy model with a representative agent having perfect foresight, a constant rate of time preference and perfect access to world capital markets, we impose $\beta = r^\star$ in order to generate an interior solution. This standard assumption made in the literature implies that the marginal utility of wealth, λ, will undergo a discrete jump when individuals receive new information and must remain constant over time from thereon, i.e. $\lambda = \bar{\lambda}$.

The homogeneity of $C(.)$ and $L(.)$ allows a two-stage decision: in the first stage, consumption and total hours worked are determined, and the intratemporal allocation between tradables and non tradables is decided at the second stage. Households split consumption between tradables and non tradables according to the following optimal rule:

$$\left(\frac{1-\varphi}{\varphi}\right) \frac{C^T}{C^N} = P^\phi. \tag{124}$$

The allocation of total hours worked between the traded and the non traded sector follows from the following optimal rule:

$$\left(\frac{\vartheta}{1-\vartheta}\right) \frac{L^N}{L^T} = \Omega^\epsilon, \tag{125}$$

where $\Omega \equiv W^N/W^T$.

Plugging (124) into total consumption expenditure, i.e., $E_C = C^T + PC^N$, one obtains the optimal demand for tradables and non tradables:

$$C^T = \frac{\varphi \, .E_C}{\left[\varphi + (1-\varphi)\ .(P)^{1-\phi}\right]}, \tag{126a}$$

$$C^N = \frac{(1-\varphi)\ .E_C}{(P)^\phi \left[\varphi + (1-\varphi)\ .(P)^{1-\phi}\right]}. \tag{126b}$$

Substituting (126a) and (126b) into the subutility function (119) while setting $C = 1$ leads to the consumption price index:

$$P_C = \left[\varphi + (1-\varphi)(P)^{1-\phi}\right]^{\frac{1}{1-\phi}}, \tag{127}$$

where $P_C' = \frac{\partial P_C}{\partial P} > 0$. Having defined the consumption price index, total consumption expenditure, E_C, can be rewritten as $P_C C$. Applying the Shephard's Lemma gives the optimal demand for non tradables:

$$C^N = \frac{\partial P_C}{\partial P} C. \tag{128}$$

Using the fact that $C^T = P_C C - P C^N$, on obtains the optimal demand for tradables:

$$C^T = \left(P_C - P P_C'\right) .C. \tag{129}$$

Denoting by α_C the non tradable content of consumption expenditure defined by:

$$\alpha_C = \frac{(1-\varphi)(P)^{1-\phi}}{\varphi + (1-\varphi)(P)^{1-\phi}} = (1-\varphi)\left(\frac{P}{P_C}\right)^{1-\phi}, \tag{130a}$$

$$1 - \alpha_C = \frac{\varphi}{\varphi + (1-\varphi)(P)^{1-\phi}} = \varphi P_C^{\phi-1}, \tag{130b}$$

one can express consumption in non tradables as a share α_C of total consumption expenditure:

$$P C^N = \frac{\partial P_C}{\partial P}\frac{P}{P_C} P_C C = \alpha_C P_C C. \tag{131}$$

The same logic applies to consumption in tradables:

$$C^T = \left(1 - \frac{\partial P_C}{\partial P}\frac{P}{P_C}\right) P_C C = (1-\alpha_C) P_C C. \tag{132}$$

The representative household maximizes $1 - L(.)$ where $L(.)$ is a CES function given by (120) with $\epsilon > 0$ the intratemporal elasticity of substitution between labor in the traded and non traded sector, given total labor income denoted by R_L measured in terms of the traded good:

$$R_L \equiv W^T L^T + W^N L^N, \tag{133}$$

where W^T is the wage rate in the traded sector and W^N is the wage rate in the non traded sector. The linear homogeneity of the subutility function $L(.)$ implies that total labor income can be expressed as $R_L = W\left(W^T, W^N\right) L$, with $W\left(W^T, W^N\right)$ is the unit cost function dual (or aggregate wage index) to L. The unit cost dual function, $W(.)$, is defined as the minimum total labor income, R_L, such that $L = L\left(L^T, L^N\right) = 1$, for a given level of the wage rates W^T and W^N. We derive below its expression.

Combining (125) together with total labor income denoted by R_L measured in terms of the traded good, i.e. $R_L \equiv W^T L^T + W^N L^N$, we are able to express labor supply to the traded and non traded sector, respectively, as functions of total labor income:

$$L^T = (1-\vartheta)\left(W^T\right)^{-1}\left[(1-\vartheta) + \vartheta\left(\frac{W^N}{W^T}\right)^{\epsilon+1}\right]^{-1} R_L,$$

$$L^N = \vartheta\left(W^T\right)^{-1}\left(\frac{W^N}{W^T}\right)^{\epsilon}\left[(1-\vartheta) + \vartheta\left(\frac{W^N}{W^T}\right)^{\epsilon+1}\right]^{-1} R_L.$$

Plugging these equations into (120), setting $L = 1$ and $R_L = W$, yields the aggregate wage index:

$$W = \left[\vartheta\left(W^T\right)^{\epsilon+1} + (1-\vartheta)\left(W^N\right)^{\epsilon+1}\right]^{\frac{1}{\epsilon+1}}. \tag{134}$$

Intratemporal allocation of hours worked between the traded and the non traded sector follows from Shephard's Lemma (or the envelope theorem):

$$L^T = \frac{\partial W}{\partial W^T} L = W_T L, \quad \text{and} \quad \frac{W^T L^T}{WL} = 1 - \alpha_L, \tag{135a}$$

$$L^N = \frac{\partial W}{\partial W^N} L = W_N L, \quad \text{and} \quad \frac{W^N L^N}{WL} = \alpha_L, \tag{135b}$$

where the non tradable and tradable content of total labor income, respectively, are:

$$\alpha_L = \frac{(1-\vartheta)\left(W^N\right)^{\epsilon+1}}{\left[\vartheta\left(W^T\right)^{\epsilon+1} + (1-\vartheta)\left(W^N\right)^{\epsilon+1}\right]} = (1-\vartheta)\left(\frac{W^N}{W}\right)^{\epsilon+1}, \tag{136a}$$

$$1 - \alpha_L = \frac{\vartheta\left(W^T\right)^{\epsilon+1}}{\left[\vartheta\left(W^T\right)^{\epsilon+1} + (1-\vartheta)\left(W^N\right)^{\epsilon+1}\right]} = \vartheta\left(\frac{W^T}{W}\right)^{\epsilon+1}. \tag{136b}$$

We write out some useful properties:

$$\frac{\partial W}{\partial W^T}\frac{W^T}{W} = (1-\alpha_L), \quad \frac{\partial W}{\partial W^N}\frac{W^N}{W} = \alpha_L, \tag{137a}$$

$$\frac{\partial W_T}{\partial W^T} = \frac{\partial^2 W}{\partial\left(W^T\right)^2} = \vartheta\epsilon\left(W^T\right)^{\epsilon-1} W^{-\epsilon}\alpha_L, \tag{137b}$$

$$\frac{\partial W_T}{\partial W^T}\frac{W^T}{W_T} = \epsilon\alpha_L > 0, \tag{137c}$$

$$\frac{\partial W_T}{\partial W^N}\frac{W^N}{W_T} = -\epsilon\alpha_L < 0, \tag{137d}$$

$$\frac{\partial W_N}{\partial W^N}\frac{W^N}{W} = \epsilon(1-\alpha_L) > 0, \tag{137e}$$

$$\frac{\partial W_N}{\partial W^T}\frac{W^T}{W} = -\epsilon(1-\alpha_L) < 0, \tag{137f}$$

where $W_j = \frac{\partial W}{\partial W^j}$ (with $j = T, N$).

E.2 Firms

There are two sectors in the economy: a sector which produces a traded good denoted by the superscript T and a sector which produces a non traded good denoted by the superscript N. Both the traded and non traded sectors use labor, L^T and L^N, according to linearly homogenous production functions:

$$Y^T = L^T, \quad \text{and} \quad Y^N = L^N. \tag{138}$$

Both sectors face a labor cost equal to the wage rate, i.e., W^T and W^N, respectively. The traded sector and non traded sector are assumed to be perfectly competitive. The first order conditions derived from profit-maximization state that factors are paid to their respective marginal products:

$$1 = W^T, \quad \text{and} \quad P = W^N \tag{139}$$

Dividing the second equality by the first equality leads to a relationship between the relative price of non tradables, P, and the relative wage, $\Omega \equiv W^N/W^T$:

$$P = \Omega. \tag{140}$$

E.3 Short-Run Static Solutions for Consumption and Labor

In this subsection, we compute "short-run static solutions". This terminology refers to solutions of static optimality conditions which are inserted in dynamic optimality conditions in order to analyze the equilibrium dynamics. The term "short-run" refers to first-order conditions, and the term "static" indicates that the solution holds at each instant of time, and thus in the long-run.

Short-Run Static Solutions for Consumption and Labor

We begin with those for consumption and labor supply. Static efficiency conditions (123a) and (123b) can be solved for consumption and labor which of course must hold at any point of time:

$$C = C\left(\bar{\lambda}, P\right), \quad L = L\left(\bar{\lambda}, W^T, W^N\right), \tag{141}$$

with

$$C_{\bar{\lambda}} = \frac{\partial C}{\partial \bar{\lambda}} = -\sigma_C \frac{C}{\bar{\lambda}} < 0, \tag{142a}$$
$$C_P = \frac{\partial C}{\partial P} = -\alpha_C \sigma_C \frac{C}{P} < 0, \tag{142b}$$
$$L_{\bar{\lambda}} = \frac{\partial L}{\partial \bar{\lambda}} = \sigma_L \frac{L}{\bar{\lambda}} > 0, \tag{142c}$$
$$L_{W^T} = \frac{\partial L}{\partial W^T} = \sigma_L L \frac{(1-\alpha_L)}{W^T} > 0, \tag{142d}$$
$$L_{W^N} = \frac{\partial L}{\partial W^N} = \sigma_L L \frac{\alpha_L}{W^N} > 0, \tag{142e}$$

where we used the fact that $\frac{\partial W}{\partial W^T}\frac{W^T}{W} = (1-\alpha_L)$ and $\frac{\partial W}{\partial W^N}\frac{W^N}{W} = \alpha_L$; σ_C and σ_L correspond to the intertemporal elasticity of substitution for consumption and labor, respectively.

Inserting first the short-run solution for consumption (141), (128) and (129) can be solved for C^T and C^N:

$$C^T = C^T\left(\bar{\lambda}, P\right), \quad C^N = C^N\left(\bar{\lambda}, P\right), \tag{143}$$

where the partial derivatives are

$$C^T_{\bar{\lambda}} = -\sigma_C \frac{C^T}{\bar{\lambda}} < 0, \tag{144a}$$
$$C^T_P = \alpha_C \frac{C^T}{P}\left(\phi - \sigma_C\right) \lesseqgtr 0, \tag{144b}$$
$$C^N_{\bar{\lambda}} = -\sigma_C \frac{C^N}{\bar{\lambda}} < 0, \tag{144c}$$
$$C^N_P = -\frac{C^N}{P}\left[\left(1-\alpha_C\right)\phi + \alpha_C \sigma_C\right] < 0, \tag{144d}$$

where we used the fact that $-\frac{P''_C P}{P'_C} = \phi\left(1-\alpha_C\right) > 0$ and $P'_C C = C^N$.

Inserting first the short-run solution for labor (141), into $L^T = \frac{\partial W\left(W^T, W^N\right)}{\partial W^T} L$ and $L^N = \frac{\partial W\left(W^T, W^N\right)}{\partial W^N} L$, we are able to solve for L^T and L^N:

$$L^T = L^T\left(\bar{\lambda}, W^T, W^N\right), \quad L^N = L^N\left(\bar{\lambda}, W^T, W^N\right), \tag{145}$$

where the partial derivatives are

$$L^T_{\bar{\lambda}} = \frac{\partial L^T}{\partial \bar{\lambda}} = \sigma_L \frac{L^T}{\bar{\lambda}} > 0, \tag{146a}$$
$$L^T_{W^T} = \frac{\partial L^T}{\partial W^T} = \frac{L^T}{W^T}\left[\epsilon \alpha_L + \sigma_L\left(1-\alpha_L\right)\right] > 0, \tag{146b}$$
$$L^T_{W^N} = \frac{\partial L^T}{\partial W^N} = \frac{L^T}{W^N}\alpha_L\left(\sigma_L - \epsilon\right) \gtreqless 0, \tag{146c}$$
$$L^N_{\bar{\lambda}} = \frac{\partial L^N}{\partial \bar{\lambda}} = \sigma_L \frac{L^N}{\bar{\lambda}} > 0, \tag{146d}$$
$$L^N_{W^N} = \frac{\partial L^N}{\partial W^N} = \frac{L^N}{W^N}\left[\epsilon\left(1-\alpha_L\right) + \sigma_L \alpha_L\right] > 0, \tag{146e}$$
$$L^N_{W^T} = \frac{\partial L^N}{\partial W^T} = \frac{L^N}{W^T}\left(1-\alpha_L\right)\left(\sigma_L - \epsilon\right) \gtreqless 0, \tag{146f}$$

(146g)

where we used the fact that $\frac{W_{TT}W^T}{W_T} = \epsilon\alpha_L$, $\frac{W_{TN}W^N}{W_T} = -\epsilon\alpha_L$, $\frac{W_{NN}W^N}{W_N} = \epsilon(1-\alpha_L)$, $\frac{W_{NT}W^T}{W_N} = -\epsilon(1-\alpha_L)$.

Short-Run Static Solutions for Sectoral Wages

First order conditions (139) can be solved for the sectoral wages:

$$W^T = \text{constant}, \quad W^N = W^N(P), \tag{147}$$

where the partial derivative is:

$$W_P^N = \frac{\partial W^N}{\partial P} = 1 = \frac{W^N}{P} > 0. \tag{148}$$

Inserting (147) into (145) yields:

$$L^T = L^T\left(\bar{\lambda}, P\right), \quad L^N = L^N\left(\bar{\lambda}, P\right), \tag{149}$$

where the partial derivatives are

$$L_P^T = \frac{\partial L^T}{\partial P} = L_{W^N}^T W_P^N = \frac{L^T}{P}\alpha_L(\sigma_L - \epsilon) \gtrless 0, \tag{150a}$$

$$L_P^N = \frac{\partial L^N}{\partial P} = L_{W^N}^N W_P^N = \frac{L^N}{P}\left[\epsilon(1-\alpha_L) + \sigma_L\alpha_L\right] > 0, \tag{150b}$$

and $L_{\bar{\lambda}}^T$ and $L_{\bar{\lambda}}^N$ are given by (146a) and (146d), respectively.

E.4 Market Clearing Conditions

To fully describe the equilibrium, we impose goods market clearing conditions. The non traded good market clearing condition requires that non traded output is equalized with demand for non tradables:

$$Y^N = C^N + G^N. \tag{151}$$

Plugging this condition into the flow budget constraint (122) and using firms' optimal conditions (139) yields the market clearing condition for tradables or the current account equation:

$$\dot{B} = r^\star B + Y^T - C^T - G^T, \tag{152}$$

where the sum of the last three terms on the RHS, i.e., $Y^T - C^T - G^T \equiv NX$, corresponds to net exports denoted by NX.

Inserting short-run static solutions for C^N for L^N given by (143) and (149), respectively, into the non traded good market clearing condition (151) gives us:

$$L^N\left(\bar{\lambda}, P\right) = C^N\left(\bar{\lambda}, P\right) + G^N. \tag{153}$$

The non traded good market clearing condition can be solved for the relative price of non tradables by totally differentiating (153):

$$\alpha_L \hat{L}^N = \omega_C \alpha_C \hat{C}^N + \frac{P\mathrm{d}G^N}{Y}, \tag{154}$$

where we denote the ratio of consumption expenditure to GDP by $\omega_C = \frac{P_C C}{Y}$; to determine the LHS of (154), we used the fact that $Y = Y^T + PY^N = W^T L^T + W^N L^N = WL$ because $Y^T = L^T$ and $Y^N = L^N$; since $W^N = P$ together with the definition of α_L given by eq. (135b), we have

$$\frac{PY^N}{Y} = \frac{W^N L^N}{WL} = \alpha_L. \tag{155}$$

Inserting short-run static solutions and collecting terms yield:

$$\hat{P} = \frac{-\hat{\bar{\lambda}}\left[\alpha_L\sigma_L + \omega_C\alpha_C\sigma_C\right] + \frac{P\mathrm{d}G^N}{Y}}{\Psi}, \tag{156}$$

where we set

$$\Psi = \alpha_L \left[\epsilon \left(1-\alpha_L\right) + \sigma_L \alpha_L\right] + \omega_C \alpha_C \left[\left(1-\alpha_C\right)\phi + \alpha_C \sigma_C\right] > 0. \tag{157}$$

Invoking the implicit functions theorem, eq. (156) leads to the short-run static solution for the relative price of non tradables:

$$P = P\left(\bar{\lambda}, G^N\right), \tag{158}$$

where $P_{\bar{\lambda}} < 0$ and $P_{G^N} > 0$.

E.5 Solutions for Sectoral Labor

Totally differentiating the short-run static solution for traded labor $L^T = L^T\left(\bar{\lambda}, P\right)$ given by (149) yields:

$$\hat{L}^T = \sigma_L \hat{\bar{\lambda}} + \alpha_L \left(\sigma_L - \epsilon\right) \hat{P}.$$

Inserting the short-run static solution for the relative price P given by (158) allows us to solve for traded labor:

$$\hat{L}^T = \frac{\left[\sigma_L \Psi + \alpha_L \left(\epsilon - \sigma_L\right)\left(\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C\right)\right] \hat{\bar{\lambda}}}{\Psi} + \frac{\alpha_L \left(\sigma_L - \epsilon\right)}{\Psi} \frac{P \mathrm{d}G^N}{Y}. \tag{159}$$

Eq. (159) solves for traded labor:

$$L^T = L^T\left(\bar{\lambda}, G^N\right), \tag{160}$$

where $L^T_{\bar{\lambda}} > 0$, and $L^T_{G^N} < 0$.

Totally differentiating the short-run static solution for traded labor $L^N = L^N\left(\bar{\lambda}, P\right)$ given by (149) leads to:

$$\hat{L}^N = \sigma_L \hat{\bar{\lambda}} + \left[\epsilon\left(1-\alpha_L\right) + \sigma_L \alpha_L\right] \hat{P}.$$

Inserting the short-run static solution for the relative price P given by (158) allows us to solve for non traded labor:

$$\begin{aligned} \hat{L}^N &= \frac{\left\{\sigma_L \Psi - \left(\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C\right)\left[\epsilon\left(1-\alpha_L\right) + \sigma_L \alpha_L\right]\right\} \hat{\bar{\lambda}}}{\Psi} \\ &+ \frac{\left[\epsilon\left(1-\alpha_L\right) + \sigma_L \alpha_L\right]}{\Psi} \frac{P \mathrm{d}G^N}{Y}, \end{aligned} \tag{161}$$

where

$$\begin{aligned} & \sigma_L \Psi - \left(\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C\right)\left[\epsilon\left(1-\alpha_L\right) + \sigma_L \alpha_L\right] \\ = \; & \omega_C \alpha_C \left\{\sigma_L \left[\left(1-\alpha_C\right)\phi + \alpha_C \sigma_C\right] - \sigma_C \left[\epsilon\left(1-\alpha_L\right) + \sigma_L \alpha_L\right]\right\} \gtrless 0. \end{aligned}$$

Eq. (161) solves for non traded labor:

$$L^N = L^N\left(\bar{\lambda}, G^N\right), \tag{162}$$

where $L^N_{\bar{\lambda}} \gtrless 0$, and $L^N_{G^N} > 0$.

E.6 Equilibrium Dynamics and Formal Solutions

Inserting the short-run static solution for L^T (160) and for C^T (143) into the current account equation (152) yields:

$$\dot{B}(t) = r^\star B(t) + L^T\left(\bar{\lambda}, G^N\right) - C^T\left(\bar{\lambda}, P\right) - G^T. \tag{163}$$

Remembering that P is fixed while the shadow value of wealth, λ, may jump when new information arrives but remains fixed over time, i.e., $\lambda = \bar{\lambda}$, and linearizing (163) in the neighborhood of the steady-state leads to:

$$\dot{B}(t) = r^\star \left(B(t) - \tilde{B}\right). \tag{164}$$

The general solution is:

$$B(t) = \tilde{B} + D_2 e^{r^\star t}, \tag{165}$$

where D_2 is an arbitrary constant determined by initial conditions. Invoking the transversality condition, i.e., $\lim_{t\to\infty} \bar{\lambda} B(t) e^{-r^\star t} = 0$, the stable solution is:

$$B(t) = \tilde{B}, \tag{166}$$

and the intertemporal solvency condition (ISC) reads:

$$\tilde{B} = B_0. \tag{167}$$

While a permanent fiscal shock does not affect the net foreign asset position, a temporary fiscal shock, by modifying initial conditions, permanently modifies the stock of foreign assets.

E.7 Steady-State

Inserting the ISC (167) and appropriate short-run static solutions which obviously hold in the long-run, the steady-state can be reduced to one equation

$$r^\star B_0 + L^T\left(\bar{\lambda}, G^N\right) - C^T\left[\bar{\lambda}, P\left(\bar{\lambda}, G^N\right)\right] - G^T = 0. \tag{168}$$

Equation (168) can be solved for the marginal utility of wealth:

$$\bar{\lambda} = \lambda\left(G^N, G^T\right). \tag{169}$$

Note that we concentrate below on a rise in government spending on non tradables G^N because empirical evidence indicate that the non-tradable content of public spending averages to 90% for OECD countries. At the end of the section, we investigate the effects of a temporary increase in G^T and show that the predictions of the model, in this configuration, are at odds with the panel VAR evidence.

Using the fact that the stock of traded bonds is initially predetermined and totally differentiating (168) yields:

$$(1-\alpha_L)\hat{L}^T = \omega_C (1-\alpha_C)\hat{C}^T + \frac{\mathrm{d}G^T}{Y}, \tag{170}$$

where we used the definition of α_L given by eq. (155).

We first solve for consumption in tradables by totally differentiating $C^T\left[\bar{\lambda}, P\left(\bar{\lambda}, G^N\right)\right]$:

$$\hat{C}^T = -\sigma_C \hat{\bar{\lambda}} + \alpha_C (\phi - \sigma_C)\hat{P}.$$

Inserting (156) allows us to solve for consumption in tradables:

$$C^T = C^T\left(\bar{\lambda}, G^N\right) \tag{171}$$

where partial derivatives are given by:

$$\hat{C}^T = -\left\{\frac{\sigma_C \Psi + \alpha_C(\phi-\sigma_C)\left[\alpha_L\sigma_L + \omega_C\alpha_C\sigma_C\right]}{\Psi}\right\}\hat{\bar{\lambda}} + \frac{\alpha_C(\phi-\sigma_C)}{\Psi}\frac{P\mathrm{d}G^N}{Y}. \tag{172}$$

Plugging $\hat{C}^T = -\sigma_C\hat{\bar{\lambda}} + \alpha_C(\phi-\sigma_C)\hat{P}$ and $\hat{L}^T = \sigma_L\hat{\bar{\lambda}} + \alpha_L(\sigma_L - \epsilon)\hat{P}$, eq. (170) can be rewritten as follows:

$$\begin{aligned} &\hat{\bar{\lambda}}\left[(1-\alpha_L)\sigma_L + \omega_C(1-\alpha_C)\sigma_C\right] \\ &+\hat{P}\left[(1-\alpha_L)\alpha_L(\sigma_L-\epsilon) - \omega_C(1-\alpha_C)\alpha_C(\phi-\sigma_C)\right] = \frac{\mathrm{d}G^T}{Y}. \end{aligned}$$

Inserting (156) into the above equation and collecting terms, the change in the marginal utility of wealth is given by:

$$\hat{\lambda} = \frac{P\mathrm{d}G^N}{Y}\frac{\left[\omega_C(1-\alpha_C)\alpha_C(\phi-\sigma_C) + (1-\alpha_L)\alpha_L(\epsilon-\sigma_L)\right]}{\Gamma} + \frac{\mathrm{d}G^T}{Y}\frac{\Psi}{\Gamma}, \tag{173}$$

where Ψ is given by (156) and we set

$$\begin{aligned} \Gamma &= \left[\alpha_L\sigma_L + \omega_C\alpha_C\sigma_C\right]\left[\omega_C(1-\alpha_C)\alpha_C(\phi-\sigma_C) + (1-\alpha_L)\alpha_L(\epsilon-\sigma_L)\right] \\ &+ \left[(1-\alpha_L)\sigma_L + \omega_C(1-\alpha_C)\sigma_C\right]\Psi > 0. \end{aligned} \tag{174}$$

E.8 Derivation of Steady-State Solutions

In this subsection, we derive steady-state solutions. The steady-state reduces to two equations:

$$r^{\star}\tilde{B} + \tilde{L}^{T} - \tilde{C}^{T} - G^{T} = 0, \tag{175a}$$

together with the intertemporal solvency condition

$$\tilde{B} = B_0, \tag{175b}$$

which jointly solve for the stock of traded bonds $\tilde{B}$ and the marginal utility of wealth $\bar{\lambda}$.

We first solve the system (175a) for $\tilde{B}$ as a function of the marginal utility of wealth, $\bar{\lambda}$ and government spending on non tradables G^N and tradables G^T. To do so, substitute solutions for traded labor (159) and for consumption in tradables (171), into the traded good market clearing condition (175a):

$$r^{\star}\tilde{B} + L^{T}\left(\bar{\lambda}, G^{N}\right) - C^{T}\left(\bar{\lambda}, G^{N}\right) - G^{T} = 0. \tag{176}$$

Solving (176) for the steady-state value of B, we are able to express B as a function of the shadow value of wealth and government spending on non tradables, G^N, and tradables, G^T:

$$\tilde{B} = B\left(\bar{\lambda}, G^{N}, G^{T}\right), \tag{177}$$

with partial derivatives given by:

$$\begin{aligned}
B_{\bar{\lambda}} \equiv \frac{\partial \tilde{B}}{\partial \bar{\lambda}} &= -\frac{\left(L^{T}_{\bar{\lambda}} - C^{T}_{\bar{\lambda}}\right)}{r^{\star}}, \\
&= -\frac{Y}{r^{\star}}\left[(1-\alpha_L)\frac{\hat{L}^{T}}{\hat{\bar{\lambda}}} - \omega_C (1-\alpha_C)\frac{\hat{C}^{T}}{\hat{\bar{\lambda}}}\right]\hat{\bar{\lambda}}, \\
&= -\frac{Y}{r^{\star}\bar{\lambda}}\frac{\Gamma}{\Psi} < 0, \qquad (178a)\\
B_{G^N} \equiv \frac{\partial \tilde{B}}{\partial G^{N}} &= -\frac{\left(L^{T}_{G^N} - C^{T}_{G^N}\right)}{r^{\star}}, \\
&= -\frac{Y}{r^{\star}}\left[(1-\alpha_L)\frac{L^{T}_{G^N}}{L^{T}} - \omega_C (1-\alpha_C)\frac{C^{T}_{G^N}}{C^{T}}\right], \\
&= \frac{Y}{r^{\star}}\left[\frac{\omega_C (1-\alpha_C)\alpha_C(\phi-\sigma_C) + (1-\alpha_L)\alpha_L(\epsilon-\sigma_L)}{\Psi}\right]\frac{P}{Y} > 0, \qquad (178b)
\end{aligned}$$

where $\Psi > 0$ is given by (156) and $\Gamma > 0$ is given by (174) and we used the fact that $(1-\alpha_L)\frac{\hat{L}^{T}}{\hat{\bar{\lambda}}} - \omega_C(1-\alpha_C)\frac{\hat{C}^{T}}{\hat{\bar{\lambda}}} = \Gamma$.

Inserting (177) into the ISC (175b) yields:

$$B\left(\bar{\lambda}, G^{N}, G^{T}\right) = B_0. \tag{179}$$

Totally differentiating the above equation and collecting terms gives the change in the equilibrium value of the marginal utility of wealth:

$$\begin{aligned}
\left.\frac{\mathrm{d}\bar{\lambda}}{\mathrm{d}G^{N}}\right|_{perm} &= -\frac{B_{G^N}}{B_{\bar{\lambda}}}, \\
&= \frac{\bar{\lambda}\left[\omega_C(1-\alpha_C)\alpha_C(\phi-\sigma_C) + (1-\alpha_L)\alpha_L(\epsilon-\sigma_L)\right]}{\Gamma}\frac{P}{Y}, \qquad (180)
\end{aligned}$$

where the subscript *perm* refers to the effect of a permanent increase in government consumption.

E.9 Derivation of Steady-State Changes Following a Permanent Government Spending Shock

We now derive the steady-state changes of key macroeconomic variables following an unanticipated and exogenous permanent government spending shock. Inserting the change in the equilibrium value of the marginal utility of wealth given by (173) into (155) gives the steady-state change of the relative price of non tradables:

$$\hat{P} = \frac{[(1-\alpha_L)\sigma_L + \omega_C(1-\alpha_C)\sigma_C]}{\Gamma}\frac{P\mathrm{d}G^N}{Y} - \frac{[\alpha_L\sigma_L + \omega_C\alpha_C\sigma_C]}{\Gamma}\frac{\mathrm{d}G^T}{Y}. \tag{181}$$

Hence, a permanent increase in G^N unambiguously appreciates the relative price of non tradables in the long-run while a permanent rise in G^T depreciates it.

Totally differentiating (159), inserting the change in the equilibrium value of the marginal utility of wealth given by (173) gives the steady-state change of traded labor:

$$\begin{aligned}\hat{L}^T &= \frac{\omega_C(1-\alpha_C)[\alpha_C(\phi-\sigma_C)\sigma_L + \sigma_C\alpha_L(\sigma_L-\epsilon)]}{\Gamma}\frac{P\mathrm{d}G^N}{Y} \\ &+ \left\{\frac{\sigma_L\alpha_L\epsilon + \omega_C\alpha_C\{\sigma_L[(1-\alpha_C)\phi + \alpha_C\sigma_C] + \sigma_C\alpha_L(\epsilon-\sigma_L)\}}{\Gamma}\right\}\frac{\mathrm{d}G^T}{Y}. \end{aligned}\tag{182}$$

In contrast to a model imposing perfect mobility of labor across sectors, traded labor does not necessarily fall. Yet, as shown later, the ratio L^T/L^N unambiguously declines.

Totally differentiating (160), inserting the change in the equilibrium value of the marginal utility of wealth given by (173) gives the steady-state change of non traded labor:

$$\begin{aligned}\hat{L}^N &= \left\{\frac{(1-\alpha_L)\sigma_L\epsilon + \omega_C(1-\alpha_C)\{\sigma_L\alpha_C(\phi-\sigma_C) + \sigma_C[\epsilon(1-\alpha_L)+\sigma_L\alpha_L]\}}{\Gamma}\right\}\frac{P\mathrm{d}G^N}{Y} \\ &- \frac{\omega_C\alpha_C}{\Gamma}\{\sigma_C[\epsilon(1-\alpha_L)+\sigma_L\alpha_L] - \sigma_L[(1-\alpha_C)\phi + \alpha_C\sigma_C]\}\frac{\mathrm{d}G^T}{Y}. \end{aligned}\tag{183}$$

According to (183), a permanent rise in G^N unambiguously raises L^N in the long-run while a permanent increase in G^T may raise or lower L^N depending on whether the cost of shifting hours worked from one sector to another is high or low.

We now derive the steady-state in the consumption wage W/P_C. To do so, remembering that $W = W\left[W^T, W^N(P)\right]$, using the fact that $\frac{\partial W}{\partial W^N}\frac{W^N}{W} = \alpha_L$ and $\frac{\partial W^N}{\partial P}\frac{P}{W^N} = 1$, the steady-state change in the aggregate wage index is:

$$\hat{W} = \alpha_L\hat{P} > 0, \tag{184}$$

where $\hat{P}$ is given by (181). Moreover, the change in the consumption price index is given by $\hat{P}_C = \alpha_C\hat{P}$. Hence, using (184), the change in the consumption aggregate wage is given by:

$$\mathrm{d}\left(\frac{W}{P_C}\right) = \frac{W}{P_C}(\alpha_L - \alpha_C)\hat{P} > 0, \tag{185}$$

where the sign follows from the fact that data indicate that $\alpha_L > \alpha_C$, i.e., the non tradable content of labor income is larger that the non tradable content of consumption expenditure.

E.10 Derivation of Formal Solutions after Temporary Fiscal Shocks

In this subsection, we determine the solutions following a temporary fiscal expansion. In order to produce a hump-shaped response in line with the evidence, the endogenous response of government spending to an exogenous fiscal shocks is assumed to be governed by the following dynamic equation:

$$\frac{dG(t)}{Y} \equiv \frac{G(t)-\tilde{G}}{Y} = \left[e^{-\xi t} - (1-g)\,e^{-\chi t}\right], \tag{186}$$

where Y is initial steady-state GDP, ξ and χ are positive parameters which satisfy the following inequality

$$\chi(1-g) > \xi > 0. \tag{187}$$

Inequality (187) guarantees that government spending rises after its initial upward jump. Because the non tradable content of government spending averages 90% for the 15 OECD countries in our sample and thus changes in public expenditure are mostly reflected by changes in purchases of non tradables by the public sector, we further assume that the rise in government consumption is fully biased toward non tradables; in linearized form, we have:

$$\tilde{P}\left(G^N(t)-\tilde{G}^N\right)=G(t)-\tilde{G}, \tag{188}$$

where we denote the long-term values with a tilde. In the quantitative analysis, we relax this assumption and consider a rise in government spending by 1 percentage point of GDP which is split between non tradables and tradables in accordance with their respective shares, at 90% and 10%, respectively.

Solution for the Net Foreign Asset Position $B(t)$

To begin with, we linearize the current account equation (163) in the neighborhood of the steady-state:

$$\dot{B}(t)=r^{\star}\left(B(t)-\tilde{B}\right)+\left(L_P^T-C_P^T\right)P_{G^N}\left(G^N(t)-\tilde{G}^N\right). \tag{189}$$

Inserting $L_P^T=\frac{L^T}{P}\alpha_L\left(\sigma_L-\epsilon\right)$ (see eq. (150a)) and $\frac{C^T}{P}\alpha_C\left(\phi-\sigma_C\right)$ (see eq. (144b)), eq. (189) can be rewritten as follows:

$$\begin{aligned}\dot{B}(t) &= r^{\star}\left(B(t)-\tilde{B}\right)+\left[\tilde{L}^T\alpha_L\left(\sigma_L-\epsilon\right)-\tilde{C}^T\alpha_C\left(\phi-\sigma_C\right)\right]\frac{P_G^N}{P}\left(G^N(t)-\tilde{G}^N\right),\\ &= r^{\star}\left(B(t)-\tilde{B}\right)-\left[\left(1-\alpha_L\right)\alpha_L\left(\epsilon-\sigma_L\right)+\left(1-\alpha_C\right)\omega_C\alpha_C\left(\phi-\sigma_C\right)\right]\frac{\tilde{P}}{\Psi}\left(G^N(t)-\tilde{G}^N\right),\\ &= r^{\star}\left(B(t)-\tilde{B}\right)-\frac{\left[\left(1-\alpha_L\right)\alpha_L\left(\epsilon-\sigma_L\right)+\left(1-\alpha_C\right)\omega_C\alpha_C\left(\phi-\sigma_C\right)\right]}{\Psi}\left(G(t)-\tilde{G}\right), \quad (190)\end{aligned}$$

where $1-\alpha_L=\frac{W^TL^T}{WL}=\frac{L^T}{Y}$ (with $Y=Y^T+PY^N=W^TL^T+W^NL^N=WL$ and $W^T=1$), we substituted $\frac{P_{G^N}}{P}=\frac{\partial P}{\partial G^N}\frac{1}{P}=\frac{P}{Y}\frac{1}{\Psi}$ to obtain the second line and we used the fact that $dG^N(t)=\frac{dG(t)}{\tilde{P}}$ to get the third line. As long as $\epsilon>\sigma_L$ and $\phi\simeq\sigma_C$, a rise in government spending above trend tends to affect negatively the net foreign asset position.

Eq. (190) can be rewritten in a more compact form

$$\dot{B}(t)=r^{\star}\left(B(t)-\tilde{B}\right)-\Upsilon_G^NY\left[e^{-\xi t}-(1-g)\,e^{-\chi t}\right], \tag{191}$$

where we have inserted (186) and set

$$\Upsilon_G^N\equiv-\frac{\partial\dot{B}(t)}{\partial G(t)}=\frac{\left[\left(1-\alpha_L\right)\alpha_L\left(\epsilon-\sigma_L\right)+\left(1-\alpha_C\right)\omega_C\alpha_C\left(\phi-\sigma_C\right)\right]}{\Psi}\gtrless 0. \tag{192}$$

Pre-multiplying by $e^{-r^{\star}\tau}$ and integrating over $(0,t)$ allow us to obtain the general solution for $B(t)$:

$$B(t)-\tilde{B}=\left[\left(B_0-\tilde{B}\right)-\frac{\Upsilon_G^NY}{\xi+r^{\star}}\left(1-\Theta'\right)\right]e^{r^{\star}t}+\frac{\Upsilon_G^NY}{\xi+r^{\star}}\left(e^{-\xi t}-\Theta'e^{-\chi t}\right), \tag{193}$$

where we used the fact that $\int_0^t e^{-(\xi+r^{\star})\tau}d\tau=\frac{\left(1-e^{-(\xi+r^{\star})t}\right)}{\xi+r^{\star}}$ and we set:

$$\Theta'=(1-g)\frac{\xi+r^{\star}}{\chi+r^{\star}}>0. \tag{194}$$

Invoking the transversality condition, one obtains the 'stable' solution for the stock of foreign assets so that $B(t)$ converges toward its steady-state value $\tilde{B}$:

$$B(t)-\tilde{B}=\frac{\Upsilon_G^NY}{\xi+r^{\star}}\left(e^{-\xi t}-\Theta'e^{-\chi t}\right). \tag{195}$$

Eq. (193) gives the trajectory for for $B(t)$ consistent with the intertemporal solvency condition:

$$\left(\tilde{B}-B_0\right)=-\frac{\Upsilon_G^NY}{\xi+r^{\star}}\left(1-\Theta'\right), \tag{196}$$

where $1-\Theta' > 0$ due to inequality (187). While the sign of Υ_G^N is ambiguous, we expect $\Upsilon_G^N > 0$ so that a temporary rise in government spending deteriorates the net foreign asset position, i.e., $d\tilde{B} < 0$. More specifically, invoking assumption 1, we have $\Upsilon_G^N > 0$ (see eq. (192)) as long as $\phi \simeq \sigma_C$; in other words, a rise in government consumption produces a decline in hours worked in the traded sector while consumption in tradables is merely affected.

Eq. (195) can be rewritten as follows:

$$B(t) - \tilde{B} = \Upsilon_G^N \int_t^{\infty} dG(\tau) e^{-r^{\star}(\tau - t)} d\tau, \tag{197}$$

where $\int_t^{\infty} dG(\tau) e^{-r^{\star}(\tau-t)} d\tau$ corresponds to the temporal path for government spending expressed in present value terms:

$$\begin{aligned} \int_t^{\infty} dG(\tau) e^{-r^{\star}(\tau-t)} d\tau &= \frac{Y e^{r^{\star} t}}{\xi + r^{\star}} \left[e^{-(\xi + r^{\star})t} - \Theta' e^{-(\chi + r^{\star})t} \right], \\ &= \frac{Y}{\xi + r^{\star}} \left(e^{-\xi t} - \Theta' e^{-\chi t} \right). \end{aligned} \tag{198}$$

Differentiating (195) w.r.t. time gives the trajectory for the current account along the transitional path when government spending follows the temporal path given by eq. (186):

$$\dot{B}(t) = -\frac{\Upsilon_G^N Y}{\xi + r^{\star}} \left(\xi e^{-\xi t} - \chi \Theta' e^{-\chi t} \right). \tag{199}$$

As long as we impose assumption 1 along with $\phi \simeq \sigma_C$, we have $\Upsilon_G^N > 0$, so that the current account deteriorates monotonically since $\left(\xi e^{-\xi t} - \chi \Theta' e^{-\chi t} \right) > 0$ for $t \geq 0$.

Evaluating (199) at time $t = 0$ leads to the initial current account response, expressed as a percentage of initial GDP, following a temporary rise in government spending:

$$\left. \frac{\dot{B}(0)}{Y} \right|_{temp} = -\frac{\Upsilon_G^N}{\xi + r^{\star}} \left(\xi - \chi \Theta' \right) < 0, \tag{200}$$

where $\Upsilon_G^N > 0$ and $(\xi - \chi\Theta') > 0$. Note that $-\left[\xi - (1-g)\chi\right] > 0$ guarantees that government spending increases after initial rise $dG(0)$, i.e., $\dot{G}(0) > 0$, inequality $(\xi - \chi\Theta') > 0$ implies that the cumulative endogenous response of government spending to an exogenous fiscal shock is decreasing in present discounted value terms.

The Change in the Equilibrium Value of the Marginal Utility of Wealth

Eq. (196) gives the steady-state change in the foreign asset position following a temporary (denoted by the subscript *temp*) rise in government spending:

$$\left. d\tilde{B} \right|_{temp} = -\frac{\Upsilon_G^N Y}{\xi + r^{\star}} \left(1 - \Theta' \right) < 0. \tag{201}$$

To determine the change in the equilibrium value of the marginal utility of wealth, we have to differentiate the market clearing condition for the traded good (176):

$$r^{\star} \left. d\tilde{B} \right|_{temp} + \left(L_{\lambda}^T - C_{\lambda}^T \right) \left. d\bar{\lambda} \right|_{temp} = 0.$$

Expressing the equation above in rate of change and dividing by initial GDP leads to:

$$\left. \frac{r^{\star} d\tilde{B}}{Y} \right|_{temp} + \left((1-\alpha_L) \frac{\hat{L}^T}{\hat{\bar{\lambda}}} - (1-\alpha_C)\, \omega_C \frac{\hat{C}^T}{\hat{\bar{\lambda}}} \right) \left. \frac{d\bar{\lambda}}{\bar{\lambda}} \right|_{temp} = 0, \tag{202}$$

where

$$\begin{aligned} & (1-\alpha_L) \frac{\hat{L}^T}{\hat{\bar{\lambda}}} - \frac{\hat{C}^T}{\hat{\bar{\lambda}}} \\ = \; & \frac{(1-\alpha_L)}{\Psi} \left\{ \sigma_L \Psi + \alpha_L \left(\epsilon - \sigma_L \right) \left[\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C \right] \right\} \\ + \; & \frac{(1-\alpha_C)\, \omega_C}{\Psi} \left\{ \sigma_C \Psi + \alpha_C \left(\phi - \sigma_C \right) \left[\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C \right] \right\} \\ = \; & \frac{\Gamma}{\Psi} > 0, \end{aligned} \tag{203}$$

with $\Psi > 0$ given by (156) and $\Gamma > 0$ by (174). Using (203), eq. (202) can be rewritten as follows:

$$\begin{aligned}
\left.\frac{d\bar{\lambda}}{\bar{\lambda}}\right|_{temp} &= -\frac{\Psi}{\Gamma}\left.\frac{r^{\star}d\tilde{B}}{Y_0}\right|_{temp}, \\
&= \frac{\Psi}{\Gamma}\frac{r^{\star}}{\xi + r^{\star}}\Upsilon_G^N\left(1-\Theta'\right), \\
&= \frac{\left[\left(1-\alpha_C\right)\omega_C\alpha_C\left(\phi-\sigma_C\right)+\left(1-\alpha_L\right)\alpha_L\left(\epsilon-\sigma_L\right)\right]}{\Gamma}\frac{r^{\star}}{\xi+r^{\star}}\left(1-\Theta'\right), \quad (204)
\end{aligned}$$

where we have substituted the steady-state change $d\tilde{B}\Big|_{temp}$ given by (201) and Υ_G^N given by(192). Since the marginal utility of wealth increases across all scenarios, we impose from now on the following condition:

$$\left(1-\alpha_C\right)\omega_C\alpha_C\left(\phi-\sigma_C\right)+\left(1-\alpha_L\right)\alpha_L\left(\epsilon-\sigma_L\right) > 0. \quad (205)$$

Importantly, following a temporary fiscal shock, the marginal utility of wealth increases less than after a permanent rise in G^N.

Steady-State Effects

To determine the long-run effects of a temporary fiscal expansion, we approximate the steady-state changes for variable $X = L, C, P, L^T, L^N, B$ with the differentials:

$$\tilde{X} - \tilde{X}_0 \equiv X\left(\bar{\lambda}, G^N\right) - X\left(\lambda_0, G^N\right) = X_{\bar{\lambda}}\mathrm{d}\bar{\lambda}\Big|_{temp}, \quad (206)$$

where $\mathrm{d}\bar{\lambda}\Big|_{temp} \equiv \bar{\lambda} - \lambda_0$ given by eq. (204), and $dG^N = 0$ since government spending is restored to its initial level; note that λ_0 is the initial steady-state value for the shadow value of wealth.

Using the fact that $P = P\left(\bar{\lambda}, G^N\right)$ and because government spending is restored to its initial level, the relative price of non tradables must depreciate in the long-run:

$$\hat{P}\Big|_{temp} = -\frac{\left[\alpha_L\sigma_L + \omega_C\alpha_C\sigma_C\right]}{\Psi}\hat{\bar{\lambda}}\Big|_{temp} < 0, \quad (207)$$

where we made use of (155) and $\hat{\bar{\lambda}}\Big|_{temp}$ is given by (204).

Totally differentiating $L^N = L^N\left(\bar{\lambda}, G^N\right)$ described by eq. (162), using the fact that $dG^N = 0$, and inserting (373) leads to the long-run adjustment of non traded employment following a temporary fiscal expansion:

$$\hat{L}^N\Big|_{temp} = \frac{\omega_C\alpha_C\left\{\sigma_L\left[\left(1-\alpha_C\right)\phi+\alpha_C\sigma_C\right]-\sigma_C\left[\epsilon\left(1-\alpha_L\right)+\sigma_L\alpha_L\right]\right\}}{\Psi}\hat{\bar{\lambda}}\Big|_{temp}. \quad (208)$$

On the one hand, the rise in the marginal utility of wealth has an expansionary effect on labor supply and thus on employment in the non traded sector. On the other hand, by driving down consumption in non tradables, the wealth effect depreciates the relative price of non tradables which lowers the non traded wage and thus exerts a negative impact on L^N.

Totally differentiating $L^T = L^T\left(\bar{\lambda}, G^N\right)$ described by eq. (160), using the fact that $dG^N = 0$, and inserting (373) leads to the long-run adjustment of traded employment following a temporary fiscal expansion:

$$\hat{L}^T\Big|_{temp} = \frac{\sigma_L\alpha_L\epsilon + \omega_C\alpha_C\left\{\sigma_L\left[\left(1-\alpha_C\right)\phi+\alpha_C\sigma_C\right]+\sigma_C\alpha_L\left(\epsilon-\sigma_L\right)\right\}}{\Psi}\hat{\bar{\lambda}}\Big|_{temp}. \quad (209)$$

The combined effect of the rise in the marginal utility of wealth and the depreciation in the relative price of non tradables raises employment in the traded sector. It is worthwhile noticing that (375) is unambiguously positive.

Denoting by NX net exports, differentiating the market clearing condition for the traded good in the long-run, i.e., $r^\star \tilde{B} + \tilde{NX} = 0$ and inserting (201) leads to the steady-state change in net exports expressed in percentage of initial GDP:

$$\frac{d\tilde{NX}|_{temp}}{Y} = -\frac{r^\star d\tilde{B}|_{temp}}{Y} = \frac{r^\star \Upsilon_G^N}{\xi + r^\star}\left(1 - \Theta'\right) > 0, \tag{210}$$

where $\Upsilon_G^N > 0$. In the long-run, a temporary fiscal expansion raises net exports. The reason is that the open economy decumulates traded bonds along the transitional path. To repay its debt, the economy must run a trade surplus.

Consumption unambiguously falls in the long-run:

$$\begin{aligned} \hat{C}\Big|_{temp} &= -\sigma_C \hat{\bar{\lambda}}\Big|_{temp} - \sigma_C \alpha_C \hat{P}\Big|_{temp}, \\ &= -\frac{\sigma_C \hat{\bar{\lambda}}|_{temp}\left\{\alpha_L\left[(1-\alpha_L)\epsilon + \sigma_L(\alpha_L - \alpha_C)\right] + \omega_C \alpha_C (1-\alpha_C)\phi\right\}}{\Psi} < 0, \end{aligned} \tag{211}$$

where the non tradable content of labor, α_L, is higher than the non tradable content of consumption expenditure, α_L, according to our evidence.

Using the fact that $\hat{W} = \alpha_L \hat{W}^N$ and $\hat{P}_C = \alpha_C \hat{P}$, a temporary fiscal expansion raises employment in the long-run:

$$\begin{aligned} \hat{L}\Big|_{temp} &= \sigma_L \hat{\bar{\lambda}}\Big|_{temp} + \sigma_L \alpha_L \hat{P}\Big|_{temp}, \\ &= \frac{\sigma_L\left\{\alpha_L \epsilon (1-\alpha_L) + \omega_C \alpha_C\left[(1-\alpha_C)\phi - \sigma_C(\alpha_L - \alpha_C)\right]\right\}}{\Psi} > 0. \end{aligned} \tag{212}$$

A temporary fiscal expansion unambiguously lowers the real consumption wage in the long-run:

$$\mathrm{d}\left(\frac{W}{P_C}\right)|_{temp} = \frac{W}{P_C}\left(\alpha_L - \alpha_C\right)\hat{P}\big|_{temp} < 0. \tag{213}$$

Since data indicate that $\alpha_L > \alpha_C$, the long-run depreciation in the relative price of non tradables drives down the real consumption wage.

Initial Responses of Sectoral Variables

To determine the initial reaction of selected variables, we linearize the short-run static solution of variable $X(t)$, i.e., $X(t) = X\left(\bar{\lambda}, G^N(t)\right)$, in the neighborhood of the steady-state:

$$X(t) - \tilde{X} = X_{G^N}\left(G^N(t) - \tilde{G}^N\right), \tag{214}$$

and evaluate its initial reaction relative to its initial steady-state value:

$$dX(0) \equiv X(0) - \tilde{X}_0 = \tilde{X} - \tilde{X}_0 + X_{G^N} dG^N(0). \tag{215}$$

Because a temporary fiscal expansion has long-run effects, variables are affected by (indirectly) the change in the shadow value of wealth $\bar{\lambda}$, as captured by $\tilde{X} - \tilde{X}_0$, and directly by the change in government spending G^N, as captured by $dG^N(0)$.

Since we are interested in responses of key macroeconomic variables in the short-run, we analyze the reactions of macroeconomic variables on impact. We first explore the response of the price of non traded goods in terms of traded goods. Evaluating (155) at time $t = 0$ yields the initial response of the relative price of non tradables:

$$\begin{aligned} \hat{P}(0)\big|_{temp} &= -\frac{\left[\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C\right]}{\Psi}\hat{\bar{\lambda}}\Big|_{temp} + \frac{1}{\Psi}\frac{P\mathrm{d}G^N(0)}{Y}, \\ &= -\frac{\left[\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C\right]}{\Psi}\hat{\bar{\lambda}}\Big|_{temp} + \frac{g}{\Psi} > \hat{P}(0)\big|_{perm} > 0, \end{aligned} \tag{216}$$

where $\Psi > 0$ and we used the fact that:

$$\frac{PdG^N(0)}{Y} = \frac{dG(0)}{Y} = 1 - (1 - g) = g > 0. \tag{217}$$

Because the rise in the marginal utility of wealth is smaller after a temporary fiscal shock than after a permanent rise in G^N, i.e., $0 < \hat{\bar{\lambda}}\big|_{temp} < \hat{\bar{\lambda}}\big|_{perm}$, P increases more on impact after a temporary shock than after a permanent shock. Intuitively, as the wealth effect is smaller when the fiscal shock is temporary, consumption in non tradables falls less which in turn triggers a larger excess demand in the non traded goods market, thus causing the relative price of non tradables to appreciate more.

Using the fact that $\mathrm{d}L^N(t) = L^N(t) - \tilde{L}^N_0 = L^N\left(\bar{\lambda}, G^N(t)\right) - L^N\left(\lambda_0, G^N_0\right)$ with $dG(t) = G(t) - G^N_0 = 0$ and totally differentiating the short-run solution for non traded labor described by eq. (162), one obtains the initial response of non traded labor following an exogenous increase in government consumption:

$$\hat{L}^N(0)\Big|_{temp} = \frac{\partial L^N}{\partial \bar{\lambda}} \frac{\bar{\lambda}}{\tilde{L}^N} \hat{\bar{\lambda}}\Big|_{temp} + L^N_{G^N} dG^N(0) > 0. \tag{218}$$

While $L^N_{G^N} > 0$, the sign of $L^N_{\bar{\lambda}}$ can be positive or negative. If $L^N_{\bar{\lambda}} < 0$, because the marginal utility of wealth increases less after a temporary rise in G^N than after a permanent increase in G^N, the negative impact on L^N produced by the wealth effect (which reduces C^N) is smaller. Remembering that L^N rises after a permanent fiscal shock, we can infer from this that non traded labor increases more following a temporary fiscal shock. If $L^N_{\bar{\lambda}} > 0$, non traded labor increases less after a temporary shock than after a permanent shock.

Using (161), the change in non traded labor in the short-run following a temporary fiscal shock can be written as follows:

$$\begin{aligned}
\hat{L}^N(0)\Big|_{temp} &= \hat{\bar{\lambda}}\Big|_{temp} \left\{ \frac{\omega_C \alpha_C \left\{\sigma_L \left[(1-\alpha_C)\phi + \alpha_C \sigma_C\right] - \sigma_C \left[\epsilon(1-\alpha_L) + \sigma_L \alpha_L\right]\right\}}{\Psi} \right\} \\
&+ \frac{\left[\epsilon(1-\alpha_L) + \sigma_L \alpha_L\right]}{\Psi} \frac{P \mathrm{d}G^N}{Y}.
\end{aligned} \tag{219}$$

Because $\hat{L}^N = \sigma_L \hat{\lambda}\big|_{temp} + \left[\epsilon(1-\alpha_L) + \alpha_L \sigma_L\right] \hat{P}\big|_{temp}$ where $\hat{\lambda}\big|_{temp} > 0$ (see eq. (193)) together with condition (205)) and $\hat{P}\big|_{temp} > 0$ (see eq. (216)), non traded labor unambiguously increases on impact after a temporary rise in G^N. Intuitively, the negative wealth effect induces households to supply more labor while the appreciation in the relative price of non tradables pushes up the non traded wage W^N which encourages workers to shift hours worked toward the non traded sector.

Totally differentiating $L^T = L^T\left(\bar{\lambda}, P\right)$ and inserting the solution for the relative price given by (158), the initial reaction of L^T following a temporary fiscal expansion can be written as follows:

$$\begin{aligned}
\hat{L}^T(0)\Big|_{temp} &= \sigma_L \hat{\lambda}\Big|_{temp} + \alpha_L (\sigma_L - \epsilon) \hat{P}\Big|_{temp}, \\
&= \frac{\Psi \sigma_L + \alpha_L(\epsilon - \sigma_L)\left[\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C\right]}{\Psi} \hat{\lambda}\Big|_{temp} - \frac{\alpha_L(\epsilon - \sigma_L) g}{\Psi} \lesseqgtr 0,
\end{aligned} \tag{220}$$

where $\Psi > 0$ (see eq. (156)), $\hat{\bar{\lambda}}\big|_{temp} > 0$ is given by (204), and we used the fact that $\frac{P dG^N(0)}{Y} = g$ (see eq. (217)) to determine (197). Using the fact that $\hat{L}^T = \sigma_L \hat{\lambda}\big|_{temp} + \alpha_L(\sigma_L - \epsilon) \hat{P}\big|_{temp}$, because both the shadow value of wealth $\bar{\lambda}$ and the relative price of non tradables P increase, we find that a rise in G^N raises L^T if $\sigma_L > \epsilon$, i.e., if labor is weakly mobile across sectors. Conversely, setting assumption 1, i.e., $\sigma_L < \epsilon$, traded labor falls because the cost of shifting hours worked from one sector to another is low enough.

Differentiating the short-run change in the real consumption wage, and using the fact that $\hat{W}^T = 0$, $\hat{W} = \alpha_L \hat{W}^N$ and $\hat{P}_C = \alpha_C \hat{P}$, yields:

$$\mathrm{d}\left(\frac{W}{P_C}\right)(0)\big|_{temp} = \frac{W}{P_C}(\alpha_L - \alpha_C)\hat{P}(0)\big|_{temp} > 0. \tag{221}$$

Because P appreciates more after a temporary fiscal shock, the real consumption aggregate wage will increase by a larger amount than after a permanent fiscal shock.

E.11 Steady-State Effects of a Temporary Government Spending Shock: Graphical Apparatus

We characterize the equilibrium graphically which allows us to build up intuition on the long-run effects of a temporary rise in G^N. Because we focus on steady-state, we omit the tilde below for simplicity purposes when it does not cause confusion.

E.11.1 The Initial Steady-State

We denote by $NX = Y^T - C^T - G^T$ net exports. Hence, in the long-run, we have $r^\star B = -NX$. Dividing both sides by Y^T, we have: $\upsilon_B = -\upsilon_{NX}$. The initial equilibrium is thus defined by the following set of equations:

$$\left(\frac{1-\varphi}{\varphi}\right)\frac{C^T}{C^N} = P^{\phi}, \tag{222a}$$

$$\left(\frac{1-\vartheta}{\vartheta}\right)\frac{L^T}{L^N} = \Omega^{-\epsilon} \tag{222b}$$

$$P = \Omega, \tag{222c}$$

$$\frac{Y^T\left(1-\upsilon_{NX}-\upsilon_{G^T}\right)}{Y^N\left(1-\upsilon_{G^N}\right)} = \frac{C^T}{C^N}, \tag{222d}$$

where $Y^T = L^T$, $Y^N = L^N$, $\Omega \equiv W^N/W^T$ is the ratio of the non traded wage to the traded wage ratio or the relative wage, and we denote by $\upsilon_{NX} \equiv NX/Y^T$ the ratio of net exports to traded output, and $\upsilon_{G^j} \equiv G^j/Y^j$ the ratio of government spending on good $j = T, N$ to output of sector $j = T, N$.

E.11.2 Graphical Apparatus

To build up intuition, we characterize the equilibrium graphically. We denote the logarithm of variables with lower-case letters. The steady state can be described by considering alternatively the goods market or the labor market.

Goods Market Equilibrium- and Labor Market Equilibrium-Schedules

The steady-state (222) can be summarized graphically in Figure 52 that traces out two schedules in the $(y^T - y^N, p)$-space. System (222a)-(222d) described above can be reduced to two equations. Substituting (222a) into eq. (222d) yields the goods market equilibrium (henceforth labelled GME) schedule:

$$\left(y^T - y^N\right)\Big|^{GME} = \phi p + \ln\left(\frac{1-\upsilon_{G^N}}{1-\upsilon_{NX}-\upsilon_{G^T}}\right) + x, \tag{223}$$

where $x = \ln\left(\frac{\varphi}{1-\varphi}\right)$. Since a rise in the relative price p raises consumption in tradables, the goods market equilibrium requires a rise in the traded output relative to non traded output. Hence the goods market equilibrium is upward-sloping in the $(y^T - y^N, p)$-space where the slope is equal to $1/\phi$.

Substituting (222b) into (222c) to eliminate ω yields the labor market equilibrium (henceforth LME) schedule:

$$\left(y^T - y^N\right)\Big|^{LME} = -\epsilon p + z, \tag{224}$$

where $z = \ln\left(\frac{\vartheta}{1-\vartheta}\right)$. A rise in the relative price p increases the relative wage ω which encourages agents to supply more labor in the non traded sector, and all the more so as the values of ϵ are higher. Hence the labor market equilibrium is downward-sloping in the $(y^T - y^N, p)$-space where the slope is equal to $-1/\epsilon$. Assuming that the shift of labor across sectors is costless, i.e., if we let ϵ tend toward infinity, wages are equalized across sectors. Graphically, the LME-schedule becomes a horizontal line. Conversely, as long as switching hours worked from one sector to another is costly, i.e., if ϵ takes finite values, the LME-schedule is negatively related to the relative price of non tradables in the $(y^T - y^N, p)$-space.

Labor Demand- and Labor Supply-Schedules

The steady-state (222) can be summarized graphically by focusing alternatively on the labor market. Eq. (222b) describes the labor supply-schedule (LS henceforth) in the $(l^T - l^N, \omega)$-space. Taking logarithm yields:

$$\left(l^T - l^N\right)\Big|^{LS} = -\epsilon\omega + z, \tag{225}$$

where $z = \ln\left(\frac{\vartheta}{1-\vartheta}\right)$. A rise in the non traded wage-traded wage ratio ω provides an incentive to shift labor supply from the traded sector towards the non traded sector. Hence the LS-schedule is downward-sloping in the $(l^T - l^N, \omega)$-space where the slope is equal to $-1/\epsilon$.

Inserting demand for traded goods in terms of non traded goods (222a) into the market clearing condition given by (222d) yields:

$$\frac{\tilde{Y}^T}{\tilde{Y}^N} = \left(\frac{\varphi}{1-\varphi}\right) P^{\phi} \left(\frac{1 - \upsilon_{G^N}}{1 - \upsilon_{NX} - \upsilon_{G^T}}\right). \tag{226}$$

Substituting first-order conditions from the firms' maximization problem and using production functions, i.e. $L^T = Y^T$ and $L^N = Y^N$, we get:

$$\frac{L^T}{L^N} = \left(\frac{\varphi}{1-\varphi}\right) \Omega^{\phi} \left(\frac{1 - \upsilon_{G^N}}{1 - \upsilon_{NX} - \upsilon_{G^T}}\right).$$

Taking logarithm yields the labor demand-schedule (LD henceforth) in the $(l^T - l^N, \omega)$-space is given by

$$\left(l^T - l^N\right)\Big|^{LD} = \phi\omega + \ln\left(\frac{1 - \upsilon_{G^N}}{1 - \upsilon_{NX} - \upsilon_{G^T}}\right) + x, \tag{227}$$

where $x = \ln\left(\frac{\varphi}{1-\varphi}\right)$. A rise in the relative wage ω raises the cost of labor in the non traded sector relative to the traded sector. To compensate for the increased labor cost, non traded firms charge prices which encourage agents to substitute traded for non traded goods and therefore produces an expansionary effect on labor demand in the traded sector. Hence the LD-schedule is upward-sloping in the $(l^T - l^N, \omega)$-space where the slope is equal to $1/\phi$.

In order to facilitate the interpretation of analytical results, it is useful to rewrite $\ln\left(\frac{1-\upsilon_{G^N}}{1+\upsilon_B - \upsilon_{G^T}}\right)$ by using a first-order Taylor approximation which implies:

$$\ln\left(1 - \upsilon_{NX} - \upsilon_{G^T}\right) - \ln\left(1 - \upsilon_{G^N}\right) \simeq -\upsilon_{NX} - \upsilon_{G^T} + \upsilon_{G^N}. \tag{228}$$

E.11.3 Long-Run Adjustments in the Relative Price and Relative Wage

We now analyze graphically and analytically the consequences on the relative price and the relative wage of a temporary increase in G^N. The initial long-run equilibrium is represented at E_0 in Figure 52. The long-run equilibrium is defined by the the system of equations (222).

Equating (223) and (224), differentiating and denoting by a hat the deviation in percentage from initial steady state, one obtains the long-run adjustment in the relative price of non tradables to an exogenous temporary rise in government consumption on non tradables:

$$\hat{p} = -\frac{\mathrm{d}\upsilon_{NX}}{\phi + \epsilon} < 0, \tag{229}$$

where we made use of the approximation given by (228) and $\mathrm{d}\upsilon_{NX} \equiv \frac{r^\star NX_1}{Y_1^T} - \frac{r^\star NX_0}{Y_0^T} > 0$ and $\mathrm{d}\upsilon_{G^N} = 0$. By raising net exports and thus the demand for tradables in the long-run, a temporary increase in government spending depreciates the relative price of non tradables.

Equating (225) and (227), differentiating and denoting by a hat the deviation from initial steady state in percentage terms, one obtains the long-run adjustment in the relative wage to an exogenous temporary rise in government consumption on non tradables:

$$\hat{\omega} = -\frac{\mathrm{d}\upsilon_{NX}}{\phi + \epsilon} < 0, \tag{230}$$

where we made use of the approximation given by (228); by raising net exports in the long-run, a rise in G^N shifts the LD-schedule to the right in the $(l^T - l^N, \omega)$-space and thus a temporary rise in G^N permanently lowers the non traded wage relative to the traded wage.

E.12 Solving the Model with Perfect Mobility of Labor across Sectors

In this subsection, we provide analytical results when assuming perfect mobility of labor across sectors. If we let ϵ tend toward infinity into eq. (120), hours worked across sectors become perfect substitutes:

$$L = L^T + L^N. \tag{231}$$

Because workers no longer experience a cost when shifting from one sector to another, hours worked in the traded and the non traded sector are perfect substitutes. Since workers are willing to devote their whole time to the sector that pays the highest wages, firms in both sectors must pay the same wage. Hence, $1 = W^T = W^N$. The wage equalization across sectors implies that $P = 1$. As a result, the relative price of non tradables remains unaffected by a government spending shock.

Inserting short-run static solutions for C^N given by (143) into the non-traded good market clearing condition gives us:

$$L^N = C^N\left(\bar{\lambda}, P\right) + G^N. \tag{232}$$

The non-traded good market clearing condition can be solved for non traded labor

$$L^N = L^N\left(\bar{\lambda}, G^N\right), \tag{233}$$

where partial derivatives are obtained by totally differentiating (232):

$$\hat{L}^N = -\frac{\omega_C \alpha_C \sigma_C}{\alpha_L}\hat{\bar{\lambda}} + \frac{1}{\alpha_L}\frac{P\mathrm{d}G^N}{Y}, \tag{234}$$

with the ratio of consumption expenditure to GDP denoted by $\omega_C = \frac{P_C C}{Y}$, and the non tradable content of GDP denoted by $\alpha_L = \frac{PY^N}{Y} = \frac{L^N}{L}$.

Inserting the short-run static solution for non traded labor (233) and the short-run static solution for aggregate labor supply given by

$$L = L\left(\bar{\lambda}\right), \quad \hat{L} = \sigma_L \hat{\bar{\lambda}}, \tag{235}$$

the resource constraint for labor given by (231) can be solved for traded labor:

$$L^T = L^T\left(\bar{\lambda}, G^N\right), \tag{236}$$

where partial derivatives are obtained by totally differentiating the resource constraint for labor given by (231):

$$\left(1-\alpha_L\right)\hat{L}^T = \sigma_L \hat{\bar{\lambda}} - \alpha_L \hat{L}^N.$$

Inserting the solution for non traded labor expressed in rate of change (234) allows us to solve for traded labor:

$$\left(1-\alpha_L\right)\hat{L}^T = \left(\sigma_L + \omega_C \alpha_C \sigma_C\right)\hat{\bar{\lambda}} - \frac{P\mathrm{d}G^N}{Y}. \tag{237}$$

Effects of a Permanent Rise in Government Spending

Inserting (236) into the current account equation, linearizing and solving yields the intertemporal solvency condition (ISC):

$$\tilde{B} = B_0. \tag{238}$$

Inserting the ISC (238) and appropriate short-run static solutions which obviously hold in the long-run, the steady-state can be reduced to one equation:

$$r^\star B_0 + L^T\left(\bar{\lambda}, G^N\right) - C^T\left(\bar{\lambda}, P\right) - G^T = 0, \tag{239}$$

where P remains constant. Equation (239) can be solved for the marginal utility of wealth:

$$\bar{\lambda} = \lambda\left(G^N, G^T\right). \tag{240}$$

Note that we concentrate below on a rise in government spending on non tradables G^N because empirical evidence indicate that the non-tradable content of public spending averages to 90% for OECD countries. Using the fact that the stock of traded bonds is initially predetermined and totally differentiating (239) yields:

$$\left(1-\alpha_L\right)\hat{L}^T = \omega_C\left(1-\alpha_C\right)\hat{C}^T + \frac{\mathrm{d}G^T}{Y}.$$

Inserting (237) and using the fact that P remains unaffected by a fiscal expansion, the change in the equilibrium value of the marginal utility of wealth is:

$$\hat{\bar{\lambda}} = \frac{\frac{P\mathrm{d}G^N}{Y} + \frac{\mathrm{d}G^T}{Y}}{\sigma_L + \omega_C\sigma_C}. \tag{241}$$

Inserting (241) into (234) yields the change in non traded labor following a permanent fiscal expansion:

$$\hat{L}^N = \frac{\sigma_L + \omega_C\sigma_C\left(1-\alpha_C\right)}{\alpha_L\left(\sigma_L+\omega_C\sigma_C\right)}\frac{P\mathrm{d}G^N}{Y} - \frac{\omega_C\alpha_C\sigma_C}{\alpha_L\left(\sigma_L+\omega_C\sigma_C\right)}\frac{\mathrm{d}G^T}{Y}. \tag{242}$$

Inserting (241) into (237) yields the change in traded labor following a permanent fiscal expansion:

$$\hat{L}^T = -\frac{\omega_C\left(1-\alpha_C\right)\sigma_C}{\left(1-\alpha_L\right)\left(\sigma_L+\omega_C\sigma_C\right)}\frac{P\mathrm{d}G^N}{Y} + \frac{\sigma_L+\omega_C\sigma_C\alpha_C}{\left(1-\alpha_L\right)\left(\sigma_L+\omega_C\sigma_C\right)}\frac{\mathrm{d}G^T}{Y}. \tag{243}$$

According to (242) and (243), a permanent fiscal expansion raises non traded labor and lowers traded labor, while wages, the relative price, and the net foreign asset position remain unchanged.

Effects of a Temporary Rise in Government Spending

Inserting first the short-run static solutions for traded labor (236) and consumption in tradables (143) into the market clearing condition for the traded good (152) yields:

$$\dot{B}(t) = r^\star B(t) + L^T\left(\bar{\lambda}, G^N(t)\right) - C^T\left(\bar{\lambda}, P\right) - G^T. \tag{244}$$

Linearizing the current account equation above around the steady-state gives us:

$$\dot{B}(t) = r^\star\left(B(t) - \tilde{B}\right) + L^T_{G^N}\left(G^N(t) - \tilde{G}^N\right). \tag{245}$$

Inserting $L^T_{G^N} = -\frac{\tilde{L}^T}{1-\alpha_L}\frac{\tilde{P}}{\tilde{Y}} = -\tilde{P}$ (see eq. (237)), eq. (245) can be rewritten as follows:

$$\dot{B}(t) = r^\star\left(B(t) - \tilde{B}\right) - \left(G(t) - \tilde{G}\right), \tag{246}$$

where we used the fact that $dG^N(t) = \frac{dG(t)}{\tilde{P}}$ since the relative price of non tradables remains constant over time as P must stick to the marginal product of labor (that reduces to 1).

Inserting the law of motion of government spending given by (186), eq. (246) can be rewritten as follows:

$$\dot{B}(t) = r^\star\left(B(t) - \tilde{B}\right) - Y\left[e^{-\xi t} - (1-g)\,e^{-\chi t}\right]. \tag{247}$$

Pre-multiplying by $e^{-r^\star\tau}$ and integrating over $(0,t)$ allow us to obtain the general solution for $B(t)$:

$$B(t) - \tilde{B} = \left[\left(B_0 - \tilde{B}\right) - \frac{Y}{\xi + r^\star}\left(1-\Theta'\right)\right]e^{r^\star t} + \frac{Y}{\xi+r^\star}\left(e^{-\xi t} - \Theta' e^{-\chi t}\right), \tag{248}$$

where we used the fact that $\int_0^t e^{-(\xi+r^\star)\tau}d\tau = \frac{\left(1-e^{-(\xi+r^\star)t}\right)}{\xi+r^\star}$ and we set:

$$\Theta' = (1-g)\,\frac{\xi+r^\star}{\chi+r^\star} > 0. \tag{249}$$

Invoking the transversality condition, one obtains the 'stable' solution for the stock of foreign assets so that $B(t)$ converges toward its steady-state value $\tilde{B}$:

$$B(t) - \tilde{B} = \frac{Y}{\xi + r^\star} \left(e^{-\xi t} - \Theta' e^{-\chi t} \right). \tag{250}$$

Eq. (250) gives the trajectory for for $B(t)$ consistent with the intertemporal solvency condition:

$$\left(\tilde{B} - B_0 \right) = -\frac{Y}{\xi + r^\star} \left(1 - \Theta' \right), \tag{251}$$

where $1 - \Theta' > 0$ due to inequality (187). According to (251), a temporary rise in government spending deteriorates the net foreign asset position, i.e., $d\tilde{B} < 0$.

Differentiating (250) w.r.t. time leads to the trajectory for the current account along the transitional path when government spending follows the temporal path given by eq. (186):

$$\dot{B}(t) = -\frac{Y}{\xi + r^\star} \left(\xi e^{-\xi t} - \chi \Theta' e^{-\chi t} \right). \tag{252}$$

According to (252), the net foreign asset position deteriorates monotonically since $\left(\xi e^{-\xi t} - \chi \Theta' e^{-\chi t} \right) > 0$ for $t \geq 0$.

Evaluating (252) at time $t = 0$ leads to the initial current account response, expressed as a percentage of initial GDP, following a temporary rise in government spending:

$$\frac{\dot{B}(0)}{Y} = -\left(\frac{\xi - \chi \Theta'}{\xi + r^\star} \right) < 0, \tag{253}$$

where $(\xi - \chi \Theta') > 0$.

The Change in the Equilibrium Value of the Marginal Utility of Wealth

Eq. (251) allows us to calculate the steady-state change in the foreign asset position following a temporary rise in government spending:

$$d\tilde{B}\Big|_{temp} = -\frac{Y}{\xi + r^\star} \left(1 - \Theta' \right). \tag{254}$$

To determine the change in the equilibrium value of the marginal utility of wealth, we have to differentiate the market clearing condition for traded goods:

$$r^\star d\tilde{B}\Big|_{temp} + \left(L^T_\lambda - C^T_\lambda \right) d\bar{\lambda}\Big|_{temp} = 0.$$

Expressing the equation above in rate of change and dividing by initial GDP leads to:

$$\frac{r^\star d\tilde{B}}{Y}\Big|_{temp} + \left((1 - \alpha_L) \frac{\hat{L}^T}{\hat{\bar{\lambda}}} - (1 - \alpha_C) \omega_C \frac{\hat{C}^T}{\hat{\bar{\lambda}}} \right) \frac{d\bar{\lambda}}{\bar{\lambda}}\Big|_{temp} = 0, \tag{255}$$

where

$$(1 - \alpha_L) \frac{\hat{L}^T}{\hat{\bar{\lambda}}} - (1 - \alpha_C) \omega_C \frac{\hat{C}^T}{\hat{\bar{\lambda}}} = \sigma_L + \omega_C \sigma_C. \tag{256}$$

Inserting (254) and (256), eq. (255) can be solved for the change in the equilibrium value of the marginal utility of wealth:

$$\begin{aligned} \frac{d\bar{\lambda}}{\bar{\lambda}}\Big|_{temp} &= -\frac{1}{\sigma_L + \omega_C \sigma_C} \frac{r^\star d\tilde{B}}{Y_0}\Big|_{temp}, \\ &= \frac{1}{\sigma_L + \omega_C \sigma_C} \frac{r^\star}{\xi + r^\star} \left(1 - \Theta' \right). \end{aligned} \tag{257}$$

Following a temporary fiscal shock, the marginal utility of wealth increases less than after a permanent rise in G^N.

E.13 A Friendly Way to Solve the Model with Imperfect Mobility of Labor

In this subsection, we solve analytically the model with imperfect mobility of labor across sectors by keeping our assumption according to which the government spending shock is fully biased toward non tradables. We relax this assumption in subsection E.19 where we consider a government spending shock which is split between non tradables and tradables. We simplify the government spending shock by assuming that the endogenous response of government spending to an exogenous fiscal shock is governed by the following dynamic equation:

$$dG(t) = \tilde{Y} g e^{-\xi t}. \tag{258}$$

According to (258), government spending rises initially by $g > 0$ percentage points of GDP and declines monotonically at rate $\xi > 0$. The latter feature simplifies substantially analytical expressions.

The short-run equilibrium can be rewritten as follows:

$$C = \left(P_C \bar{\lambda}\right)^{-\sigma_C}, \tag{259a}$$

$$L = \left(\bar{\lambda} W\right)^{\sigma_L}, \tag{259b}$$

$$L^N = \alpha_L \frac{W}{W^N} L, \tag{259c}$$

$$L^T = \left(1 - \alpha_L\right) \frac{W}{W^T} L, \tag{259d}$$

$$C^N = \alpha_C \frac{P_C}{P} C, \tag{259e}$$

$$C^T = \left(1 - \alpha_C\right) P_C C, \tag{259f}$$

$$W^T = 1, \tag{259g}$$

$$W^N = P, \tag{259h}$$

$$Y^N = C^N + G^N, \tag{259i}$$

$$\dot{B} = r^\star B + Y^T - C^T - G^T, \tag{259j}$$

where $Y^N = L^N$, $Y^T = L^T$, α_C is given by eq. (130a) and α_L is given by eq. (136a).

Short-Run Solutions

Substituting first (259a) into (259e), (259b) and (259h) into (259c), the market clearing condition (259i) for the non traded good can be rewritten as follows:

$$\frac{\alpha_L \bar{\lambda}^{\sigma_L} W^{1+\sigma_L}}{P} = \frac{\alpha_C P_C^{1-\sigma_C} \bar{\lambda}^{-\sigma_C}}{P} + G^N. \tag{260}$$

As will be useful later, we compute the change in percentage of the shares of non tradables and tradables into consumption and labor. Totally differentiating (130a)-(131), and (136a)-(136b) yields:

$$\hat{\alpha}_C = \left(1 - \phi\right)\left(1 - \alpha_C\right) \hat{P}, \tag{261a}$$

$$\left(1 - \hat{\alpha_C}\right) = \left(\phi - 1\right) \alpha_C \hat{P}, \tag{261b}$$

$$\hat{\alpha}_L = \left(\epsilon + 1\right)\left(1 - \alpha_L\right) \hat{P}, \tag{261c}$$

$$\left(1 - \hat{\alpha_L}\right) = -\left(\epsilon + 1\right) \alpha_L \hat{P}, \tag{261d}$$

where we used the fact that $\hat{P}_C = \alpha_C \hat{P}$ (since $P^T = 1$), and $\hat{W} = \alpha_L \hat{P}$ (since $W^T = P^T = 1$ and $W^N = P$).

Totally differentiating (260), using (261a) et (261c), leads to:

$$\hat{\alpha}_L + \sigma_L \hat{\bar{\lambda}} + \left(1 + \sigma_L\right) \hat{W} - \hat{P} = \frac{C^N}{L^N} \left[\hat{\alpha}_C + \left(1 - \sigma_C\right) \hat{P}_C - \sigma_C \hat{\bar{\lambda}} - \hat{P}\right] + \frac{dG^N}{L^N},$$

$$\frac{PL^N}{Y} \left[\hat{\alpha}_L + \sigma_L \hat{\bar{\lambda}} + \left(1 + \sigma_L\right) \hat{W} - \hat{P}\right] = \frac{PC^N}{Y} \left[\hat{\alpha}_C + \left(1 - \sigma_C\right) \hat{P}_C - \sigma_C \hat{\bar{\lambda}} - \hat{P}\right] + \frac{PdG^N}{Y},$$

$$\alpha_L \left\{\left(1 + \epsilon\right)\left(1 - \alpha_L\right) \hat{P} + \left[\left(1 + \sigma_L\right) \alpha_L - 1\right] \hat{P} + \sigma_L \hat{\bar{\lambda}}\right\}$$

$$= \alpha_C \omega_C \left\{\left(1 - \phi\right)\left(1 - \alpha_C\right) \hat{P} + \left[\left(1 - \sigma_C\right) \alpha_C - 1\right] \hat{P} - \sigma_C \hat{\bar{\lambda}}\right\} + \frac{PdG^N}{Y},$$

where $\omega_C = \frac{P_C C}{Y}$, $\frac{PC^N}{P_C C} = \alpha_C$, $\frac{PL^N}{Y} = \frac{W^N L^N}{WL} = \alpha_L$. Collecting terms, the deviation in percentage from the initial steady-state for the relative price of non tradables is described by:

$$\hat{P} = \frac{-\left[\alpha_L \sigma_L + \alpha_C \omega_C \sigma_C\right]}{\Psi} \hat{\bar{\lambda}} + \frac{1}{\Psi} \frac{PdG^N}{Y}, \tag{262}$$

where Ψ is given (157).

Totally differentiating (259b) and using the fact that $\hat{W} = \alpha_L \hat{W}^N + (1 - \alpha_L) \hat{W}^T$ with $\hat{W}^N = \hat{P}$ and $\hat{W}^T = 0$ leads to the response of employment in percentage deviation from initial steady-state:

$$\hat{L} = \sigma_L \hat{\bar{\lambda}} + \sigma_L \alpha_L \hat{P}. \tag{263}$$

Substituting (259c) and (259h) into (259c) leads to $L^T = (1 - \alpha_L)(W)^{1+\sigma_L} \left(\bar{\lambda}\right)^{\sigma_L}$. Totally differentiating and using the fact that $\widehat{(1 - \alpha_L)} = -(1 + \epsilon) \hat{W}$ with $\hat{W} = \alpha_L \hat{P}$, one obtains:

$$\begin{aligned} \hat{L}^T &= -(\epsilon - \sigma_L) \alpha_L \hat{P} + \sigma_L \hat{\bar{\lambda}}, \\ &= \left\{ \frac{\sigma_L \Psi + \alpha_L (\epsilon - \sigma_L) \left[\alpha_L \sigma_L + \alpha_C \omega_C \sigma_C\right]}{\Psi} \right\} \hat{\bar{\lambda}} - \frac{\alpha_L (\epsilon - \sigma_L)}{\Psi} \frac{PdG^N}{Y}. \end{aligned} \tag{264}$$

Substituting (259b) and (259h) into (259d) leads to $L^N = \frac{\alpha_L}{P}(W)^{1+\sigma_L} \bar{\lambda}^{\sigma_L}$. Totally differentiating yields:

$$\begin{aligned} \hat{L}^N &= \left[(1 + \epsilon)(1 - \alpha_L) + (1 + \sigma_L) \alpha_L - 1\right] \hat{P} + \sigma_L \hat{\bar{\lambda}}, \\ &= \left[\epsilon (1 - \alpha_L) + \alpha_L \sigma_L\right] \hat{P} + \sigma_L \hat{\bar{\lambda}}, \\ &= \left\{ \frac{\sigma_L \Psi - \left[\epsilon (1 - \alpha_L) + \alpha_L \sigma_L\right] \left[\alpha_L \sigma_L + \alpha_C \omega_C \sigma_C\right]}{\Psi} \right\} \hat{\bar{\lambda}} \\ &+ \frac{\left[\epsilon (1 - \alpha_L) + \alpha_L \sigma_L\right]}{\Psi} \frac{PdG^N}{Y}. \end{aligned} \tag{265}$$

Solution for the Net Foreign Asset Position

Substituting $L^T = (1 - \alpha_L)(W)^{1+\sigma_L} \left(\bar{\lambda}\right)^{\sigma_L}$ and $C^T = (1 - \alpha_C) P_C^{1-\sigma_C} \bar{\lambda}^{-\sigma_C}$ into (259j) leads to:

$$\dot{B}(t) = r^\star B(t) + (1 - \alpha_L(t)) W(t)^{1+\sigma_L} \bar{\lambda}^{\sigma_L} - (1 - \alpha_C(t)) P_C(t)^{1-\sigma_C} \bar{\lambda}^{-\sigma_C} - G^T. \tag{266}$$

Using the fact that both $\bar{\lambda}$ and G^T are constant over time, linearizing (266) in the neighborhood of the steady-state yields:

$$\begin{aligned} \dot{B}(t) &= r^\star dB(t) - \tilde{L}^T \frac{\alpha_L (\epsilon - \sigma_L)}{\Psi} \frac{\tilde{P} dG^N(t)}{\tilde{Y}} - \tilde{C}^T \frac{\alpha_C (\phi - \sigma_C)}{\Psi} \frac{\tilde{P} dG^N(t)}{\tilde{Y}}, \\ &= r^\star dB(t) - \tilde{Y} \Upsilon_G^N g e^{-\xi t}. \end{aligned}$$

where $\frac{\partial \dot{B}(t)}{\partial G(t)} = -\Upsilon_G^N = -\frac{\left[(1-\alpha_L)\alpha_L(\epsilon - \sigma_L) + (1-\alpha_C)\omega_C \alpha_C (\phi - \sigma_C)\right]}{\Psi} < 0$ is given by eq. (192). Substituting the law of motion of government spending (258) and solving leads to the general solution for the net foreign asset position:

$$B(t) - \tilde{B} = \left[\left(B_0 - \tilde{B}\right) - \frac{\Upsilon_G^N \tilde{Y}}{\xi + r^\star} g\right] e^{r^\star t} + \frac{\Upsilon_G^N \tilde{Y}}{\xi + r^\star} g e^{-\xi t}. \tag{267}$$

Invoking the transversality condition gives the solution for $B(t)$:

$$B(t) - \tilde{B} = \frac{\Upsilon_G^N \tilde{Y}}{\xi + r^\star} g e^{-\xi t}, \tag{268}$$

consistent with the intertemporal solvency condition

$$\left(\tilde{B} - B_0\right) = -\frac{\Upsilon_G^N \tilde{Y}}{\xi + r^\star} g. \tag{269}$$

To determine the change in the equilibrium value of the marginal utility of wealth, we have to differentiate the market clearing condition (266) for the traded good evaluated at the steady-state (i.e., $\dot{B}(t) = 0$), using the fact that in the long-run government spending reverts to its initial level (i.e., $dG^N = 0$):

$$r^\star \frac{d\tilde{B}}{\tilde{Y}} + (1-\alpha_L)\,\hat{\tilde{L}}^T = (1-\alpha_C)\,\omega_C \hat{\tilde{C}}^T,$$

$$\hat{\tilde{\lambda}} = -\frac{\Psi}{\Gamma} r^\star \frac{d\tilde{B}}{\tilde{Y}},$$

where $\Gamma > 0$ is given by eq. (174). Substituting (269) into the above equation leads to the change in the equilibrium value of the marginal utility of wealth:

$$\hat{\tilde{\lambda}} = \frac{\Psi}{\Gamma} \frac{r^\star}{\xi + r^\star} \Upsilon_G^N g > 0, \tag{270}$$

where $\Gamma > 0$, $\Psi > 0$, $\Upsilon_G^N > 0$, $\xi > 0$, and $g > 0$.

Before evaluating the short-run effects of the fiscal shock, it is useful to rewrite Γ given by eq. (174) as follows:

$$\begin{aligned} \Gamma &= \Psi \left\{ \left[(1-\alpha_L)\,\sigma_L + \omega_C\,(1-\alpha_C)\,\sigma_C\right] + \left[\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C\right] \Upsilon_G^N \right\}, \quad (271)\\ &> \left[\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C\right] \Upsilon_G^N \Psi, \end{aligned}$$

where we used the fact that $\Upsilon_G^N \Psi = \left[(1-\alpha_L)\,\alpha_L\,(\epsilon - \sigma_L) + (1-\alpha_C)\,\omega_C \alpha_C\,(\phi - \sigma_C)\right]$. Eq. (271) implies that the following inequality holds:

$$0 < \frac{\Psi \Upsilon_G^N}{\Gamma} \left(\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C\right) < 1, \tag{272}$$

where $\Gamma > 0$, $\Psi > 0$, and $\Upsilon_G^N > 0$.

Impact Effects of a Temporary Fiscal Expansion

Evaluating (262) at time $t = 0$, inserting (270), and using the fact that $\frac{\tilde{P} dG^N(0)}{\tilde{Y}} = \frac{dG(0)}{\tilde{Y}} = g > 0$, leads to the initial response of the relative price of non tradables:

$$\begin{aligned} \hat{P}(0) &= \frac{-\left[\alpha_L \sigma_L + \alpha_C \omega_C \sigma_C\right]}{\Psi} \hat{\tilde{\lambda}} + \frac{1}{\Psi} \frac{\tilde{P} dG^N(0)}{\tilde{Y}}, \\ &= \left\{ -\left[\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C\right] \frac{\Upsilon_G^N \Psi}{\Gamma} \frac{r^\star}{\xi + r^\star} + 1 \right\} \frac{g}{\Psi} > 0, \quad (273) \end{aligned}$$

where the term in braces is unambiguously positive due to inequality (272) and $0 < \frac{r^\star}{\xi + r^\star} < 1$.

Substituting the change in the equilibrium value of the marginal utility of wealth given by eq. (270) into (265), and multiplying both sides by α_L leads to the initial reaction of non traded labor from initial steady-state in total labor units:

$$\begin{aligned} \alpha_L \hat{L}^N(0) &= \frac{\alpha_L\left[\epsilon\,(1-\alpha_L) + \alpha_L \sigma_L\right]}{\Psi} \left[1 - \left(\alpha_L \sigma_L + \alpha_C \omega_C \sigma_C\right) \frac{\Psi \Upsilon_G^N}{\Gamma} \frac{r^\star}{\xi + r^\star}\right] g \\ &+ \alpha_L \sigma_L \frac{\Psi \Upsilon_G^N}{\Gamma} \frac{r^\star}{\xi + r^\star} g > 0, \quad (274) \end{aligned}$$

where the term in brackets $\left[1 - \left(\alpha_L \sigma_L + \alpha_C \omega_C \sigma_C\right) \frac{\Psi \Upsilon_G^N}{\Gamma} \frac{r^\star}{\xi + r^\star}\right]$ is unambiguously positive due to inequality (272) and $0 < \frac{r^\star}{\xi + r^\star} < 1$; hence, labor in the non traded sector unambiguously increases.

Substituting the change in the equilibrium value of the marginal utility of wealth given by eq. (270) into (264) and multiplying both sides by $1 - \alpha_L$ leads to the initial reaction of traded labor from initial steady-state in total labor units:

$$\begin{aligned} (1-\alpha_L)\,\hat{L}^T(0) &= -\frac{(1-\alpha_L)\,\alpha_L\,(\epsilon - \sigma_L)}{\Psi} \left[1 - \left(\alpha_L \sigma_L + \alpha_C \omega_C \sigma_C\right) \frac{\Psi \Upsilon_G^N}{\Gamma} \frac{r^\star}{\xi + r^\star}\right] g \\ &+ (1-\alpha_L)\,\sigma_L \frac{\Psi \Upsilon_G^N}{\Gamma} \frac{r^\star}{\xi + r^\star} g \lesseqgtr 0, \quad (275) \end{aligned}$$

where inequality (272) together with $0 < \frac{r^\star}{\xi + r^\star} < 1$ imply that the first term on the RHS is unambiguously negative as long as we set assumption 1.

Differentiating (268) with respect to time leads to the response of the current account as a percentage of GDP:

$$\frac{\dot{B}(t)}{\tilde{Y}} = -\Upsilon_G^N \frac{\xi}{\xi + r^\star} g e^{-\xi t} < 0, \tag{276}$$

where $\Upsilon_G^N > 0$.

We now investigate the impact of a government spending shock on sectoral output (or alternatively labor since $Y^j = L^j$) shares. To begin with, real GDP which we denote by Y_R is equal to the sum of value added at constant prices:

$$Y_R = Y^T + \tilde{P} Y^N, \tag{277}$$

where $\tilde{P}$ corresponds to the initial steady-state value of the relative price of non tradables. Using the fact that $Y^j = L^j$, totally differentiating (277) gives:

$$\hat{Y}_R = (1 - \alpha_L)\, \hat{L}^T + \alpha_L \hat{L}^N. \tag{278}$$

Using the fact that $\hat{L}^T = \sigma_L \hat{\bar{\lambda}} - \alpha_L (\epsilon - \sigma_L) \hat{P}$ and $\hat{L}^N = \sigma_L \hat{\bar{\lambda}} + [\epsilon (1 - \alpha_L) + \sigma_L \alpha_L] \hat{P}$, eq. (278) can be rewritten as follows:

$$\hat{Y}_R = \sigma_L \hat{\bar{\lambda}} + \alpha_L \sigma_L \hat{P}. \tag{279}$$

According to (279), a government spending shock impinges on real GDP through two channels; first, by inducing agents to supply more labor, the negative wealth effect pushes up output; second, since the relative price of non tradables appreciates, non traded firms are induced to produce and thus to hire more; as workers' experience mobility costs, non traded firms have to pay higher wages which increase the aggregate wage, W, in proportion to the non tradable content of labor compensation, α_L; consequently, agents are encouraged to increase hours worked more which pushes up further real GDP.

To compute the change in the sectoral output share calculated as the growth differential between sectoral output and real GDP in total output units, we divide both sides of eq. (277) by Y_R and totally differentiate:

$$0 = (1 - \alpha_L) \left(\hat{Y}^T - \hat{Y}_R \right) + \alpha_L \left(\hat{Y}^N - \hat{Y}_R \right). \tag{280}$$

The first and the second term on the RHS of eq. (280) corresponds to the response of output share in sector $j = T, N$ in total output units. More precisely, the change in the sectoral output share is measured by the product of the growth differential between output of sector j and real GDP and the share of sector j in GDP.

Using the fact that $\hat{L}^N = \sigma_L \hat{\bar{\lambda}} + [\epsilon (1 - \alpha_L) + \sigma_L \alpha_L] \hat{P}$, inserting (278), and evaluating at time $t = 0$, the response of the output share of non tradables is given by:

$$\alpha_L \left(\hat{Y}^N(0) - \hat{Y}_R(0) \right) = \alpha_L (1 - \alpha_L) \epsilon \hat{P}(0), \tag{281}$$

where $\hat{P}(0)$ corresponds to the initial response of the relative price of non tradables in percentage deviation from trend (see eq. (273)).

Using the fact that $\hat{L}^T = \sigma_L \hat{\bar{\lambda}} - \alpha_L (\epsilon - \sigma_L) \hat{P}$, inserting (278), and evaluating at time $t = 0$, the response of the output share of tradables is given by:

$$(1 - \alpha_L) \left(\hat{Y}^T(0) - \hat{Y}_R(0) \right) = -\alpha_L (1 - \alpha_L) \epsilon \hat{P}(0), \tag{282}$$

where the initial change in the relative price of non tradables relative to initial steady state in percent, $\hat{P}(0)$, is described by eq. (273). It is straightforward to see that (282) is exactly the opposite of eq. (281).

E.14 A Friendly Way to Solve the Model with Perfect Mobility of Labor

When assuming perfect mobility of labor, the short-run equilibrium reduces to:

$$C = \left(P_C \bar{\lambda}\right)^{-\sigma_C}, \tag{283a}$$

$$L = \left(\bar{\lambda} W\right)^{\sigma_L}, \tag{283b}$$

$$C^N = \alpha_C \frac{P_C}{P} C, \tag{283c}$$

$$C^T = (1-\alpha_C) P_C C, \tag{283d}$$

$$W^T = 1, \tag{283e}$$

$$W^N = P, \tag{283f}$$

$$W^N = W^T = W, \tag{283g}$$

$$L = L^T + L^N, \tag{283h}$$

$$Y^N = C^N + G^N, \tag{283i}$$

$$\dot{B} = r^\star B + Y^T - C^T - G^T, \tag{283j}$$

where $Y^N = L^N$, $Y^T = L^T$, and α_C is given by eq. (130a).

Short-Run Solutions

Substituting (283e) and (283f) into (283g) leads to:

$$P = 1. \tag{284}$$

Because sectoral wages must equalize while the marginal product of labor in the traded sector is fixed, the relative price of non tradables remains unaffected by a government spending shock, both in the short-run and the long-run.

Substituting first (283a) into (283c), the market clearing condition (151) for the non traded good can be rewritten as follows:

$$L^N = \frac{\alpha_C P_C^{1-\sigma_C} \bar{\lambda}^{-\sigma_C}}{P} + G^N. \tag{285}$$

Totally differentiating (285), using (284), leads to:

$$\alpha_L \hat{L}^N = -\alpha_C \omega_C \sigma_C \hat{\bar{\lambda}} + \frac{P dG^N}{Y}. \tag{286}$$

Inserting $L = \bar{\lambda}^{\sigma_L}$ (since $W = 1$) into (283h), differentiating and using (286) leads to:

$$(1-\alpha_L) \hat{L}^T = \left[\sigma_L + \alpha_C \omega_C \sigma_C\right] \hat{\bar{\lambda}} - \frac{P dG^N}{Y}. \tag{287}$$

Inserting $L^T = L - L^N$ together with $L^N = C^N + G^N$ and $L = \bar{\lambda}^{\sigma_L}$ (since $W = 1$) into (283j), the market clearing condition for the traded good can be written as follows:

$$\begin{aligned} \dot{B}(t) &= r^\star B(t) + L - P_C C - G^T - P G^N(t), \\ &= r^\star B(t) + \bar{\lambda}^{\sigma_L} - (1-\alpha_C) P_C^{1-\sigma_C} \bar{\lambda}^{-\sigma_C} - P G^N(t) - G^T. \end{aligned} \tag{288}$$

Using the fact that both $\bar{\lambda}$, G^T, and P are constant over time, linearizing (288) in the neighborhood of the steady-state leads to:

$$\dot{B}(t) = r^\star dB(t) - \tilde{P} dG^N(t).$$

Substituting the law of motion of government spending (258) and solving leads to the general solution for the net foreign asset position:

$$B(t) - \tilde{B} = \left[\left(B_0 - \tilde{B}\right) + \frac{\tilde{Y}}{\xi + r^\star} g\right] e^{r^\star t} - \frac{\tilde{Y}}{\xi + r^\star} g e^{-\xi t}. \tag{289}$$

Invoking the transversality condition gives the solution for $B(t)$:

$$B(t) - \tilde{B} = \frac{\tilde{Y}}{\xi + r^{\star}} g e^{-\xi t}, \tag{290}$$

consistent with the intertemporal solvency condition

$$\left(\tilde{B} - B_0\right) = -\frac{\tilde{Y}}{\xi + r^{\star}} g. \tag{291}$$

To determine the change in the equilibrium value of the marginal utility of wealth, we have to differentiate the market clearing condition (283j) for the traded good evaluated at the steady-state (i.e., $\dot{B}(t) = 0$), using the fact that government spending reverts to its initial level in the long-run (i.e., $dG^N = 0$):

$$\begin{aligned} & r^{\star} \frac{d\tilde{B}}{\tilde{Y}} + (1 - \alpha_L) \hat{\tilde{L}}^T = (1 - \alpha_C) \omega_C \hat{\tilde{C}}^T, \\ & \hat{\tilde{\lambda}} = -r^{\star} \frac{d\tilde{B}}{\tilde{Y}}, \end{aligned}$$

where we used (287) (setting $dG^N = 0$) and $\hat{\tilde{C}}^T = -\sigma_C \hat{\tilde{\lambda}}$. Substituting (291) into the above equation leads to the change in the equilibrium value of the marginal utility of wealth:

$$\hat{\tilde{\lambda}} = \frac{1}{\sigma_L + \omega_C \sigma_C} \frac{r^{\star}}{\xi + r^{\star}} g > 0, \tag{292}$$

where $\xi > 0$ and $g > 0$. According to (292), a temporary rise in government consumption generates a negative wealth effect reflected by an increase in the shadow value of wealth.

E.15 Perfect Mobility of Labor as a Special Case of a Model with Limited Substitutability in Hours Worked across Sectors

In order to generate barriers to mobility, we assume limited substitutability in hours worked across sectors along the lines of Horvath [2000]. The degree of substitutability of hours worked across sectors captures the extent of workers' mobility costs. As the elasticity of labor supply across sectors takes higher values, workers experience lower mobility costs and thus the degree of labor mobility increases. The advantage of this modelling strategy is that it allows us to consider the range of all degrees of labor mobility across sectors. Specifically, if we let ϵ be zero or tend toward infinity, total immobility ($\epsilon = 0$) and perfect mobility ($\epsilon \to \infty$), respectively, emerges as a special case. In this subsection, we investigate how the degree of labor mobility affects the magnitude of initial responses of sectoral variables to a government spending shock.

As will be useful later, we compute several expressions. Inserting the expression for Ψ given by (157) into the expression of Υ_G^N described by (192), letting ϵ tend toward infinity and applying l'Hôpital's rule leads to:

$$\begin{aligned} \lim_{\epsilon \to \infty} \Upsilon_G^N &= \lim_{\epsilon \to \infty} \frac{\left[(1 - \alpha_L) \alpha_L (\epsilon - \sigma_L) + (1 - \alpha_C) \omega_C \alpha_C (\phi - \sigma_C)\right]}{\alpha_L \left[\epsilon (1 - \alpha_L) + \sigma_L \alpha_L\right] + \omega_C \alpha_C \left[(1 - \alpha_C) \phi + \alpha_C \sigma_C\right]}, \\ &= \frac{\alpha_L (1 - \alpha_L)}{\alpha_L (1 - \alpha_L)} = 1. \end{aligned} \tag{293}$$

Using the expression for Γ given by eq. (271), letting ϵ tend toward infinity and applying l'Hôpital's rule leads to:

$$\begin{aligned} \lim_{\epsilon \to \infty} \frac{\Psi \Upsilon_G^N}{\Gamma} &= \lim_{\epsilon \to \infty} \frac{\Upsilon_G^N}{\left[(1 - \alpha_L) \sigma_L + \omega_C (1 - \alpha_C) \sigma_C\right] + \left[\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C\right] \Upsilon_G^N}, \\ &= \frac{1}{\sigma_L + \omega_C \sigma_C}, \end{aligned} \tag{294}$$

where we used the fact that $\lim_{\epsilon\to\infty}\Upsilon_G^N = 1$ (see eq. (293)). Finally, we compute two additional expressions by inserting the expression for Ψ given by (157), letting ϵ tend toward infinity and applying l'Hôpital's rule:

$$\begin{aligned}
\lim_{\epsilon\to\infty}\frac{\alpha_L\left[\epsilon\left(1-\alpha_L\right)+\alpha_L\sigma_L\right]}{\Psi} &= \lim_{\epsilon\to\infty}\frac{\alpha_L\left[\epsilon\left(1-\alpha_L\right)+\alpha_L\sigma_L\right]}{\alpha_L\left[\epsilon\left(1-\alpha_L\right)+\sigma_L\alpha_L\right]+\omega_C\alpha_C\left[\left(1-\alpha_C\right)\phi+\alpha_C\sigma_C\right]}, \\
&= \frac{\alpha_L\left(1-\alpha_L\right)}{\alpha_L\left(1-\alpha_L\right)} = 1, \qquad (295a)\\
\lim_{\epsilon\to\infty}\frac{\left(1-\alpha_L\right)\alpha_L\left(\epsilon-\sigma_L\right)}{\Psi} &= \lim_{\epsilon\to\infty}\frac{\alpha_L\left[\epsilon\left(1-\alpha_L\right)+\alpha_L\sigma_L\right]}{\alpha_L\left[\epsilon\left(1-\alpha_L\right)+\sigma_L\alpha_L\right]+\omega_C\alpha_C\left[\left(1-\alpha_C\right)\phi+\alpha_C\sigma_C\right]}, \\
&= \frac{\alpha_L\left(1-\alpha_L\right)}{\alpha_L\left(1-\alpha_L\right)} = 1. \qquad (295b)
\end{aligned}$$

Letting ϵ tend toward infinity into eq. (274) and using (293) together with (295a), the initial response of hours worked in the non traded sector relative to the initial steady-state in total labor units can be rewritten as follows:

$$\begin{aligned}
\lim_{\epsilon\to\infty}\alpha_L\hat{L}^N(0) &= \lim_{\epsilon\to\infty}\frac{\alpha_L\left[\epsilon\left(1-\alpha_L\right)+\alpha_L\sigma_L\right]}{\Psi}\left[1-\left(\alpha_L\sigma_L+\alpha_C\omega_C\sigma_C\right)\frac{\Psi\Upsilon_G^N}{\Gamma}\frac{r^\star}{\xi+r^\star}\right]g \\
&+ \lim_{\epsilon\to\infty}\alpha_L\sigma_L\frac{\Psi\Upsilon_G^N}{\Gamma}\frac{r^\star}{\xi+r^\star}g > 0, \\
&= \left[1-\frac{\alpha_L\sigma_L+\alpha_C\omega_C\sigma_C}{\sigma_L+\omega_C\sigma_C}\frac{r^\star}{\xi+r^\star}\right]g + \frac{\alpha_L\sigma_L}{\sigma_L+\omega_C\sigma_C}\frac{r^\star}{\xi+r^\star}g, \\
&= \left[1-\frac{\alpha_C\omega_C\sigma_C}{\sigma_L+\omega_C\sigma_C}\frac{r^\star}{\xi+r^\star}\right]g > 0. \qquad (296)
\end{aligned}$$

Eq. (296) gives the initial response of hours worked in the non traded sector to an exogenous temporary increase in G^N when labor can freely move from one sector to another. As discussed below, the magnitude of the rise in non traded labor on impact, i.e., $\alpha_L\hat{L}^N(0) > 0$, can be larger or lower than that with a difficulty in reallocating labor across sectors. Intuitively, in the latter case, the relative price of non tradables appreciates which exerts a strong positive impact on the reallocation of labor toward the non traded sector.

Letting ϵ tend toward infinity into eq. (275) and using (293) together with (295a), the initial response of hours worked in the traded sector relative to the initial steady-state in total labor units can be rewritten as follows:

$$\begin{aligned}
\lim_{\epsilon\to\infty}\left(1-\alpha_L\right)\hat{L}^T(0) &= \lim_{\epsilon\to\infty}-\frac{\left(1-\alpha_L\right)\alpha_L\left(\epsilon-\sigma_L\right)}{\Psi}\left[1-\left(\alpha_L\sigma_L+\alpha_C\omega_C\sigma_C\right)\frac{\Psi\Upsilon_G^N}{\Gamma}\frac{r^\star}{\xi+r^\star}\right]g \\
&+ \lim_{\epsilon\to\infty}\left(1-\alpha_L\right)\sigma_L\frac{\Psi\Upsilon_G^N}{\Gamma}\frac{r^\star}{\xi+r^\star}g \lesseqgtr 0, \\
&= -\left[1-\frac{\alpha_L\sigma_L+\alpha_C\omega_C\sigma_C}{\sigma_L+\omega_C\sigma_C}\frac{r^\star}{\xi+r^\star}\right]g + \frac{\left(1-\alpha_L\right)\sigma_L}{\sigma_L+\omega_C\sigma_C}\frac{r^\star}{\xi+r^\star}g, \\
&= -\left[1-\frac{\sigma_L+\alpha_C\omega_C\sigma_C}{\sigma_L+\omega_C\sigma_C}\frac{r^\star}{\xi+r^\star}\right]g < 0. \qquad (297)
\end{aligned}$$

Summing (296) and (297) leads to:

$$\begin{aligned}
\lim_{\epsilon\to\infty}\alpha_L\hat{L}^N(0) + \lim_{\epsilon\to\infty}\left(1-\alpha_L\right)\hat{L}^T(0) &= \frac{\sigma_L}{\sigma_L+\omega_C\sigma_C}\frac{r^\star}{\xi+r^\star}g, \\
&= \lim_{\epsilon\to\infty}\hat{L}(0), \qquad (298)
\end{aligned}$$

where the last equality is derived by letting ϵ tend toward infinity into eq. (263).

We now investigate the magnitude of the response of the output share of tradables when imposing perfect mobility of labor across sectors. Letting ϵ tend toward infinity into eq. (281), using (294) together with the fact that $\lim_{\epsilon\to\infty}\frac{\alpha_L(1-\alpha_L)}{\Psi} = 1$, and applying l'Hôpital's rule, the initial response of the output share of non tradables can be rewritten as follows:

$$\begin{aligned}
\lim_{\epsilon\to\infty}\alpha_L\left(\hat{Y}^N(0)-\hat{Y}_R(0)\right) &= \lim_{\epsilon\to\infty}\alpha_L\left(1-\alpha_L\right)\epsilon\hat{P}(0), \\
&= \left[1-\left(\frac{\alpha_L\sigma_L+\alpha_C\omega_C\sigma_C}{\sigma_L+\omega_C\sigma_C}\right)\frac{r^\star}{\xi+r^\star}\right]g > 0, \qquad (299)
\end{aligned}$$

where $0 < \left(\frac{\alpha_L \sigma_L + \alpha_C \omega_C \sigma_C}{\sigma_L + \omega_C \sigma_C}\right) < 1$.

Applying the same logic to the output share of tradables described by eq. (282), the response of the traded output relative to GDP in percent of output when assuming perfect mobility of labor across sectors is:

$$\begin{aligned}
\lim_{\epsilon \to \infty} (1-\alpha_L)\left(\hat{Y}^T(0) - \hat{Y}_R(0)\right) &= -\alpha_L (1-\alpha_L) \epsilon \hat{P}(0), \\
&= -\lim_{\epsilon \to \infty} \alpha_L (1-\alpha_L) \epsilon \hat{P}(0), \\
&= -\left[1 - \left(\frac{\alpha_L \sigma_L + \alpha_C \omega_C \sigma_C}{\sigma_L + \omega_C \sigma_C}\right) \frac{r^\star}{\xi + r^\star}\right] g < 0. \quad (300)
\end{aligned}$$

E.16 Relationship between the magnitude of impact responses and the degree of labor mobility across sectors: Proofs of Results in Section 4.2

We now investigate the relationship between the magnitude of responses of sectoral labor and the degree of labor mobility across sectors captured by ϵ. To do so, we have to first rewrite $\frac{\Psi \Upsilon_G^N}{\Gamma}$ (see the first line of eq. (294)) as follows

$$\frac{\Psi \Upsilon_G^N}{\Gamma} = \frac{\Upsilon_G^N}{\left[(1-\alpha_L)\sigma_L + \omega_C (1-\alpha_C)\sigma_C\right] + \left[\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C\right] \Upsilon_G^N}, \quad (301)$$

and to determine whether $\frac{\Psi \Upsilon_G^N}{\Gamma}$ increases or decreases as the degree of labor mobility rises. To do so, we have to determine the relationship between Υ_G^N described by (192) and ϵ:

$$\frac{\partial \Upsilon_G^N}{\partial \epsilon} = \frac{(1-\alpha_L)\alpha_L (\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C)}{\Psi^2} > 0, \quad (302)$$

where Ψ is given by eq. (157). When $\epsilon = 0$, Υ_G^N described by (192) becomes:

$$\Upsilon_G^N\big|_{\epsilon=0} = 1 - \frac{(\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C)}{(\alpha_L)^2 \sigma_L + \omega_C \alpha_C \left[(1-\alpha_C)\phi + \alpha_C \sigma_C\right]} \lessgtr 0. \quad (303)$$

In sum, Υ_G^N can take negative values when ϵ is close to 0, is increasing with ϵ and takes a maximum value of 1 when we let $\epsilon \to \infty$. Differentiating (301) with respect to ϵ leads to:

$$\begin{aligned}
\frac{\partial \frac{\Psi \Upsilon_G^N}{\Gamma}}{\partial \epsilon} &= \frac{\frac{\partial \Upsilon_G^N}{\partial \epsilon}\left[(1-\alpha_L)\sigma_L + \omega_C (1-\alpha_C)\sigma_C\right]}{\left\{\left[(1-\alpha_L)\sigma_L + \omega_C (1-\alpha_C)\sigma_C\right] + \left[\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C\right]\Upsilon_G^N\right\}^2} > 0, \\
&= \frac{(1-\alpha_L)\alpha_L \left[\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C\right]\left[(1-\alpha_L)\sigma_L + \omega_C (1-\alpha_C)\sigma_C\right]}{\Gamma^2} > 0. \quad (304)
\end{aligned}$$

Because $\frac{\Psi \Upsilon_G^N}{\Gamma}$ and Ψ are both positive and increasing with ϵ while $\lim_{\epsilon \to \infty} \frac{\Psi \Upsilon_G^N}{\Gamma} = \frac{1}{\sigma_L + \omega_C \sigma_C}$ (see eq. 294) and $\lim_{\epsilon \to \infty} \Psi = \infty$, the initial reaction of the relative price to a government spending shock is unambiguously decreasing with ϵ; differentiating (273) with respect to ϵ leads to:

$$\begin{aligned}
\frac{\partial \hat{P}(0)}{\partial \epsilon} &= -\frac{g}{\Psi}\left[\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C\right] \frac{r^\star}{\xi + r^\star} \frac{\partial \frac{\Psi \Upsilon_G^N}{\Gamma}}{\partial \epsilon} \\
&- \left\{1 - \left[\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C\right] \frac{r^\star}{\xi + r^\star} \frac{\Psi \Upsilon_G^N}{\Gamma}\right\} \frac{g}{\Psi^2} \frac{\partial \Psi}{\partial \epsilon} < 0. \quad (305)
\end{aligned}$$

A rise in ϵ mitigates the appreciation in the relative price of non tradables by amplifying the increase in the supply of non tradables and by reducing the excess of demand for non tradables. First, in countries where labor is more mobile across sectors, a government spending shock biased toward non tradables leads to a larger increase in non traded output which mitigates the appreciation in the relative price of non tradables. Second, as ϵ takes higher values, the wealth effect becomes larger so that private consumption is crowded out by a larger amount which results in a lower excess demand of non tradables.

E.16.1 Relationship between and $\alpha_L\left(\hat{Y}^N(0)-\hat{Y}_R(0)\right)$ and ϵ

Totally differentiating the response of output share of non tradables to a government spending shock described by eq. (281) with respect to ϵ leads to:

$$\frac{\partial \alpha_L\left(\hat{Y}^N(0)-\hat{Y}_R(0)\right)}{\partial \epsilon}=\alpha_L\left(1-\alpha_L\right)\epsilon\hat{P}(0)\left[1+\frac{\partial \hat{P}(0)}{\partial \epsilon}\frac{\epsilon}{\hat{P}(0)}\right]. \tag{306}$$

According to (306), the relationship between the positive response of output share of non tradables and the degree of labor mobility across sectors is ambiguous. On the one hand, as shown by the first term in brackets on the RHS of (306), a rise in the parameter ϵ amplifies the reallocation of labor toward the non traded sector and thus increases further the output share of non tradables. On the other hand, the rise in the degree of labor mobility also mitigates the rise in the output share as higher mobility increases further the shadow value of wealth which amplifies the crowding out of private consumption by public spending and thus moderates the excess demand in the non traded goods market. Consequently, the relative price of non tradables appreciates by a lower amount which reduces the incentive to increase non traded output. While we address this ambiguity numerically in the main text when we simulate the full model with physical capital accumulation subject to adjustment costs, we provide a formal proof below that $\frac{\partial \alpha_L\left(\hat{Y}^N(0)-\hat{Y}_R(0)\right)}{\partial \epsilon}>0$ in a model with labor only.

For the RHS of eq. (306) to be positive, we must have:

$$-\frac{\partial \hat{P}(0)}{\partial \epsilon}\frac{\epsilon}{\hat{P}(0)}<1. \tag{307}$$

To show that inequality (307) holds, we have to make assumptions. We are able to sign expressions in two polar cases: $\xi\to\infty$ and $\xi\to 0$. The former and the latter case correspond to situations where the government spending shock is weakly persistent (i.e., G increases initially and is restored back toward its initial level) and highly persistent (i.e., the fiscal shock is permanent).

A Weakly Persistent Fiscal Shock

Letting $\xi\to\infty$ into eq. (273), the initial appreciation in the relative price of non tradables reduces to:

$$\hat{P}(0)\big|_{\xi\to\infty}=\frac{g}{\Psi}>0, \tag{308}$$

where Ψ is given by eq. (157). Differentiating (308) w.r.t. ϵ leads to:

$$\frac{\partial \hat{P}(0)\big|_{\xi\to\infty}}{\partial \epsilon}=-\frac{g\alpha_L\left(1-\alpha_L\right)}{\Psi^2}<0. \tag{309}$$

Combining (308) and (309), the elasticity (in absolute terms) of the impact response of the relative price to the degree of labor mobility is thus given by:

$$0<-\frac{\partial \hat{P}(0)\big|_{\xi\to\infty}}{\partial \epsilon}\frac{\epsilon}{\hat{P}(0)\big|_{\xi\to\infty}}=\frac{\alpha_L\left(1-\alpha_L\right)\epsilon}{\Psi}<1. \tag{310}$$

Since $\Psi>\alpha_L\epsilon\left(1-\alpha_L\right)$, the elasticity is strictly smaller than one and thus the RHS of eq. (306) is unambiguously positive.

A Highly Persistent Fiscal Shock

Letting $\xi\to 0$ into eq. (273), the initial appreciation in the relative price of non tradables reduces to:

$$\hat{P}(0)\big|_{\xi\to 0}=\frac{g}{\Psi}\left[1-\left(\alpha_L\sigma_L+\omega_C\alpha_C\sigma_C\right)\frac{\Upsilon^N_G\Psi}{\Gamma}\right]. \tag{311}$$

Differentiating (308) w.r.t. ϵ leas to:

$$\begin{aligned}\frac{\partial \hat{P}(0)\big|_{\xi\to 0}}{\partial \epsilon} &= -\frac{g\alpha_L\left(1-\alpha_L\right)}{\Psi^2}\left[1-\left(\alpha_L\sigma_L+\omega_C\alpha_C\sigma_C\right)\frac{\Upsilon^N_G\Psi}{\Gamma}\right]\\ &- \frac{g}{\Psi}\left(\alpha_L\sigma_L+\omega_C\alpha_C\sigma_C\right)\frac{\partial\frac{\Psi\Upsilon^N_G}{\Gamma}}{\partial \epsilon},\end{aligned} \tag{312}$$

where $\frac{\partial \frac{\Psi \Upsilon_G^N}{\Gamma}}{\partial \epsilon}$ is given by eq. (304). Computing the following term:

$$\left[1 - \left(\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C\right) \frac{\Upsilon_G^N \Psi}{\Gamma}\right] = \frac{\Psi \left[\left(1-\alpha_L\right) \sigma_L + \omega_C \left(1-\alpha_C\right) \sigma_C\right]}{\Gamma}, \tag{313}$$

the initial reaction of the relative price (311) can be rewritten as follows:

$$\hat{P}(0)\big|_{\xi \to 0} = g \frac{\left[\left(1-\alpha_L\right) \sigma_L + \omega_C \left(1-\alpha_C\right) \sigma_C\right]}{\Gamma} > 0. \tag{314}$$

Making use of (313) and inserting (304), eq. (312) reads as:

$$\frac{\partial \hat{P}(0)\big|_{\xi \to 0}}{\partial \epsilon} = -\frac{g \alpha_L \left(1-\alpha_L\right) \left[\left(1-\alpha_L\right) \sigma_L + \omega_C \left(1-\alpha_C\right) \sigma_C\right]}{\Psi \Gamma^2} \left[\Gamma + \left(\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C\right)^2\right]. \tag{315}$$

Calculating the elasticity in absolute terms of $\hat{P}(0)$ w.r.t. ϵ by combining (314) and (315), we have to show that the following inequality holds for the RHS of eq. (306) to be positive:

$$-\frac{\partial \hat{P}(0)\big|_{\xi \to 0}}{\partial \epsilon} \frac{\epsilon}{\hat{P}(0)\big|_{\xi \to 0}} = \frac{\alpha_L \left(1-\alpha_L\right) \epsilon}{\Psi} \left[1 + \frac{\left(\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C\right)^2}{\Gamma}\right] < 1. \tag{316}$$

To show (316), it is useful to write down the following properties:

$$\Psi = \alpha_L \left(1-\alpha_L\right) \left(\epsilon - \sigma_L\right) + \omega_C \alpha_C \left(1-\alpha_C\right) \left(\phi - \sigma_C\right) + \alpha_L \sigma_L + \omega_C \alpha_C \sigma_C, \tag{317a}$$

$$\Upsilon_G^N \Psi = \Psi - \left(\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C\right), \tag{317b}$$

$$\Gamma = \Psi \left(\sigma_L + \omega_C \sigma_C\right) - \left(\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C\right)^2, \tag{317c}$$

where we made use of (317b) to obtain (317c), i.e.,

$$\begin{aligned} \Gamma &= \Psi \left\{\left[\left(1-\alpha_L\right) \sigma_L + \omega_C \left(1-\alpha_C\right) \sigma_C\right] + \left[\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C\right] \Upsilon_G^N\right\}, \\ &= \Psi \left[\left(1-\alpha_L\right) \sigma_L + \omega_C \left(1-\alpha_C\right) \sigma_C\right] \\ &\quad + \left[\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C\right] \left[\Psi - \left(\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C\right)\right]. \end{aligned} \tag{318}$$

Using (317c), eq. (316) can be rewritteen as follows:

$$\frac{\partial \hat{P}(0)\big|_{\xi \to 0}}{\partial \epsilon} \frac{\epsilon}{\hat{P}(0)\big|_{\xi \to 0}} = \alpha_L \left(1-\alpha_L\right) \epsilon \frac{\left(\sigma_L + \omega_C \sigma_C\right)}{\Gamma} < 1. \tag{319}$$

Thus, making use of eq. (317c), the elasticity (319) is smaller than one if the following inequality holds:

$$\begin{aligned} &\Gamma > \alpha_L \left(1-\alpha_L\right) \epsilon \left(\sigma_L + \omega_C \sigma_C\right), \\ &\Psi \left(\sigma_L + \omega_C \sigma_C\right) - \left(\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C\right)^2 > \alpha_L \left(1-\alpha_L\right) \epsilon \left(\sigma_L + \omega_C \sigma_C\right), \\ &\omega_C \sigma_L \sigma_C \left(\alpha_L - \alpha_C\right)^2 + \left(\sigma_L + \omega_C \sigma_C\right) \omega_C \alpha_C \left(1-\alpha_C\right) \phi > 0. \end{aligned} \tag{320}$$

Since (320) holds for all range of values of parameters, elasticity (307) is strictly smaller than one and thus the RHS of eq. (306) holds.

Relationship between $\alpha_L \left(\hat{Y}^N(0) - \hat{Y}_R(0)\right)$ and ϵ

As shown by eqs. (306) and (307), $\alpha_L \left(\hat{Y}^N(0) - \hat{Y}_R(0)\right)$ is increasing with ϵ as long as $-\frac{\partial \hat{P}(0)}{\partial \epsilon} \frac{\epsilon}{\hat{P}(0)} < 1$. Combining (310) et (319), we find that the elasticity $-\frac{\partial \hat{P}(0)}{\partial \epsilon} \frac{\epsilon}{\hat{P}(0)}$ varies from a low of $\frac{\alpha_L (1-\alpha_L) \epsilon}{\Psi}$ when the shock is weakly persistent to a high of $\frac{\alpha_L (1-\alpha_L) \epsilon}{\Psi} \left[1 + \frac{\left(\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C\right)^2}{\Gamma}\right]$. Hence, when ξ takes intermediate values, the elasticity falls into the following range of values:

$$-\frac{\partial \hat{P}(0)}{\partial \epsilon} \frac{\epsilon}{\hat{P}(0)} \in \left\{\frac{\alpha_L \left(1-\alpha_L\right) \epsilon}{\Psi}, \frac{\alpha_L \left(1-\alpha_L\right) \epsilon}{\Psi} \left[1 + \frac{\left(\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C\right)^2}{\Gamma}\right]\right\}. \tag{321}$$

E.16.2 Relationship between and $\alpha_L \hat{Y}^N(0)$ and ϵ

In the special case where $\sigma_L = 0$, analytical expression of $\alpha_L \hat{Y}^N(0)$ described by eq. (274) reduces to:

$$\alpha_L \hat{L}^N(0)\Big|_{\sigma_L=0} = \frac{\alpha_L \epsilon (1-\alpha_L)}{\Psi} \left[1 - \alpha_C \omega_C \sigma_C \frac{\Psi \Upsilon_G^N}{\Gamma} \frac{r^\star}{\xi + r^\star}\right] g > 0. \tag{322}$$

Eq. (322) corresponds to eq. (281) when setting $\sigma_L = 0$, i.e.,

$$\alpha_L \hat{L}^N(0)\Big|_{\sigma_L=0} = \alpha_L \left(\hat{Y}^N(0) - \hat{Y}_R(0)\right)\Big|_{\sigma_L=0}. \tag{323}$$

Since our proof for $\frac{\partial \alpha_L \left(\hat{Y}^N(0) - \hat{Y}_R(0)\right)}{\partial \epsilon}$ summarized by inequality (321) also holds for $\sigma_L = 0$, we have

$$\frac{\partial \alpha_L \hat{L}^N(0)\Big|_{\sigma_L=0}}{\partial \epsilon} < 0. \tag{324}$$

E.16.3 Relationship between $\hat{L}(0)$ and ϵ

The initial reaction of hours worked to a fiscal shock is:

$$\hat{L}(0) = \sigma_L \left[\hat{\bar{\lambda}} + \alpha_L \hat{P}(0)\right] \tag{325}$$

where $\hat{\bar{\lambda}}$ and $\hat{P}(0)$ are given by (270) and (273), respectively. **Eq. (325) corresponds to eq. (38) in the main text.**

As for the share of non tradables in GDP, we investigate the relationship between the initial reaction of hours worked to a fiscal shock, $\hat{L}(0)$, and the degree of labor mobility across sectors, ϵ, by considering two polar cases.

A Weakly Persistent Fiscal Shock

Letting $\xi \to \infty$ into eq. (273) and (270), the initial appreciation in the relative price of non tradables reduces to:

$$\hat{P}(0)\big|_{\xi\to\infty} = \frac{g}{\Psi} > 0, \tag{326}$$

where Ψ is given by eq. (157) and the marginal utility of wealth remains unaffected:

$$\hat{\bar{\lambda}}\big|_{\xi\to\infty} = 0. \tag{327}$$

Differentiating (325) w.r.t. ϵ and using (309) leads to:

$$\begin{aligned} \frac{\partial \hat{L}(0)\big|_{\xi\to\infty}}{\partial \epsilon} &= \sigma_L \alpha_L \frac{\partial \hat{P}(0)\big|_{\xi\to\infty}}{\partial \epsilon}, \\ &= -\sigma_L \alpha_L \frac{g \alpha_L (1-\alpha_L)}{\Psi^2} < 0. \end{aligned} \tag{328}$$

A Highly Persistent Fiscal Shock

Letting $\xi \to 0$ into eq. (325) and using eqs. (270) and (273), the initial reaction of hours worked can be rewritten as follows:

$$\begin{aligned} \hat{L}(0)\big|_{\xi\to 0} &= \sigma_L \left[\hat{\bar{\lambda}}\big|_{\xi\to 0} + \alpha_L \hat{P}(0)\big|_{\xi\to 0}\right], \\ &= g\sigma_L \left\{\frac{\Upsilon_G^N \Psi}{\Gamma} + \frac{\alpha_L}{\Psi}\left[1 - (\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C) \frac{\Upsilon_G^N \Psi}{\Gamma}\right]\right\}. \end{aligned} \tag{329}$$

Differentiating (329) w.r.t. ϵ, making use of (304) and (316) leads to:

$$\begin{aligned}
\frac{\partial \hat{L}(0)\big|_{\xi\to\infty}}{\partial \epsilon} &= \sigma_L \left[\frac{\partial \frac{\Psi \Upsilon_G^N}{\Gamma}}{\partial \epsilon} g + \alpha_L \frac{\partial \hat{P}(0)\big|_{\xi\to 0}}{\partial \epsilon} \right], \\
&= g\sigma_L \frac{(1-\alpha_L)\alpha_L\left[(1-\alpha_L)\sigma_L + \omega_C(1-\alpha_C)\sigma_C\right]}{\Psi\Gamma^2} \Big[\Psi\left(\alpha_L\sigma_L + \omega_C\alpha_C\sigma_C\right) \\
&- \alpha_L\Gamma - \alpha_L\left(\alpha_L\sigma_L + \omega_C\alpha_C\sigma_C\right)^2 \Big], \\
&= -g\sigma_L \frac{(1-\alpha_L)\alpha_L\left[(1-\alpha_L)\sigma_L + \omega_C(1-\alpha_C)\sigma_C\right]}{\Gamma^2} \\
&\quad \times \omega_C\sigma_C\left(\alpha_L - \omega_C\alpha_C\right) < 0, \qquad (330)
\end{aligned}$$

where we used (317c) to obtain the last line of eq. (330), i.e, we computed the following term:

$$\begin{aligned}
& \Psi\left(\alpha_L\sigma_L + \omega_C\alpha_C\sigma_C\right) - \alpha_L\Gamma - \alpha_L\left(\alpha_L\sigma_L + \omega_C\alpha_C\sigma_C\right)^2, \\
= \; & \Psi\omega_C\sigma_C\left(\alpha_L - \omega_C\alpha_C\right) > 0. \qquad (331)
\end{aligned}$$

The RHS of eq. (330) is positive since according to the market clearing condition for non tradables expressed in percentage point of GDP, we have:

$$\alpha_L = \omega_C\alpha_C + \omega_G\omega_{G^N}, \qquad (332)$$

and thus as long as $\omega_{G^N} > 0$, we have:

$$\alpha_L - \omega_C\alpha_C > 0. \qquad (333)$$

In conclusion, the initial reaction of hours worked is decreasing with the degree of labor mobility across sectors, ϵ.

E.17 Elasticity of Labor Supply and the Share of Non Tradables: Sensitivity Analysis

In this subsection, we investigate how the elasticity of labor supply, σ_L, and the non tradable content of consumption expenditure, α_C, influence the magnitude of the sectoral impact of a government spending shock.

E.17.1 Sensitivity to the Intertemporal Elasticity for Labor Supply

We first investigate the implications of the Frisch elasticity of labor supply for the responses of the marginal utility of wealth and the relative price of non tradables which are described by (270) and (273), respectively. To do so, we have to explore the relationship between $\frac{\Psi\Upsilon_G^N}{\Gamma}$ and σ_L. Differentiating Υ_G^N w.r.t. σ_L leads to:

$$\frac{\partial \Upsilon_G^N}{\partial \sigma_L} = -\frac{\alpha_L}{\Psi^2}\left\{\alpha_L(1-\alpha_L)\epsilon + \omega_C\sigma_C\left[(1-\alpha_C)\phi - (\alpha_L-\alpha_C)\sigma_C\right]\right\} \lesseqgtr 0. \qquad (334)$$

While the sign of $\frac{\partial \Upsilon_G^N}{\partial \sigma_L}$, is ambiguous, when ϕ is close to σ_C, we find that $\frac{\partial \Upsilon_G^N}{\partial \sigma_L} < 0$. Eq. (301) can be rewritten as follows:

$$\frac{\Psi\Upsilon_G^N}{\Gamma} = \frac{1}{\frac{\left[(1-\alpha_L)\sigma_L + \omega_C(1-\alpha_C)\sigma_C\right]}{\Upsilon_G^N} + \left[\alpha_L\sigma_L + \omega_C\alpha_C\sigma_C\right]}. \qquad (335)$$

Because the denominator is higher as the values of σ_L increase, the marginal utility of wealth rises by a smaller amount (see eq. (270)). Intuitively, because agents supply more labor following a rise in government consumption, private savings falls by a smaller amount which results in a lower current account deficit. Thus, the marginal utility of wealth must increase less for the intertemporal solvency condition to hold. According to (273), increasing

σ_L exerts opposite effects on $\hat{P}(0)$. First, because the marginal utility of wealth increases less, consumption in non tradables falls less while hours worked rises more in the non traded sector as agents supply more labor. If both effects offset each other, excess demand in the non traded goods market is unchanged. On the other hand, raising σ_L makes the relative price more responsive to the excess demand in the non traded goods market following a rise in G^N as reflected by larger values in Ψ (see eq. (157)). Overall, one may expect that the last effect predominates so that the relative price of non tradables appreciates less when the elasticity σ_L is high. As a result, the responses of sectoral labor and thus sectoral output shares described by (281) for non tradables and (282) for tradables, respectively, should be less pronounced as the relative price appreciates less.

E.17.2 Sensitivity to Non Tradable Share

We first investigate the implications of increasing α_C for the responses of the marginal utility of wealth and the relative price of non tradables which are described by (270) and (273), respectively. To do so, we first evaluate Υ_G^N when we let α_C tend toward zero and one, respectively:

$$\lim_{\alpha_C \to 0} \Upsilon_G^N = \frac{(1-\alpha_L)\,\alpha_L\,(\epsilon - \sigma_L)}{\alpha_L\left[\epsilon\,(1-\alpha_L) + \alpha_L \sigma_L\right]}, \tag{336a}$$

$$\lim_{\alpha_C \to 1} \Upsilon_G^N = \frac{(1-\alpha_L)\,\alpha_L\,(\epsilon - \sigma_L)}{\alpha_L\left[\epsilon\,(1-\alpha_L) + \alpha_L \sigma_L\right] + \omega_C \sigma_C}. \tag{336b}$$

It is straightforward to see that the following inequality holds:

$$\lim_{\alpha_C \to 0} \Upsilon_G^N > \lim_{\alpha_C \to 1} \Upsilon_G^N > 0. \tag{337}$$

Then, we evaluate $\frac{\Psi \Upsilon_G^N}{\Gamma}$ when we let α_C tend toward zero and one, respectively:

$$\lim_{\alpha_C \to 0} \frac{\Psi \Upsilon_G^N}{\Gamma} = \frac{1}{\frac{\left[(1-\alpha_L)\sigma_L + \omega_C \sigma_C\right]}{\lim_{\alpha_C \to 0} \Upsilon_G^N} + \alpha_L \sigma_L}, \tag{338a}$$

$$\lim_{\alpha_C \to 1} \frac{\Psi \Upsilon_G^N}{\Gamma} = \frac{1}{\frac{(1-\alpha_L)\sigma_L}{\lim_{\alpha_C \to 1} \Upsilon_G^N} + \alpha_L \sigma_L + \omega_C \sigma_C}. \tag{338b}$$

Substituting (336a) into (338a) and (336b) into (338b), after tedious computations, it can be shown analytically that:

$$\left\{\frac{\left[(1-\alpha_L)\,\sigma_L + \omega_C \sigma_C\right]}{\lim_{\alpha_C \to 0} \Upsilon_G^N} + \alpha_L \sigma_L\right\} - \left\{\frac{(1-\alpha_L)\,\sigma_L}{\lim_{\alpha_C \to 1} \Upsilon_G^N} + \alpha_L \sigma_L + \omega_C \sigma_C\right\} > 0, \tag{339}$$

and thus

$$\lim_{\alpha_C \to 1} \frac{\Psi \Upsilon_G^N}{\Gamma} > \lim_{\alpha_C \to 0} \frac{\Psi \Upsilon_G^N}{\Gamma} > 0. \tag{340}$$

Intuitively, as α_C takes higher values, the share of tradables falls. At the final steady-state, net exports must be larger for the open economy to be solvent. To improve the balance of trade in the long-run, output of tradables must be higher while consumption in tradables must be lower. Because the share of tradables in the economy is lower, the marginal utility of wealth must increase by a larger amount to lower consumption in tradables and thus to increase net exports.

As the negative wealth effect is stronger, excess demand for non tradables and thus the subsequent appreciation in the relative price P are smaller which mitigates the shift of resources toward the non traded sector and thus moderates the fall in traded output and the rise in non traded output.

E.18 Effects of a Rise in Government Consumption on Tradables, G^T

In this subsection, we explore the effects of a rise in government consumption on tradables, G^T, while keeping fixed public purchases of non tradables, G^N. Since G^N is unchanged, eq. (262) reduces to:

$$\hat{P} = \frac{-\left[\alpha_L \sigma_L + \alpha_C \omega_C \sigma_C\right]}{\Psi} \hat{\bar{\lambda}}, \tag{341}$$

where $\Psi = \alpha_L \left[\epsilon\left(1-\alpha_L\right) + \sigma_L \alpha_L\right] + \omega_C \alpha_C \left[\left(1-\alpha_C\right)\phi + \alpha_C \sigma_C\right] > 0$ (see eq. (157)).

Inserting (341) into $\hat{L}^T = -\alpha_L\left(\epsilon - \sigma_L\right)\hat{P} + \sigma_L \hat{\bar{\lambda}}$ leads to the change in traded labor relative to initial steady-state:

$$\hat{L}^T = \left\{\sigma_L + \frac{\alpha_L\left(\epsilon-\sigma_L\right)\left[\alpha_L \sigma_L + \alpha_C \omega_C \sigma_C\right]}{\Psi}\right\} \hat{\bar{\lambda}}. \tag{342}$$

Inserting (341) into $\hat{L}^N = \left[\epsilon\left(1-\alpha_L\right) + \alpha_L \sigma_L\right]\hat{P} + \sigma_L \hat{\bar{\lambda}}$ leads to the change in non traded labor from initial steady-state:

$$\hat{L}^N = \left\{\sigma_L - \frac{\left[\epsilon\left(1-\alpha_L\right)+\alpha_L\sigma_L\right]\left[\alpha_L \sigma_L + \alpha_C \omega_C \sigma_C\right]}{\Psi}\right\} \hat{\bar{\lambda}}, \tag{343}$$

where the term in braces is positive if and only if:

$$\sigma_L\left[\left(1-\alpha_C\right)\phi + \alpha_C\sigma_C\right] > \sigma_C\left[\epsilon\left(1-\alpha_L\right) + \alpha_L\sigma_L\right].$$

One interesting case is that where $\sigma_C = \phi = 1$. Eq. (343) can be rewritten as follows:

$$\hat{L}^N = -\left\{\frac{\alpha_C \omega_C \left(1-\alpha_L\right)\left(\epsilon - \sigma_L\right)}{\Psi'}\right\} \hat{\bar{\lambda}} < 0, \tag{344}$$

where the sign follows from assumption 1 and we used the fact that $\Psi' = \Psi\big|_{\phi=\sigma_C=1} = \alpha_L\left[\epsilon\left(1-\alpha_L\right) + \sigma_L\alpha_L\right] + \omega_C\alpha_C > 0$ to derive (344).

Applying the theorem of implicit functions, eqs. (341)-(343) lead to the short-run static solutions for the relative price, both traded and non traded labor which depend exclusively on the shadow value of wealth:

$$P = P\left(\bar{\lambda}\right), \quad L^T = L^T\left(\bar{\lambda}\right), \quad L^N = L^N\left(\bar{\lambda}\right). \tag{345}$$

Inserting (341) into $\hat{C}^T = \alpha_C\left(\phi - \sigma_C\right)\hat{P} - \sigma_C\hat{\bar{\lambda}}$ leads to the response of consumption in tradables in percentage relative to initial steady-state:

$$\hat{C}^T = \left\{\sigma_C + \frac{\alpha_C\left(\phi-\sigma_C\right)\left[\alpha_L \sigma_L + \alpha_C \omega_C \sigma_C\right]}{\Psi}\right\} \hat{\bar{\lambda}}. \tag{346}$$

Inserting (341) into $\hat{C}^N = \left[\phi\left(1-\alpha_C\right) + \alpha_C\sigma_C\right]\hat{P} - \sigma_C\hat{\bar{\lambda}}$ leads to the response of consumption in non tradables in percentage relative to initial steady-state:

$$\begin{aligned} \hat{C}^N &= -\left\{\sigma_C - \frac{\left[\phi\left(1-\alpha_C\right)+\alpha_C\sigma_C\right]\left[\alpha_L \sigma_L + \alpha_C \omega_C \sigma_C\right]}{\Psi}\right\} \hat{\bar{\lambda}}, \\ &= -\frac{\alpha_L\left\{\sigma_C\left[\epsilon\left(1-\alpha_L\right)+\alpha_L\sigma_L\right] - \sigma_L\left[\phi\left(1-\alpha_C\right)+\alpha_C\sigma_C\right]\right\}}{\Psi}\hat{\bar{\lambda}}. \end{aligned} \tag{347}$$

If $\phi = \sigma_C = 1$, consumption in non tradables falls under assumption 1. Applying the theorem of implicit functions, eqs. (346)-(347) lead to the short-run static solution for consumption in tradables and consumption in non tradables which depend exclusively on the shadow value of wealth:

$$C^T = C^T\left(\bar{\lambda}\right), \quad C^N = C^N\left(\bar{\lambda}\right). \tag{348}$$

Substituting short-run static solutions for traded labor, i.e., $L^T = L^T\left(\bar{\lambda}\right)$ and $C^T = C^T\left(\bar{\lambda}\right)$, into (259j) leads to:

$$\dot{B}(t) = r^{\star}B(t) + L^T\left(\bar{\lambda}\right) - C^T\left(\bar{\lambda}\right) - G^T(t). \tag{349}$$

Using the fact that both $\bar{\lambda}$ and G^N are both constant over time, linearizing (349) in the neighborhood of the steady-state yields:

$$\begin{aligned}\dot{B}(t) &= r^\star\left(B(t)-\tilde{B}\right)-\left(G(t)-\tilde{G}\right)\\ &= r^\star\left(B(t)-\tilde{B}\right)-\tilde{Y}ge^{-\xi t}.\end{aligned}$$

where we used the fact that $G^T(t)-\tilde{G}^T = G(t)-\tilde{G} = \tilde{Y}ge^{-\xi t}$. Solving leads to the general solution for the net foreign asset position:

$$B(t)-\tilde{B} = \left[\left(B_0-\tilde{B}\right)-\frac{\tilde{Y}g}{\xi+r^\star}\right]e^{r^\star t}+\frac{\tilde{Y}g}{\xi+r^\star}e^{-\xi t}. \tag{350}$$

Invoking the transversality condition gives the solution for $B(t)$:

$$B(t)-\tilde{B} = \frac{\tilde{Y}g}{\xi+r^\star}e^{-\xi t}, \tag{351}$$

consistent with the intertemporal solvency condition

$$\left(\tilde{B}-B_0\right) = -\frac{\tilde{Y}g}{\xi+r^\star}. \tag{352}$$

Setting $\dot{B}(t)=0$ into (349), totally differentiating and inserting (343) together with (346) allow us to determine the change in the equilibrium value of the marginal utility of wealth:

$$\begin{aligned}&r^\star\frac{d\tilde{B}}{\tilde{Y}}+(1-\alpha_L)\,\hat{\tilde{L}}^T = (1-\alpha_C)\,\omega_C\hat{\tilde{C}}^T,\\ &\hat{\tilde{\lambda}} = -\frac{\Psi}{\Gamma}r^\star\frac{d\tilde{B}}{\tilde{Y}},\end{aligned}$$

where $\Gamma>0$ is given by eq. (174). Substituting (352) into the above equation leads to the change in the equilibrium value of the marginal utility of wealth:

$$\hat{\tilde{\lambda}} = \frac{\Psi}{\Gamma}\frac{r^\star}{\xi+r^\star}g>0, \tag{353}$$

where $\Gamma>0$, $\Psi>0$, $\Upsilon_G^N>0$, $\xi>0$, and $g>0$. According to (353), an unanticipated temporary rise in G^T increases the shadow value of wealth and thus produces a negative wealth effect.

Inserting (353) into eq. (341) leads to the once-and-for-all decline in the relative price of non tradables:

$$\hat{P}(0) = \hat{\tilde{P}} = -\frac{[\alpha_L\sigma_L+\alpha_C\omega_C\sigma_C]}{\Psi}\frac{\Psi}{\Gamma}\frac{r^\star}{\xi+r^\star}g<0. \tag{354}$$

The depreciation in the relative price of non tradables along with the negative wealth effect which induces agents to supply more labor increases unambiguously traded hours worked:

$$\hat{L}^T(0) = \hat{\tilde{L}}^T = \left\{\sigma_L+\frac{\alpha_L(\epsilon-\sigma_L)[\alpha_L\sigma_L+\alpha_C\omega_C\sigma_C]}{\Psi}\right\}\frac{\Psi}{\Gamma}\frac{r^\star}{\xi+r^\star}g>0, \tag{355}$$

where we substituted (353) into (343). While the negative wealth effect exerts a positive impact on non traded hours worked, the depreciation in the relative price of non tradables has a negative effect on non traded hours worked:

$$\hat{L}^N = \left\{\sigma_L-\frac{[\epsilon(1-\alpha_L)+\alpha_L\sigma_L][\alpha_L\sigma_L+\alpha_C\omega_C\sigma_C]}{\Psi}\right\}\frac{\Psi}{\Gamma}\frac{r^\star}{\xi+r^\star}g \lesseqgtr 0. \tag{356}$$

In the special case where $\phi=\sigma_C=1$, non traded labor unambiguously falls under assumption 1 according to which $\epsilon>\sigma_L$.

Differentiating (351) with respect to time leads to the response of the current account:

$$\frac{\dot{B}(t)}{\tilde{Y}} = -\frac{\xi}{\xi + r^{\star}} g e^{-\xi t} < 0. \tag{357}$$

According to (357), a rise in G^T triggers a current account deficit and thus permanently lowers the net foreign asset position in the long-run.

Turning to the responses of sectoral output shares, the depreciation in the relative price of non tradables unambiguously lowers the output share of non tradables and increases the output share of tradables. Inserting (354) into (281) leads to the response of the output share of non tradables to a rise in G^T:

$$\begin{aligned} \alpha_L \left(\hat{Y}^N(0) - \hat{Y}_R(0) \right) &= \alpha_L (1-\alpha_L) \epsilon \hat{P}(0), \\ &= -\alpha_L (1-\alpha_L) \epsilon \frac{[\alpha_L \sigma_L + \alpha_C \omega_C \sigma_C]}{\Psi} \frac{\Psi}{\Gamma} \frac{r^{\star}}{\xi + r^{\star}} g < 0. \end{aligned} \tag{358}$$

Inserting (354) into (282) leads to the response of the output share of tradables to a rise in G^T:

$$\begin{aligned} (1-\alpha_L) \left(\hat{Y}^T(0) - \hat{Y}_R(0) \right) &= -\alpha_L (1-\alpha_L) \epsilon \hat{P}(0), \\ &= \alpha_L (1-\alpha_L) \epsilon \frac{[\alpha_L \sigma_L + \alpha_C \omega_C \sigma_C]}{\Psi} \frac{\Psi}{\Gamma} \frac{r^{\star}}{\xi + r^{\star}} g > 0. \end{aligned} \tag{359}$$

Finally, inserting (341) into (279) yields the one-for-and-all change in real GDP:

$$\begin{aligned} \hat{Y}_R &= \frac{\sigma_L}{\Psi} \left\{ \Psi - \alpha_L [\alpha_L \sigma_L + \alpha_C \omega_C \sigma_C] \right\}, \\ &= \frac{\sigma_L}{\Psi} \left\{ \alpha_L (1-\epsilon_L) + \omega_C \alpha_C [(1-\alpha_C) \phi - (\alpha_L - \alpha_C) \sigma_C] \right\} \gtrless 0, \end{aligned} \tag{360}$$

where we have inserted Ψ given by eq. (157).

Pre-multiplying eqs. (355) and (356) by $1-\alpha_L$ and α_L, respectively, and letting ϵ tend toward infinity lead to:

$$\lim_{\epsilon \to \infty} \alpha_L \hat{L}^N(0) = -\frac{\alpha_C \omega_C \sigma_C}{\sigma_L + \omega_C \sigma_C} \frac{r^{\star}}{\xi + r^{\star}} g < 0, \tag{361a}$$

$$\lim_{\epsilon \to \infty} (1-\alpha_L) \hat{L}^T(0) = \frac{\sigma_L + \alpha_C \omega_C \sigma_C}{\sigma_L + \omega_C \sigma_C} \frac{r^{\star}}{\xi + r^{\star}} g > 0. \tag{361b}$$

Letting ϵ tend toward infinity into eqs. (358) and (359) leads to the responses of output shares of non tradables and tradables, respectively, when we impose perfect mobility of labor across sectors:

$$\lim_{\epsilon \to \infty} \alpha_L \left(\hat{Y}^N(0) - \hat{Y}_R(0) \right) = -\frac{\alpha_L \sigma_L + \alpha_C \omega_C \sigma_C}{\sigma_L + \omega_C \sigma_C} \frac{r^{\star}}{\xi + r^{\star}} g < 0, \tag{362a}$$

$$\lim_{\epsilon \to \infty} (1-\alpha_L) \left(\hat{Y}^T(0) - \hat{Y}_R(0) \right) = \frac{\alpha_L \sigma_L + \alpha_C \omega_C \sigma_C}{\sigma_L + \omega_C \sigma_C} \frac{r^{\star}}{\xi + r^{\star}} g > 0. \tag{362b}$$

E.19 Government Spending Shock Split between Non Tradables and Tradables and Imperfect Mobility of Labor across Sectors: Proofs of Results in Section 4.2

So far, we have assumed that the rise in government spending is fully biased toward non tradables. In this subsection, we relax this assumption and assume that the rise in government spending is split between non tradables and tradables in accordance with their share in government spending:

$$\frac{dG(t)}{\tilde{Y}} = \omega_{G^N} \frac{dG(t)}{\tilde{Y}} + \omega_{G^T} \frac{dG(t)}{\tilde{Y}}. \tag{363}$$

The endogenous response of government spending to an exogenous fiscal shock is governed by eq. (258). We emphasize below the main changes with respect to those obtained when setting $\omega_{G^T} = 0$.

The short-run equilibrium is identical to (259). Adopting the same steps as in subsection E.13, the deviation in percentage from the initial steady-state for the relative price of non tradables now reads as follows:

$$\hat{P}(t) = \frac{-\left[\alpha_L \sigma_L + \alpha_C \omega_C \sigma_C\right]}{\Psi} \hat{\bar{\lambda}} + \frac{1}{\Psi} \omega_G^N \frac{dG(t)}{Y}, \tag{364}$$

where Ψ is given by (157). **Eq. (364) corresponds to eq. (30) in the main text**.

Solution for the Net Foreign Asset Position

Substituting $L^T(t) = (1-\alpha_L(t))\,(W(t))^{1+\sigma_L}\left(\bar{\lambda}\right)^{\sigma_L}$ and $C^T(t) = (1-\alpha_C)\,(P_C(t))^{1-\sigma_C}\,\bar{\lambda}^{-\sigma_C}$ into (259j) leads to:

$$\dot{B}(t) = r^\star B(t) + (1-\alpha_L(t))\,W(t)^{1+\sigma_L}\bar{\lambda}^{\sigma_L} - (1-\alpha_C(t))\,P_C(t)^{1-\sigma_C}\bar{\lambda}^{-\sigma_C} - G^T(t). \tag{365}$$

Using the fact that $\bar{\lambda}$ is constant over time, linearizing (365) in the neighborhood of the steady-state yields:

$$\begin{aligned}
\dot{B}(t) &= r^\star dB(t) - \tilde{L}^T \frac{\alpha_L(\epsilon-\sigma_L)}{\Psi}\omega_{G^N} dG(t) - \tilde{C}^T \frac{\alpha_C(\phi-\sigma_C)}{\Psi}\omega_{G^N} dG(t) - \omega_{G^T} dG(t), \\
&= r^\star dB(t) - \tilde{Y}\Upsilon_G g e^{-\xi t}.
\end{aligned}$$

where

$$\frac{\partial \dot{B}(t)}{\partial G(t)} = -\Upsilon_G \equiv -\left[\Upsilon_G^N \omega_{G^N} + \omega_{G^T}\right], \tag{366}$$

with

$$\Upsilon_G^N = \frac{\left[(1-\alpha_L)\,\alpha_L(\epsilon-\sigma_L) + (1-\alpha_C)\,\omega_C\alpha_C(\phi-\sigma_C)\right]}{\Psi} > 0. \tag{367}$$

It is worth mentioning that it is straightforward to show that

$$\Upsilon_G^N \leq 1, \quad \text{and} \quad \Upsilon_G^N < 1 \quad \text{if} \quad \epsilon < \infty. \tag{368}$$

Substituting the law of motion of government spending (258) and solving leads to the general solution for the net foreign asset position:

$$B(t) - \tilde{B} = \left[\left(B_0 - \tilde{B}\right) - \frac{\Upsilon_G \tilde{Y}}{\xi + r^\star} g\right] e^{r^\star t} + \frac{\Upsilon_G \tilde{Y}}{\xi + r^\star} g e^{-\xi t}. \tag{369}$$

Invoking the transversality condition gives the solution for $B(t)$:

$$B(t) - \tilde{B} = \frac{\Upsilon_G \tilde{Y}}{\xi + r^\star} g e^{-\xi t}, \tag{370}$$

consistent with the intertemporal solvency condition

$$\left(\tilde{B} - B_0\right) = -\frac{\Upsilon_G \tilde{Y}}{\xi + r^\star} g. \tag{371}$$

Eq. (370) corresponds to eq. (31) while eq. (371) corresponds to eq. (32) in the main text.

To determine the change in the equilibrium value of the marginal utility of wealth, we have to differentiate the market clearing condition (266) for the traded good evaluated at the steady-state (i.e., $\dot{B}(t) = 0$), using the fact that in the long-run government spending reverts to its initial level (i.e., $dG = 0$):

$$\begin{aligned}
&r^\star \frac{d\tilde{B}}{\tilde{Y}} + (1-\alpha_L)\,\hat{\tilde{L}}^T = (1-\alpha_C)\,\omega_C \hat{\tilde{C}}^T, \\
&\hat{\bar{\lambda}} = -\frac{\Psi}{\Gamma} r^\star \frac{d\tilde{B}}{\tilde{Y}},
\end{aligned}$$

where $\Gamma > 0$ is given by eq. (174). Substituting (371) into the above equation leads to the change in the equilibrium value of the marginal utility of wealth:

$$\hat{\bar{\lambda}} = \frac{\Psi \Upsilon_G}{\Gamma} \frac{r^\star}{\xi + r^\star} g > 0, \tag{372}$$

where $\Gamma > 0$, $\Psi > 0$, $\Upsilon_G > 0$, $\xi > 0$, and $g > 0$. **Eq. (372) corresponds to eq. (33) in the main text**.

Impact Effects of a Temporary Fiscal Expansion

Evaluating (364) at time $t = 0$, inserting (372), and using the fact that $\frac{dG(0)}{Y} = g > 0$, leads to the initial response of the relative price of non tradables:

$$\begin{aligned}
\hat{P}(0) &= \left\{\omega_{G^N} - \left[\alpha_L\sigma_L + \alpha_C\omega_C\sigma_C\right]\hat{\bar{\lambda}}\right\}\frac{g}{\Psi}, \\
&= \left\{\omega_{G^N} - \left[\alpha_L\sigma_L + \alpha_C\omega_C\sigma_C\right]\frac{\Psi\left[\Upsilon_G^N\omega_{G^N} + \omega_{G^T}\right]}{\Gamma}\frac{r^\star}{\xi + r^\star}\right\}\frac{g}{\Psi}, \\
&= \omega_{G^N}\left\{1 - \left[\alpha_L\sigma_L + \omega_C\alpha_C\sigma_C\right]\frac{\Upsilon_G^N\Psi}{\Gamma}\frac{r^\star}{\xi + r^\star}\right\}\frac{g}{\Psi} \\
&\quad - \left[\alpha_L\sigma_L + \omega_C\alpha_C\sigma_C\right]\frac{\Psi}{\Gamma}\frac{r^\star}{\xi + r^\star}\omega_{G^T}\frac{g}{\Psi} \gtrless 0.
\end{aligned} \tag{373}$$

The second line of eq. (373) corresponds to eq. (34) in the main text. When the rise in government spending, $G(t)$, is split between tradables and non tradables, the relative price of non tradables may appreciate or depreciate. For clarity purposes, let us consider two polar cases. If the government spending shock is fully biased toward non tradables, i.e., $\omega_{G^N} = 1$, then the second term on the RHS of eq. (373) vanishes. Due to inequality (272), i.e., $0 < \frac{\Psi\Upsilon_G^N}{\Gamma}\left(\alpha_L\sigma_L + \omega_C\alpha_C\sigma_C\right) < 1$, along with and $0 < \frac{r^\star}{\xi + r^\star} < 1$, a rise in $G(t)$ unambiguously appreciates the relative price of non tradables. Conversely, if the government spending shock is fully biased toward tradables, i.e., $\omega_{G^T} = 1$, then the first term on the RHS of eq. (373) vanishes. Thus, the relative price of non tradables depreciates. Intuitively, a rise in G^T while keeping G^N fixed, leads to a negative wealth effect which lowers C^N. As a result, an excess supply shows up in the non traded goods market which leads to a depreciation in the relative price of non tradables. Because $\hat{P}(0)$ is monotonically increasing with ω_{G^N}:

$$\frac{\partial\hat{P}(0)}{\partial\omega_{G^N}} = \hat{P}(0)\big|_{\omega_{G^N}=1} > 0, \tag{374}$$

where $\hat{P}(0)\big|_{\omega_{G^N}=1}$ is given by (273), there is a critical value $\bar{\omega}_{G^N}$ so that $\hat{P}(0) > 0$ for $\omega_{G^N} > \bar{\omega}_{G^N}$.

Substituting the change in the equilibrium value of the marginal utility of wealth given by eq. (372) into (265), and multiplying both sides by α_L leads to the initial reaction of non traded labor from initial steady-state in total labor units:

$$\alpha_L\hat{L}^N(0) = \alpha_L\left[\epsilon\left(1 - \alpha_L\right) + \alpha_L\sigma_L\right]\hat{P}(0) + \alpha_L\sigma_L\frac{\Psi\Upsilon_G}{\Gamma}\frac{r^\star}{\xi + r^\star}g > 0, \tag{375}$$

where $\hat{P}(0) \gtrless 0$.

Substituting the change in the equilibrium value of the marginal utility of wealth given by eq. (372) into (264) and multiplying both sides by $1 - \alpha_L$ leads to the initial reaction of traded labor from initial steady-state in total labor units:

$$\left(1 - \alpha_L\right)\hat{L}^T(0) = -\left(1 - \alpha_L\right)\alpha_L\left(\epsilon - \sigma_L\right)\hat{P}(0) + \left(1 - \alpha_L\right)\sigma_L\frac{\Psi\Upsilon_G}{\Gamma}\frac{r^\star}{\xi + r^\star}g \lessgtr 0, \tag{376}$$

where $\hat{P}(0) \gtrless 0$.

Inserting (373) into (281), the response of the share of non tradables in real GDP to a government spending shock is given by:

$$\begin{aligned}
\alpha_L\left(\hat{Y}^N(0) - \hat{Y}_R(0)\right) &= \alpha_L\left(1 - \alpha_L\right)\epsilon\hat{P}(0), \\
&= \frac{\alpha_L\left(1 - \alpha_L\right)\epsilon}{\Psi}\left[\omega_{G^N} - \left[\alpha_L\sigma_L + \omega_C\alpha_C\sigma_C\right]\frac{\Upsilon_G\Psi}{\Gamma}\frac{r^\star}{\xi + r^\star}\right\}g,
\end{aligned} \tag{377}$$

where $\Upsilon_G = \Upsilon_G^N\omega_{G^N} + \omega_{G^T} > 0$. **Eq. (377) corresponds to eq. (36) in the main text.**

Differentiating (370) with respect to time leads to the response of the current account as a percentage of GDP:

$$\frac{\dot{B}(t)}{\tilde{Y}} = -\Upsilon_G \frac{\xi}{\xi + r^\star} g e^{-\xi t} < 0, \tag{378}$$

where $\Upsilon_G > 0$.

Relationship between and $\alpha_L \left(\hat{Y}^N(0) - \hat{Y}_R(0)\right)$ and ϵ

In subsection E.20, we have proved that $\frac{\partial \alpha_L \left(\hat{Y}^N(0) - \hat{Y}_R(0)\right)}{\partial \epsilon} > 0$. We now provide a formal proof that this positive relationship holds with $0 < \omega_{G^N} < 1$. As shown in eq. (307), we must have $0 < -\frac{\partial \hat{P}(0)}{\partial \epsilon} \frac{\epsilon}{\hat{P}(0)} < 1$. We thus totally differentiate (373) with respect to ϵ and multiply the result by $\epsilon / \hat{P}(0)$:

$$\begin{aligned} -\frac{\partial \hat{P}(0)}{\partial \epsilon} \frac{\epsilon}{\hat{P}(0)} &= \frac{\omega_{G^N} \hat{P}(0)|_{\omega_{G^N}=1}}{\hat{P}(0)} \left(-\frac{\partial \hat{P}(0)}{\partial \epsilon} \frac{\epsilon}{\hat{P}(0)} \right) \Big|_{\omega_{G^N}=1} \\ &\quad - \frac{1}{\hat{P}(0)} \left[\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C \right] \frac{\omega_{G^T} g}{\Gamma} \frac{r^\star}{\xi + r^\star} \frac{\partial \Gamma}{\partial \epsilon} \frac{\epsilon}{\Gamma}, \end{aligned} \tag{379}$$

where $\left(-\frac{\partial \hat{P}(0)}{\partial \epsilon} \frac{\epsilon}{\hat{P}(0)} \right) \Big|_{\omega_{G^N}=1}$ is given by (310) when $\xi \to \infty$ and (319) when $\xi \to 0$.

A Weakly Persistent Fiscal Shock: $\xi \to \infty$

Letting $\xi \to \infty$ into eq. (379) leads to:

$$0 < -\frac{\partial \hat{P}(0)\big|_{\xi \to \infty}}{\partial \epsilon} \frac{\epsilon}{\hat{P}(0)\big|_{\xi \to \infty}} = \frac{\alpha_L (1 - \alpha_L) \epsilon}{\Psi} < 1. \tag{380}$$

Thus, whether we assume that the government shock is fully biased toward non tradables or is split between non tradables and tradables, the elasticity of the response of the relative price w.r.t the degree of labor mobility across sectors is identical because the wealth effect vanishes and thus a rise in G^T has no effect on the relative price.

A Highly Persistent Fiscal Shock: $\xi \to 0$

As shall be useful, we compute the following term:

$$\frac{\partial \Gamma}{\partial \epsilon} \frac{\epsilon}{\Gamma} = \alpha_L (1 - \alpha_L) \epsilon \frac{(\sigma_L + \omega_C \sigma_C)}{\Gamma} < 1, \tag{381}$$

where Γ is given by eq. (174). Making use of (319), eq. (379) can be rewritten as follows:

$$\begin{aligned} -\frac{\partial \hat{P}(0)}{\partial \epsilon} \frac{\epsilon}{\hat{P}(0)} &= \frac{\omega_{G^N} \hat{P}(0)|_{\omega_{G^N}=1} - \left[\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C \right] \frac{\omega_{G^T} g}{\Gamma}}{\hat{P}(0)} \alpha_L (1 - \alpha_L) \epsilon \frac{(\sigma_L + \omega_C \sigma_C)}{\Gamma}, \\ &= \alpha_L (1 - \alpha_L) \epsilon \frac{(\sigma_L + \omega_C \sigma_C)}{\Gamma}. \end{aligned} \tag{382}$$

In sum, whether we assume $\omega_{G^N} = 1$ or $0 < \omega_{G^N} < 1$, when ξ takes intermediate values, the elasticity falls into the following range of values:

$$-\frac{\partial \hat{P}(0)}{\partial \epsilon} \frac{\epsilon}{\hat{P}(0)} \in \left\{ \frac{\alpha_L (1 - \alpha_L) \epsilon}{\Psi}, \frac{\alpha_L (1 - \alpha_L) \epsilon}{\Psi} \left[1 + \frac{(\alpha_L \sigma_L + \omega_C \alpha_C \sigma_C)^2}{\Gamma} \right] \right\}. \tag{383}$$

Finally, we show in subsection E.20 that $\alpha_L \left(\hat{Y}^N(0) - \hat{Y}_R(0)\right) > (\omega_{G^N} - \alpha_L) g > 0$ because we need analytical results when imposing perfect mobility of labor across sectors to demonstrate this result when allowing for imperfect mobility of labor.

E.20 Government Spending Shock Split Between Non Tradables and Tradables and Perfect Mobility of Labor across Sectors

We now consider a rise in government spending split between non tradables and tradables in the special case of perfect mobility of labor across sectors. We emphasize the main changes. Totally differentiating (285), using (284), leads to:

$$\alpha_L \hat{L}^N(t) = -\alpha_C \omega_C \sigma_C \hat{\bar{\lambda}} + \omega_{G^N} \frac{dG(t)}{Y}. \tag{384}$$

Inserting $L = \bar{\lambda}^{\sigma_L}$ (since $W = 1$) into (283h), differentiating and using (384) leads to:

$$(1-\alpha_L)\,\hat{L}^T(t) = [\sigma_L + \alpha_C\omega_C\sigma_C]\,\hat{\bar{\lambda}} - \omega_{G^N}\frac{dG(t)}{Y}. \tag{385}$$

Inserting $L^T = L - L^N$ together with $L^N = C^N + G^N$ and $L = \bar{\lambda}^{\sigma_L}$ (since $W = 1$) into (283j), the market clearing condition for the traded good can be written as follows:

$$\begin{aligned}\dot{B}(t) &= r^\star B(t) + L - P_C C - G^T(t) - PG^N(t), \\ &= r^\star B(t) + \bar{\lambda}^{\sigma_L} - (1-\alpha_C)\,P_C^{1-\sigma_C}\bar{\lambda}^{-\sigma_C} - PG^N(t) - G^T(t).\end{aligned} \tag{386}$$

Using the fact that both $\bar{\lambda}$ and P are constant over time, linearizing (386) in the neighborhood of the steady-state leads to:

$$\dot{B}(t) = r^\star dB(t) - dG(t).$$

Substituting the law of motion of government spending (258) and solving leads to the general solution for the net foreign asset position as described by eq. (289). The stable solution for the net foreign asset position and the intertemporal solvency condition are identical to (290) and (291), respectively. Thus, the change in the equilibrium value of the marginal utility of wealth is identical as well to eq. (292).

Real GDP is equal to the sum of sectoral value added evaluated at constant prices:

$$Y_R = L^T + P_0 L^N. \tag{387}$$

Totally differentiating (387) and substituting both (384) and (385) leads to:

$$\begin{aligned}\hat{Y}_R &= \alpha_L\hat{L}^N + (1-\alpha_L)\,\hat{L}^T, \\ &= \sigma_L\hat{\bar{\lambda}} > 0.\end{aligned} \tag{388}$$

Evaluating (384) at time $t = 0$ and inserting (388), and then substituting (292), the response of the output share of non tradables is given by:

$$\begin{aligned}\alpha_L\left(\hat{Y}^N(0) - \hat{Y}_R(0)\right) &= \left[\omega_{G^N} g - (\alpha_L\sigma_L + \omega_C\alpha_C\sigma_C)\,\hat{\bar{\lambda}}\right], \\ &= \left[\omega_{G^N} - \left(\frac{\alpha_L\sigma_L + \omega_C\alpha_C\sigma_C}{\sigma_L + \omega_C\sigma_C}\right)\frac{r^\star}{\xi + r^\star}\right] g \gtrless 0.\end{aligned} \tag{389}$$

Letting ϵ tend toward infinity into eq. (377), using (294), i.e., $\lim_{\epsilon\to\infty}\frac{\Psi\Upsilon_G^N}{\Gamma} = \frac{1}{\sigma_L+\omega_C\sigma_C}$, and using the fact that $\lim_{\epsilon\to\infty}\frac{\Psi}{\Gamma} = \frac{1}{\sigma_L+\omega_C\sigma_C}$ since $\lim_{\epsilon\to\infty}\Upsilon_G^N = 1$ (see eq. (293)), and applying l'Hôpital's rule leads to eq. (389) since $\lim_{\epsilon\to\infty}\frac{\alpha_L(1-\alpha_L)\epsilon}{\Psi} = 1$. **Eq. (389) corresponds to eq. (36) in the main text.**

As shown in section C.2, keeping the private demand components fixed, the response of the share of non tradables in real GDP is given by $\alpha_L\left(\hat{Y}^N(0) - \hat{Y}_R(0)\right) = (\omega_{G^N} - \alpha_L)\frac{dG(t)}{Y}$ (see eq. (103)), where in terms of section C.2, we have $\alpha_L = \nu^{Y,N}$. In a general equilibrium model, the private sector' demand components respond to a fiscal shock and thus the response of the share of non tradables in real GDP deviates from $(\omega_{G^N} - \alpha_L)\frac{dG(t)}{Y}$. To calculate the extent of the discrepancy between the response of the share of non tradables in real GDP described by eq. (389) and that when keeping private sector's demand components fixed as described by eq. (103), we add and subtract α_L in the RHS of eq. (389):

$$\alpha_L\left(\hat{Y}^N(0) - \hat{Y}_R(0)\right) = \left\{(\omega_{G^N} - \alpha_L) + \left[\alpha_L - \left(\frac{\alpha_L\sigma_L + \omega_C\alpha_C\sigma_C}{\sigma_L + \omega_C\sigma_C}\right)\frac{r^\star}{\xi + r^\star}\right]\right\} g. \tag{390}$$

where

$$\left[\alpha_L - \left(\frac{\alpha_L\sigma_L + \omega_C\alpha_C\sigma_C}{\sigma_L + \omega_C\sigma_C}\right)\frac{r^\star}{\xi + r^\star}\right] > 0. \tag{391}$$

The RHS of eq. (391) is unambiguously positive since $\alpha_L \geq \alpha_C$ as our evidence suggest and $0 < \frac{r^\star}{\xi+r^\star} < 1$. According to (390), the share of non tradables in real GDP unambiguously rises as long as $\omega_{G^N} > \alpha_L$. As captured by the positive term (391), the share of non tradables in real GDP increases more in a general equilibrium model where demand components adjust in response to a fiscal shock because the rise in government spending triggers a fall in net exports on impact which further biases the sectoral demand shock toward non tradables.

While $\alpha_L \left(\hat{Y}^N(0) - \hat{Y}_R(0)\right)$ is larger than $(\omega_{G^N} - \alpha_L)\, g$ when $\epsilon \to \infty$ due to inequality (391), we now show that $\alpha_L \left(\hat{Y}^N(0) - \hat{Y}_R(0)\right) > (\omega_{G^N} - \alpha_L)\, g > 0$ holds as well with imperfect mobility of labor across sectors. First, since $\lim_{\epsilon\to\infty} \frac{\Psi\Upsilon_G^N}{\Gamma} = \frac{1}{\sigma_L+\omega_C\sigma_C}$ (294) and $\frac{\partial \frac{\Psi\Upsilon_G^N}{\Gamma}}{\partial\epsilon} > 0$ (see eq. (304)), we thus have:

$$\begin{aligned}
\frac{\Psi\Upsilon_G^N}{\Gamma} &\leq \frac{1}{\sigma_L + \omega_C\sigma_C}, \\
\frac{\Psi\Upsilon_G^N}{\Gamma}\left(\alpha_L\sigma_L + \alpha_C\omega_C\sigma_C\right) &\leq \frac{\alpha_L\sigma_L + \alpha_C\omega_C\sigma_C}{\sigma_L + \omega_C\sigma_C}, \\
\frac{\Psi\Upsilon_G^N\omega_{G^N}}{\Gamma}\left(\alpha_L\sigma_L + \alpha_C\omega_C\sigma_C\right) &\leq \frac{\alpha_L\sigma_L + \alpha_C\omega_C\sigma_C}{\sigma_L + \omega_C\sigma_C}\omega_{G^N}.
\end{aligned} \tag{392}$$

Second, since $\lim_{\epsilon\to\infty} \Upsilon_G^N = 1$ (see eq. (293)) and $\frac{\partial\Upsilon_G^N}{\partial\epsilon} > 0$ (see eq. (302)), the first line of (392) implies the following inequalities:

$$\begin{aligned}
\frac{\Psi}{\Gamma} &\leq \frac{1}{\sigma_L + \omega_C\sigma_C}, \\
\frac{\Psi}{\Gamma}\left(\alpha_L\sigma_L + \alpha_C\omega_C\sigma_C\right) &\leq \frac{\alpha_L\sigma_L + \alpha_C\omega_C\sigma_C}{\sigma_L + \omega_C\sigma_C}, \\
\frac{\Psi\omega_{G^T}}{\Gamma}\left(\alpha_L\sigma_L + \alpha_C\omega_C\sigma_C\right) &\leq \frac{\alpha_L\sigma_L + \alpha_C\omega_C\sigma_C}{\sigma_L + \omega_C\sigma_C}\omega_{G^T}.
\end{aligned} \tag{393}$$

Combining (392) and (393) leads to:

$$\begin{aligned}
\frac{\Psi\left[\Upsilon_G^N\omega_{G^N} + \omega_{G^T}\right]}{\Gamma}\left[\alpha_L\sigma_L + \alpha_C\omega_C\sigma_C\right] &\leq \frac{\alpha_L\sigma_L + \alpha_C\omega_C\sigma_C}{\sigma_L + \omega_C\sigma_C}\left(\omega_{G^N} + \omega_{G^T}\right), \\
\frac{\Psi\left[\Upsilon_G^N\omega_{G^N} + \omega_{G^T}\right]}{\Gamma}\left[\alpha_L\sigma_L + \alpha_C\omega_C\sigma_C\right] &\leq \frac{\alpha_L\sigma_L + \alpha_C\omega_C\sigma_C}{\sigma_L + \omega_C\sigma_C},
\end{aligned} \tag{394}$$

where we used the fact that $\omega_{G^N} + \omega_{G^T} = 1$. From inequalities (391) and (394), we thus have:

$$\alpha_L \left(\hat{Y}^N(0) - \hat{Y}_R(0)\right) > (\omega_{G^N} - \alpha_L)\, g, \tag{395}$$

whether $\epsilon \to \infty$ or $0 < \epsilon < \infty$.

F Solving the Model with Physical Capital

This section extends the two-sector model with imperfect mobility of labor to physical capital accumulation which is subject to installation costs.

F.1 Household's Maximization Problem

At each instant of time, the representative household consumes traded and non traded goods denoted by C^T and C^N, respectively, which are aggregated by means of a CES function:

$$C = \left[\varphi^{\frac{1}{\phi}}\left(C^T\right)^{\frac{\phi-1}{\phi}} + (1-\varphi)^{\frac{1}{\phi}}\left(C^N\right)^{\frac{\phi-1}{\phi}}\right]^{\frac{\phi}{\phi-1}}, \tag{396}$$

where $0 < \varphi < 1$ is the weight of the traded good in the overall consumption bundle and ϕ corresponds to the elasticity of substitution between traded goods and non traded goods.

As in De Cordoba and Kehoe [2000], the investment good is produced using inputs of the traded good and the non traded good according to a constant-returns-to-scale function which is assumed to take a CES form:

$$J = \left[\varphi_J^{\frac{1}{\phi_J}} \left(J^T\right)^{\frac{\phi_J - 1}{\phi_J}} + (1 - \varphi_J)^{\frac{1}{\phi_J}} \left(J^N\right)^{\frac{\phi_J - 1}{\phi_J}}\right]^{\frac{\phi_J}{\phi_J - 1}}, \tag{397}$$

where φ_J is the weight of the investment traded input ($0 < \varphi_J < 1$) and ϕ_J corresponds to the intratemporal elasticity of substitution in investment between traded and non traded inputs.

Following Horvath [2000], we assume that hours worked in the traded and the non traded sectors are aggregated by means of a CES function:

$$L = \left[\vartheta^{-1/\epsilon} \left(L^H\right)^{\frac{\epsilon+1}{\epsilon}} + (1 - \vartheta)^{-1/\epsilon} \left(L^N\right)^{\frac{\epsilon+1}{\epsilon}}\right]^{\frac{\epsilon}{\epsilon+1}}, \tag{398}$$

where $0 < \vartheta < 1$ is the weight of labor supply to the traded sector in the labor index $L(.)$ and ϵ measures the ease with which hours worked can be substituted for each other and thereby captures the degree of labor mobility across sectors.

The representative household chooses consumption, decides on labor supply, and investment that maximizes his/her lifetime utility:

$$U = \int_0^\infty \left\{ \frac{1}{1 - \frac{1}{\sigma_C}} C(t)^{1 - \frac{1}{\sigma_C}} - \frac{1}{1 + \frac{1}{\sigma_L}} L(t)^{1 + \frac{1}{\sigma_L}} \right\} e^{-\beta t} \mathrm{d}t, \tag{399}$$

subject to the flow budget constraint:

$$\dot{B}(t) = r^\star B(t) + R(t)K(t) + W(t)L(t) - T(t) - P_C\left(P(t)\right)C(t) - P_J\left(P(t)\right)J(t), \tag{400}$$

and capital accumulation which evolves as follows:

$$\dot{K}(t) = I(t) - \delta_K K(t), \tag{401}$$

where I is investment and $0 \leq \delta_K < 1$ is a fixed depreciation rate. The first term on the RHS of (400) $r^\star B(t) + R(t)K(t) + W\left(W^T(t), W^N(t)\right)L(t) - T(t)$ is the representative household's real disposable income while the second term on the RHS $P_C\left(P(t)\right)C(t) + P_J\left(P(t)\right)J(t)$ corresponds to consumption and investment expenditure including capital installation costs. More specifically, we assume that capital accumulation is subject to increasing and convex cost of net investment, $I(t) - \delta_K K(t)$:

$$J(t) = I(t) + \Psi\left(I(t), K(t)\right)K(t), \tag{402}$$

where $\Psi(.)$ is increasing (i.e., $\Psi'(.) > 0$), convex (i.e., $\Psi''(.) > 0$), is equal to zero at δ_K (i.e., $\Psi(\delta_K) = 0$), and has first partial derivative equal to zero as well at δ_K (i.e., $\Psi'(\delta_K) = 0$). We suppose the following functional form for the adjustment cost function:

$$\Psi\left(I(t), K(t)\right) = \frac{\kappa}{2}\left(\frac{I(t)}{K(t)} - \delta_K\right)^2. \tag{403}$$

Using (404), partial derivatives of total investment expenditure are:

$$\frac{\partial J(t)}{\partial I(t)} = 1 + \kappa\left(\frac{I(t)}{K(t)} - \delta_K\right), \tag{404a}$$

$$\frac{\partial J(t)}{\partial K(t)} = -\frac{\kappa}{2}\left(\frac{I(t)}{K(t)} - \delta_K\right)\left(\frac{I(t)}{K(t)} + \delta_K\right). \tag{404b}$$

Denoting the co-state variables associated with (404a) and (404b) by λ and Q', respectively, the first-order conditions characterizing the representative household's optimal plans are:

$$C(t) = (P_C(t)\lambda)^{-\sigma_C}\,, \tag{405a}$$
$$L(t) = (W(t)\lambda)^{\sigma_L}\,, \tag{405b}$$
$$Q(t) = P_J(t)\left[1+\kappa\left(\frac{I(t)}{K(t)}-\delta_K\right)\right], \tag{405c}$$
$$\dot{\lambda}(t) = \lambda\left(\beta - r^{\star}\right), \tag{405d}$$
$$\dot{Q}(t) = \left(r^{\star}+\delta_K\right)Q(t) - \left\{R(t) + P_J(t)\frac{\kappa}{2}\left(\frac{I(t)}{K(t)}-\delta_K\right)\left(\frac{I(t)}{K(t)}+\delta_K\right)\right\}, \tag{405e}$$

and the transversality conditions $\lim_{t\to\infty}\bar{\lambda}B(t)e^{-\beta t}=0$ and $\lim_{t\to\infty}Q(t)K(t)e^{-\beta t}=0$; to derive (405c) and (405e), we used the fact that $Q(t)=Q'(t)/\lambda(t)$.

Since preferences over both goods embodied in the the consumption index (396) are homothetic, an exact consumption price index can be derived which we denote by P_C:

$$P_C = \left[\varphi + (1-\varphi)\left(P\right)^{1-\phi}\right]^{\frac{1}{1-\phi}}, \tag{406}$$

Given the consumption-based price index (406) and applying Shephard's lemma (or the envelope theorem), i.e, $C^N = \frac{\partial P_C}{\partial P}C = P_C'C$ and $C^T = \left(P_C - PP_C'\right)C$, yields the following demand of traded and non traded goods:

$$C^T = \varphi\left(\frac{1}{P_C}\right)^{-\phi}C, \tag{407a}$$
$$C^N = (1-\varphi)\left(\frac{P}{P_C}\right)^{-\phi}C, \tag{407b}$$
$$\tag{407c}$$

Combining (407a) and (407b) leads to the optimal intratemporal allocation of expenditure between traded and non traded goods:

$$\left(\frac{\varphi}{1-\varphi}\right)\frac{C^N}{C^T} = P^{-\phi}, \tag{408}$$

where P is the relative price of non-tradables and ϕ captures the extent to which consumers are willing to raise C^T/C^N when P appreciates by 1%. Denoting by α_C the non tradable content of consumption expenditure defined as follows:

$$\alpha_C \;=\; (1-\varphi)\left(\frac{P}{P_C}\right)^{1-\phi},, \tag{409a}$$
$$1-\alpha_C \;=\; \varphi\left(\frac{1}{P_C}\right)^{1-\phi}, \tag{409b}$$

consumption expenditure in non tradables and tradables can be rewritten as $PC^N = \alpha_C P_C C$ and $C^T = \left(1-\alpha_C\right)P_C C$, respectively.

The same logic applies to intratemporal decisions for investment inputs. Given the CES aggregator function (397), we can derive the appropriate price index for investment which we denote by P_J:

$$P_J = \left[\varphi_J + (1-\varphi_J)\left(P\right)^{1-\phi_J}\right]^{\frac{1}{1-\phi_J}}. \tag{410}$$

Applying the envelope theorem, i.e., $J^N = \frac{\partial P_J}{\partial P}J = P_J'J$, we can derive the demand for inputs of the traded good and the non traded good:

$$J^T = \varphi_J\left(\frac{1}{P_J}\right)^{-\phi_J}J, \tag{411a}$$
$$J^N = (1-\varphi_J)\left(\frac{1}{P_J}\right)^{-\phi_J}J. \tag{411b}$$

Combining (411a) and (411b) leads to the optimal intratemporal allocation of expenditure between traded and non traded goods:

$$\left(\frac{\varphi_J}{1-\varphi_J}\right)\frac{J^N}{J^T} = P^{-\phi_J}, \tag{412}$$

where ϕ_J is the elasticity of substitution between tradables and non tradables for investment. Denoting by α_J the non tradable content of expenditure expenditure defined as follows:

$$\alpha_J = (1-\varphi_J)\left(\frac{P}{P_J}\right)^{1-\phi_J}, , \tag{413a}$$

$$1-\alpha_J = \varphi_J\left(\frac{1}{P_J}\right)^{1-\phi_J}, \tag{413b}$$

investment expenditure in non tradables and tradables can be rewritten as $PJ^N = \alpha_J P_J J$ and $J^T = (1-\alpha_J) P_J J$, respectively.

As will be useful later, the percentage change in the consumption and investment price index is proportional to the appreciation in the relative price of non tradables since terms of trade are assumed exogenous:

$$\hat{P}_C = \alpha_C \hat{P}, \tag{414a}$$

$$\hat{P}_J = \alpha_J \hat{P}. \tag{414b}$$

The aggregate wage index, $W(t)$, associated with the labor index defined above (398) is:

$$W = \left[\vartheta\left(W^T\right)^{\epsilon+1} + (1-\vartheta)\left(W^N\right)^{\epsilon+1}\right]^{\frac{1}{\epsilon+1}}, \tag{415}$$

where W^T and W^N are wages paid in the traded and the non traded sectors, respectively. Given the aggregate wage index (415) and applying the envelope theorem, i.e., $L^T = \frac{\partial W(W^T,W^N)}{\partial W^T}L$ and $L^N = \frac{\partial W(W^T,W^N)}{\partial W^N}L$, we can derive the allocation of aggregate labor supply to the traded and the non traded sector:

$$L^T = \vartheta\left(\frac{W^H}{W}\right)^{\epsilon} L, \tag{416a}$$

$$L^N = (1-\vartheta)\left(\frac{W^N}{W}\right)^{\epsilon} L. \tag{416b}$$

As will be useful later, the percentage change in the aggregate wage index is a weighted average of percentage changes in sectoral wages:

$$\hat{W} = (1-\alpha_L)\hat{W}^H + \alpha_L \hat{W}^N, \tag{417}$$

where α_L is the non tradable content of aggregate labor compensation:

$$\alpha_L = (1-\vartheta)\left(\frac{W^N}{W}\right)^{1+\epsilon}, \tag{418a}$$

$$1-\alpha_L = \vartheta\left(\frac{W^T}{W}\right)^{1+\epsilon}. \tag{418b}$$

Combining (416a) and (416b) leads to the optimal allocation of hours worked to the traded and the non traded sector:

$$\left(\frac{\vartheta}{1-\vartheta}\right)\frac{L^N}{L^T} = \Omega^{\epsilon}, \tag{419}$$

where $\Omega \equiv W^N/W^T$ is the relative wage and ϵ captures the extent to which workers are willing to shift hours worked toward the non traded sector when Ω rises by 1%.

F.2 Firm's Maximization Problem

Each sector $j = T, N$ uses physical capital, K^j, and labor, L^j, according to constant returns to scale production functions:

$$Y^j = Z^j \left(L^j\right)^{\theta^j} \left(K^j\right)^{1-\theta^j}, \tag{420}$$

where θ^j is the labor income share in sector j and Z^j corresponds to the total factor productivity index which is introduced for calibration purposes. Both sectors face two cost components: a capital rental cost equal to R, and a labor cost equal to the wage rate, i.e., W^T in the traded sector and W^N in the non traded sector. Both sectors are assumed to be perfectly competitive.

Since capital can move freely between the two sectors while the shift of labor across sectors is costly, only marginal products of capital in the traded and the non traded sector equalize:

$$Z^T \left(1-\theta^T\right) \left(k^T\right)^{-\theta^T} = P Z^N \left(1-\theta^N\right) \left(k^N\right)^{-\theta^N} \equiv R, \tag{421a}$$

$$Z^T \theta^T \left(k^T\right)^{1-\theta^T} \equiv W^T, \tag{421b}$$

$$P Z^N \theta^N \left(k^N\right)^{1-\theta^N} \equiv W^N, \tag{421c}$$

where the capital-labor ratio for sector $j = T, N$ is denoted by $k^j \equiv K^j/L^j$. These static efficiency conditions state that the value of the marginal product of labor in sector j is equal to the labor cost W^j while the value of the marginal product of capital in the traded and the non traded sector must be equal to the capital rental cost, R.

Aggregating over the two sectors gives us the resource constraint for capital:

$$K^T + K^N = K. \tag{422}$$

F.3 Solving the Model

Before linearizing, we have to determine short-run static solutions. Static efficiency conditions (405a) and (405b) can be solved for consumption and labor which of course must hold at any point of time:

$$C = C\left(\bar{\lambda}, P\right), \quad L = L\left(\bar{\lambda}, W^T, W^N\right), \tag{423}$$

with

$$\hat{C} \;=\; = -\sigma_C \hat{\bar{\lambda}} - \alpha_C \sigma_C \frac{C}{P}, \tag{424a}$$

$$\hat{L} \;=\; \sigma_L \hat{\bar{\lambda}} + \sigma_L \left(1-\alpha_L\right) \hat{W}^T + \sigma_L \alpha_L \hat{W}^N, \tag{424b}$$

where we made use of (414a) and (417); σ_C and σ_L correspond to the intertemporal elasticity of substitution for consumption and labor, respectively. A rise in the shadow value of wealth induces agents to cut their real expenditure and to supply more labor. By raising the consumption price index, an appreciation in the relative price of non tradables drives down consumption. A rise in sectoral wage rates increases the aggregate wage index which provides an incentive to increase hours worked.

Inserting first the optimal decision for consumption (405a) into demand for traded and non traded goods described by (407a) and (407b) gives the short-run static solutions for C^T and C^N:

$$C^T = C^T\left(\bar{\lambda}, P\right), \quad C^N = C^N\left(\bar{\lambda}, P\right), \tag{425}$$

with partial derivatives given by

$$\hat{C}^T \;=\; -\sigma_C \hat{\bar{\lambda}} + \alpha_C \left(\phi - \sigma_C\right) \hat{P}, \tag{426a}$$

$$\hat{C}^N \;=\; -\sigma_C \hat{\bar{\lambda}} - \left[\left(1-\alpha_C\right)\phi + \alpha_C \sigma_C\right] \hat{P}, \tag{426b}$$

where we used the fact that $-\frac{P''_C P}{P'_C} = \phi(1-\alpha_C) > 0$ and $P'_C C = C^N$. A rise in the shadow value of wealth lowers both C^T and C^N. An appreciation in P lowers unambiguously C^N and increases C^T if $\phi > \sigma_C$.

Inserting first the optimal decision for labor supply (405b) into optimal supply of hours worked to the traded (416a) and the non traded sector (416b), enables us to solve for L^T and L^N:

$$L^T = L^T\left(\bar{\lambda}, W^T, W^N\right), \quad L^N = L^N\left(\bar{\lambda}, W^T, W^N\right), \tag{427}$$

with partial derivatives given by:

$$\hat{L}^T = \sigma_L \hat{\bar{\lambda}} + \left[\epsilon\alpha_L + \sigma_L(1-\alpha_L)\right]\hat{W}^T - \alpha_L(\epsilon - \sigma_L)\hat{W}^N, \tag{428a}$$

$$\hat{L}^N = \sigma_L \hat{\bar{\lambda}} + \left[\epsilon(1-\alpha_L) + \sigma_L\alpha_L\right]\hat{W}^N - (1-\alpha_L)(\epsilon - \sigma_L)\hat{W}^T, \tag{428b}$$

$$\tag{428c}$$

where we used the fact that $\frac{W_{TT}W^T}{W_T} = \epsilon\alpha_L$, $\frac{W_{TN}W^N}{W_T} = -\epsilon\alpha_L$, $\frac{W_{NN}W^N}{W_N} = \epsilon(1-\alpha_L)$, $\frac{W_{NT}W^T}{W_N} = -\epsilon(1-\alpha_L)$. The interpretation of these results deserves attention. A rise in the shadow value of wealth induces agents to supply more labor in both sectors. When the traded sector pays higher wages, i.e., W^T rises, workers supply more labor in that sector. Higher wages in the traded sector exerts opposite effects on L^N. On the one hand, because increased W^T raises the aggregate wage index in proportion to $(1-\alpha_L)$, workers are encouraged to supply more labor which in turn increases L^N (and L^T). On the other hand, if the cost of switching sectors is not too high, i.e., if the values of ϵ are not too low, workers are encouraged to reallocate hours worked toward the traded sector. If $\epsilon > \sigma_L$, a rise in W^T lowers L^N. The same logic applies when analyzing the effect of a rise in W^N.

Plugging the short-run static solutions for L^T and L^N given by (427) into the resource constraint for capital (422), the system of four equations consisting of (421a)-(421c) together with (422) can be solved for the sectoral wage rates W^j and sectoral capital-labor ratios k^j. Keeping TFPs unchanged, and log-differentiating (421a)-(421c) together with (422) yields in matrix form:

$$\begin{pmatrix} -\theta^T & \theta^N & 0 & 0 \\ \left(1-\theta^T\right) & 0 & -1 & 0 \\ 0 & \left(1-\theta^N\right) & 0 & -1 \\ (1-\xi) & \xi & \Psi_{W^T} & \Psi_{W^N} \end{pmatrix} \begin{pmatrix} \hat{k}^T \\ \hat{k}^N \\ \hat{W}^T \\ \hat{W}^N \end{pmatrix}$$

$$= \begin{pmatrix} \hat{P} \\ 0 \\ -\hat{P} \\ \hat{K} - \Psi_{\bar{\lambda}}\hat{\bar{\lambda}} \end{pmatrix}, \tag{429}$$

where we set:

$$\Psi_{W^T} = \left(1-\xi^N\right)\frac{L^T_{W^T}W^T}{L^T} + \xi^N\frac{L^N_{W^T}W^T}{L^N}, \tag{430a}$$

$$\Psi_{W^N} = \left(1-\xi^N\right)\frac{L^T_{W^N}W^N}{L^T} + \xi^N\frac{L^N_{W^N}W^N}{L^N}, \tag{430b}$$

$$\xi^N \equiv \frac{k^N L^N}{K}, \tag{430c}$$

$$\Psi_{\bar{\lambda}} = \left(1-\xi^N\right)\sigma_L + \xi^N\sigma_L = \sigma_L. \tag{430d}$$

The determinant of (429) is:

$$G \equiv -\left\{\theta^T\left[\left(1-\theta^N\right)\Psi_{W^N} + \xi^N\right] + \theta^N\left[\left(1-\theta^T\right)\Psi_{W^T} + \left(1-\xi^N\right)\right]\right\} \lessgtr 0, \tag{431}$$

where

$$\Psi_{W^T} = \left(1-\xi^N\right)\epsilon + (1-\alpha_L)(\sigma_L - \epsilon), \tag{432a}$$

$$\Psi_{W^N} = \xi^N\epsilon + \alpha_L(\sigma_L - \epsilon), \tag{432b}$$

$$\Psi_{W^T} + \Psi_{W^N} = \sigma_L. \tag{432c}$$

The sign of G depends on $\epsilon \gtreqless \sigma_L$; for the baseline calibration, we have $\epsilon > \sigma_L$; because the discrepancy is small, we find it convenient to assume $\sigma_L \simeq \epsilon$ so that a rise in W^T (W^N) does not affect L^N (L^T). Hence, we have $G < 0$. In the following, for clarity purposes, when discussing the results, we assume that $\sigma_L \simeq \epsilon$ so that determinant G given by eq. (431) is negative. Note that all our statements below also hold when $\epsilon > \sigma_L$.

The short-run static solutions for sectoral wages are:

$$W^T = W^T\left(\bar{\lambda}, K, P\right), \quad W^N = W^N\left(\bar{\lambda}, K, P\right), \tag{433}$$

with

$$\frac{\hat{W}^T}{\hat{K}} = -\frac{\left(1-\theta^T\right)\theta^N}{G} > 0, \tag{434a}$$
$$\frac{\hat{W}^N}{\hat{K}} = -\frac{\left(1-\theta^N\right)\theta^T}{G} > 0, \tag{434b}$$
$$\frac{\hat{W}^T}{\hat{P}} = \frac{\left(1-\theta^T\right)\left(\Psi_{W^N}+\xi^N\right)}{G} < 0, \tag{434c}$$
$$\frac{\hat{W}^N}{\hat{P}} = -\frac{\left\{\theta^T\xi^N + \left[\left(1-\xi^N\right) + + \left(1-\theta^T\right)\Psi_{W^T}\right]\right\}}{G} > 0, \tag{434d}$$
$$\frac{\hat{W}^T}{\hat{\bar{\lambda}}} = \frac{\sigma_L\left(1-\theta^T\right)\theta^N}{G} < 0, \tag{434e}$$
$$\frac{\hat{W}^N}{\hat{\bar{\lambda}}} = \frac{\sigma_L\left(1-\theta^N\right)\theta^T}{G} < 0, \tag{434f}$$
$$\tag{434g}$$

The short-run static solutions for capital-labor ratios are:

$$k^T = k^T\left(\lambda, K, P\right), \quad k^N = k^N\left(\bar{\lambda}, K, P\right), \tag{435}$$

with

$$\frac{\hat{k}^T}{\hat{K}} = -\frac{\theta^N}{G} > 0, \tag{436a}$$
$$\frac{\hat{k}^N}{\hat{K}} = -\frac{\theta^T}{G} > 0, \tag{436b}$$
$$\frac{\hat{k}^T}{\hat{P}} = \frac{\Psi_{W^N}+\xi^N}{G} < 0, \tag{436c}$$
$$\frac{\hat{k}^N}{\hat{P}} = \frac{\left\{\theta^T\Psi_{W^N} - \left[\left(1-\theta^T\right)\Psi_{W^T} + \left(1-\xi^N\right)\right]\right\}}{G} > 0, \tag{436d}$$
$$\frac{\hat{k}^T}{\hat{\bar{\lambda}}} = \frac{\sigma_L\theta^N}{G} < 0, \tag{436e}$$
$$\frac{\hat{k}^N}{\hat{\bar{\lambda}}} = \frac{\sigma_L\theta^T}{G} < 0. \tag{436f}$$
$$\tag{436g}$$

An increase in the capital stock K raises capital-labor ratios and thereby wage rates in both sectors. A rise in λ encourages agents to supply more labor which reduces sectoral capital-labor ratios and thereby wage rates in both sectors. In the standard model assuming perfect mobility of labor across sectors, an appreciation in the relative price of non tradables shifts resources toward the non traded sector and increases (lowers) k^N and k^T if the traded sector is more (less) capital intensive than the non-traded sector. In a model with limited labor mobility, k^N increases as P appreciates irrespective of whether the traded sector is more or less capital intensive than the non traded sector.

Inserting first sectoral wages (433), sectoral employment (427) can be solved as functions of the shadow value of wealth, the capital stock and the relative price of non tradables:

$$L^T = L^T\left(\bar{\lambda}, K, P\right), \quad L^N = L^N\left(\bar{\lambda}, K, P\right), \tag{437}$$

where the partial derivatives are not shown as we cannot determine the sign of analytical expressions in the general case. Yet, when assuming $\sigma_L \simeq \epsilon$ and using the fact that $\hat{W}^T = \left(1-\theta^T\right)\hat{k}^T$ we have

$$\hat{L}^T = \sigma_L \hat{\lambda} + \left[\epsilon \alpha_L + \sigma_L \left(1-\alpha_L\right)\right]\left(1-\theta^T\right)\hat{k}^T.$$

Using (436), we find that traded labor is increasing with the capital stock K and decreasing with the relative price of non tradables. Adopting a similar reasoning for non traded labor, we have:

$$\hat{L}^N = \sigma_L \hat{\lambda} + \left[\epsilon\left(1-\alpha_L\right) + \sigma_L \alpha_L\right]\hat{W}^N.$$

Using (436), we find that non traded labor is increasing with both the capital stock K and the relative price of non tradables.

Production functions (420) can be rewritten ad follows:

$$Y^j = Z^j L^j \left(k^j\right)^{1-\theta^j}, \quad j = T, N. \tag{438}$$

Inserting first short-run static solutions for sectoral capital-labor ratios (435) and sectoral labor (437) into the production functions of the traded and non traded sectors yields:

$$Y^T = Y^T\left(\bar{\lambda}, K, P\right), \quad Y^N = Y^N\left(\bar{\lambda}, K, P\right), \tag{439}$$

where the partial derivatives are not shown as we cannot determine the sign of expressions. In the standard two-sector model imposing perfect mobility of labor across sectors, the Rybczynski effect implies that a rise in K raises the output of the sector which is relatively more capital intensive. With a difficulty in reallocating labor across sectors, the Rybczynski effect does no hold as a rise in K now increases both traded and non traded outputs. The reason is that due to imperfect mobility of labor, increasing the capital stock raises capital-labor labor ratios in both sectors so that both Y^T and Y^N rise. As in the standard model assuming perfect mobility of labor, an appreciation in the relative price of non tradables shifts resources toward the non traded sector, but all the less so as labor is less mobile across sectors.

The Return on Domestic Capital, R

The return on domestic capital is:

$$R = Z^T\left(1-\theta^T\right)\left(k^T\right)^{-\theta^T}. \tag{440}$$

Inserting first the short-run static solution for the capital-labor ratio k^T given by (435), eq. (440) can be solved for the return on domestic capital:

$$R = R\left(\bar{\lambda}, K, P\right), \tag{441}$$

where partial derivatives are given by:

$$R_K = \frac{\partial R}{\partial K} = -\theta^T \frac{R}{k^T} k^T_K < 0, \tag{442a}$$

$$R_P = \frac{\partial R}{\partial P} = -\theta^T \frac{R}{k^T} k^T_P > 0. \tag{442b}$$

Optimal Investment Decision, I/K

Eq. (405c) can be solved for the investment rate:

$$\frac{I}{K} = v\left(\frac{Q}{P_I(P)}\right) + \delta_K, \tag{443}$$

where

$$v\left(.\right) = \frac{1}{\kappa}\left(\frac{Q}{P_J} - 1\right), \tag{444}$$

with

$$v_Q = \frac{\partial v(.)}{\partial Q} = \frac{1}{\kappa}\frac{1}{P_J} > 0, \quad v_P = \frac{\partial v(.)}{\partial P} = -\frac{Q}{\kappa}\frac{\alpha_J}{P_J P} < 0. \tag{445}$$

Inserting (443) into (403), investment including capital installation costs can be rewritten as follows:

$$\begin{aligned} J &= K\left[\frac{I}{K}+\frac{\kappa}{2}\left(\frac{I}{K}-\delta_K\right)^2\right], \\ &= K\left[v(.)+\delta_K+\frac{\kappa}{2}\left(v(.)\right)^2\right]. \end{aligned} \tag{446}$$

The Relative Price of Non Tradables, P

Finally, we have to solve for the relative price of non tradables by using the non traded goods market clearing condition:

$$Y^N = C^N + G^N + J^N. \tag{447}$$

Remembering that the non traded input J^N used to produce investment goods is equal to $P_J' J$, inserting short-run static solutions for C^N and Y^N given by (425) and (439), respectively, and substituting (446), the non traded goods market clearing condition (447) can be rewritten as follows:

$$Y^N\left(\bar{\lambda}, K, P\right) = C^N\left(\bar{\lambda}, P\right) + G^N + P_J' K\left[v(.)+\delta_K+\frac{\kappa}{2}\left(v(.)\right)^2\right]. \tag{448}$$

Eq. (448) can be solved for the relative price of non tradables:

$$P = P\left(\bar{\lambda}, K, Q, G^N\right), \tag{449}$$

with partial derivatives given by:

$$P_K = \frac{\partial P}{\partial K} = \frac{-\frac{Y_K^N}{P_J'}+\frac{J}{K}}{\Psi^P} \lessgtr 0, \tag{450a}$$

$$P_Q = \frac{\partial P}{\partial Q} = \frac{K v_Q\left[1+\kappa v(.)\right]}{\Psi^P} > 0, \tag{450b}$$

$$P_{G^N} = \frac{1}{P_J'\Psi^P} > 0, \tag{450c}$$

where we set

$$\Psi^P = \left[\left(Y_P^N - C_P^N\right) + \frac{J^N \phi_J\left(1-\alpha_J\right)}{P}\right]\frac{1}{P_J'} - K v_P\left[1+\kappa v(.)\right] > 0. \tag{451}$$

F.4 Equilibrium Dynamics

Remembering that the non traded input J^N used to produce the capital good is equal to $P_J' J$, using the fact that $J^N = Y^N - C^N - G^N$ and inserting $I = \dot{K} + \delta_K$, the capital accumulation equation can be rewritten as follows:

$$\dot{K} = \frac{Y^N - C^N - G^N}{P_J'} - \delta_K K - \frac{\kappa}{2}\left(\frac{I}{K}-\delta_K\right)^2 K. \tag{452}$$

Inserting short-run static solutions for non traded output (439), consumption in non tradables (425), and optimal investment decision (443) into the physical capital accumulation equation (452) and the dynamic equation for the shadow value of capital stock (404b), the dynamic system is:

$$\begin{aligned} \dot{K} \equiv \Upsilon\left(K, P, Q, G^N\right) &= \frac{Y^N\left(K, P(.), \bar{\lambda}\right) - C^N\left(\bar{\lambda}, P(.)\right) - G^N}{P_J'\left(P(.)\right)} \\ &\quad -\delta_K K - \frac{K}{2\kappa}\left[\frac{Q}{P_J\left(P(.)\right)}-1\right]^2, \end{aligned} \tag{453a}$$

$$\dot{Q} \equiv \Sigma\left(K, P, Q, G^N\right) = \left(r^\star + \delta_K\right)Q - \left[R\left(K, P(.)\right) + P_J\frac{\kappa}{2}v(.)\left(v(.)+2\delta_K\right)\right]. \tag{453b}$$

As will be useful, let us denote by Υ_K, Υ_Q, and Υ_P the partial derivatives evaluated at the steady-state of the capital accumulation equation w.r.t. K and Q (for given P), respectively, and P:

$$\Upsilon_K\Big|_{\text{P fixed}} \equiv \frac{\partial \dot{K}}{\partial K}\Big|_{\text{P fixed}} = \left(\frac{Y_K^N}{P_J'} - \delta_K\right) > 0, \tag{454a}$$

$$\Upsilon_P \equiv \frac{\partial \dot{K}}{\partial P} = \left[\left(Y_P^N - C_P^N\right) + \frac{\tilde{I}^N \phi_J \left(1-\alpha_J\right)}{\tilde{P}}\right]\frac{1}{P_J'} > 0, \tag{454b}$$

$$\Upsilon_Q\Big|_{\text{P fixed}} \equiv \frac{\partial \dot{K}}{\partial Q}\Big|_{\text{P fixed}} = 0, \tag{454c}$$

where we used the fact that in the long-run, $\tilde{J}^N = \tilde{I}^N$ and $\tilde{Q} = P_J\left(\tilde{P}\right)$.

Let us denote by Σ_K, Σ_Q, and Σ_P the partial derivatives evaluated at the steady-state of the dynamic equation for the marginal value of an additional unit of capital w.r.t. K and Q (for given P), respectively, and P:

$$\Sigma_K\big|_{\text{P fixed}} \equiv \frac{\partial \dot{Q}}{\partial K}\Big|_{\text{P fixed}} = -R_K > 0, \tag{455a}$$

$$\Sigma_P \equiv \frac{\partial \dot{Q}}{\partial P} = -R_P - P_J \kappa v_P \delta_K \lesseqgtr 0, \tag{455b}$$

$$\Sigma_Q\big|_{\text{P fixed}} \equiv \frac{\partial \dot{Q}}{\partial Q}\Big|_{\text{P fixed}} = \left(r^\star + \delta_K\right) - P_J \kappa v_Q \delta_K = r^\star > 0, \tag{455c}$$

where R_K given by (442a) is evaluated at the steady-state, i.e., $-P_J\left(r^\star + \delta_K\right)\theta^T \frac{k_K^T}{\tilde{k}^T} < 0$, and $R_P = -P_J\left(r^\star + \delta_K\right)\theta^T \frac{k_P^T}{\tilde{k}^T} > 0$ (see eq. (442b)); to derive (455c), we inserted $v_Q = \frac{1}{\kappa P_J}$ given by (445).

Denoting steady-state values with a tilde, linearizing (453a)-(453b) in the neighborhood of the steady-state yields in matrix form:

$$\begin{pmatrix} \dot{K}(t) \\ \dot{Q}(t) \end{pmatrix} = \begin{pmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{pmatrix} \begin{pmatrix} K(t) - \tilde{K} \\ Q(t) - \tilde{Q} \end{pmatrix}, \tag{456}$$

where the coefficients of the Jacobian matrix J are given by:

$$a_{11} = \Upsilon_K\big|_{\text{P fixed}} + \Upsilon_P P_K > 0, \tag{457a}$$

$$a_{12} = \Upsilon_P P_Q > 0, \tag{457b}$$

$$a_{21} = \Sigma_K\big|_{\text{P fixed}} + \Sigma_P P_K > 0, \tag{457c}$$

$$a_{22} = r^\star + \Sigma_P P_Q > 0, \tag{457d}$$

with partial derivatives being evaluated at the steady-state; we used the fact that at the steady-state $\tilde{J}/\tilde{K} = \tilde{I}/\tilde{K} = \delta_K$ and $\tilde{R} = Z^T\left(1-\theta^T\right)\left(\tilde{k}^T\right)^{-\theta^T} = P_J\left(r^\star + \delta_K\right)$.

Saddle path stability requires the determinant of the Jacobian matrix Det$J$ given by $a_{11}a_{22} - a_{21}a_{12}$ to be negative. While the term $a_{21}a_{12}$ is always positive, regardless of sectoral capital intensities, the term $a_{11}a_{22}$ can be positive or negative. Because both the elasticity k^N with respect to P and the tradable content of investment expenditure $(1-\alpha_J)$ are smaller than one and exert opposite effects on the marginal product of capital, the term $a_{11}a_{22}$ is small so that the saddle-path stability condition is fulfilled regardless of sectoral capital intensities. When investment expenditure are traded only, i.e., $\alpha_J = 0$, we have $a_{22} < 0$ while $a_{11} > 0$; as a result, the determinant of the Jacobian matrix given by $a_{11}a_{22} - a_{21}a_{12}$ is always negative in this case so that the equilibrium is saddle-path. When $0 < \alpha_J < 1$, the sign of the Jacobian matrix is ambiguous; for all plausible sets of parametrization, we find that the long-run equilibrium is saddle path.

Assuming that the saddle-path stability condition is fulfilled, and denoting the negative eigenvalue by ν_1 and the positive eigenvalue by ν_2, the general solutions for K and Q are:

$$K(t) - \tilde{K} = D_1 e^{\nu_1 t} + D_2 e^{\nu_2 t}, \quad Q(t) - \tilde{Q} = \omega_2^1 D_1 e^{\nu_1 t} + \omega_2^2 D_2 e^{\nu_2 t}, \tag{458}$$

where K_0 is the initial capital stock and $\left(1, \omega_2^i\right)'$ is the eigenvector associated with eigenvalue ν_i:

$$\omega_2^i = \frac{\nu_i - a_{11}}{a_{12}}. \tag{459}$$

Because $\nu_1 < 0$, $a_{11} > 0$ and $a_{12} > 0$, we have $\omega_2^1 < 0$, regardless of sectoral capital intensities, which implies that the shadow value of investment and the stock physical capital move in opposite direction along a stable path.

Remembering that $J^T = (1-\alpha_J) P_J J$, the current account equation is given by:

$$\begin{aligned} \dot{B} \equiv \Xi(B,K,Q,G) &= r^\star B + Y^T - C^T - G^T - (1-\alpha_J) P_J J, \\ &= r^\star B + Y^T - C^T - G^T - \left(\frac{1-\alpha_J}{\alpha_J}\right) P\left(Y^N - C^N - G^N\right), \end{aligned} \tag{460}$$

where we used the fact that $P_J' J = Y^N - C^N - G^N$. As will be useful later, let us denote by Ξ_K and Ξ_P the partial derivatives of the accumulation equation for traded bonds w.r.t. K (for given P) and P:

$$\Xi_K\big|_{\text{P fixed}} \equiv \frac{\partial \dot{B}}{\partial K}\Big|_{\text{P fixed}} = Y_K^T - \left(\frac{1-\alpha_J}{\alpha_J}\right) \tilde{P} Y_K^N \geq 0, \tag{461a}$$

$$\Xi_P \equiv \frac{\partial \dot{B}}{\partial P} = \left(Y_P^T - C_P^T\right) - \left(\frac{1-\alpha_J}{\alpha_J}\right) \tilde{P}\left(Y_P^N - C_P^N\right) - \phi_J \left(\frac{1-\alpha_J}{\alpha_J}\right) \tilde{I}^N < 0, \tag{461b}$$

where we used the fact that $\frac{\partial\left(\frac{1-\alpha_J}{\alpha_J}\right)}{\partial P} = -\frac{1}{P}\left[\left(\frac{1-\alpha_J}{\alpha_J}\right) - \phi_J \left(\frac{1-\alpha_J}{\alpha_J}\right)\right]$ and at the steady-state, we have $\tilde{J}^N = \tilde{I}^N$ since capital installation costs are absent in the long run.

Inserting first the short-run static solutions for traded output (439) and consumption in tradables (425) into the accumulation equation of foreign bonds (460), linearizing, substituting the solutions for $K(t)$ and $Q(t)$ given by (458) yields the general solution for traded bonds:

$$B(t) = \tilde{B} + \left[\left(B_0 - \tilde{B}\right) - \Psi_1 D_1 - \Psi_2 D_2\right] e^{r^\star t} + \Psi_1 D_1 e^{\nu_1 t} + \Psi_2 D_2 e^{\nu_2 t}, \tag{462}$$

where B_0 is the initial stock of traded bonds and we set

$$\Xi_K = \Xi_K\big|_{\text{P fixed}} + \Xi_P P_K, \tag{463a}$$

$$\Xi_Q = \Xi_P P_Q, \tag{463b}$$

$$N_i = \Xi_K + \Xi_Q \omega_2^i, \tag{463c}$$

$$\Psi_i = \frac{N_i}{\nu_i - r^\star}. \tag{463d}$$

Invoking the transversality condition leads to the linearized version of the nations's intertemporal solvency condition:

$$\tilde{B} - B_0 = \Psi_1 \left(\tilde{K} - K_0\right), \tag{464}$$

where K_0 is the initial stock of physical capital.

F.5 Derivation of the Accumulation Equation of Financial Wealth

Remembering that the stock of financial wealth $A(t)$ is equal to $B(t) + Q(t)K(t)$, differentiating w.r.t. time, i.e., $\dot{A}(t) = \dot{B}(t) + \dot{Q}(t)K(t) + Q(t)\dot{K}(t)$, plugging the dynamic equation for the marginal value of capital (405e), inserting the accumulation equations for physical capital (404b) and traded bonds (404a), yields the accumulation equation for the stock of financial wealth or the dynamic equation for private savings:

$$\dot{A}(t) = r^\star A(t) + W(t)L(t) - T(t) - P_C\left(P(t)\right) C(t). \tag{465}$$

We first determine short-run static solutions for aggregate labor supply and aggregate wage index. Inserting short-run static solutions for sectoral wages (433) into the short-run static solution for aggregate labor supply (421), we can solve for total hours worked:

$$L = L\left(\bar{\lambda}, K, P\right), \tag{466}$$

where partial derivatives are given by

$$\begin{aligned} L_K &\equiv \frac{\partial L}{\partial K} = L_{W^T} W_K^T + L_{W^N} W_K^N > 0, &(467a)\\ L_P &\equiv \frac{\partial L}{\partial P} = L_{W^T} W_P^T + L_{W^N} W_P^N \gtrless 0. &(467b)\end{aligned}$$

Substituting short-run static solutions for sectoral wages (433) into the aggregate wage index $W \equiv W\left(W^T, W^N\right)$, we can solve for the aggregate wage index:

$$W = W\left(\bar{\lambda}, K, P\right), \tag{468}$$

where partial derivatives are given by

$$\begin{aligned} W_K &\equiv \frac{\partial W}{\partial K} = W_{W^T} W_K^T + W_{W^N} W_K^N, &(469a)\\ W_P &\equiv \frac{\partial W}{\partial P} = W_{W^T} W_P^T + W_{W^N} W_P^N, &(469b)\end{aligned}$$

with $W_{W^T} = \left(W/W^T\right)(1-\alpha_L)$ and $W_{W^N} = \left(W/W^N\right)\alpha_L$.

As will be useful, let us denote by Λ_K and Λ_P the partial derivatives of the accumulation equation for financial wealth w.r.t. K (for given P) and P:

$$\begin{aligned} \Lambda_K &\equiv \left.\frac{\partial \dot{A}}{\partial K}\right|_{\text{P fixed}} = \left(W_K \tilde{L} + \tilde{W} L_K\right) > 0, &(470a)\\ \Lambda_P &\equiv \frac{\partial \dot{A}}{\partial P} = \left(W_P \tilde{L} + \tilde{W} L_P\right) - \left(\tilde{C}^N + P_C C_P + G^N\right) \lesseqgtr 0, &(470b)\end{aligned}$$

where all partial derivatives are evaluated at the steady-state.

Inserting short-run static solutions for aggregate labor supply (466), for the aggregate wage index (468) and consumption (423) into the accumulation equation of financial wealth (465), linearizing around the steady-state, and solving yields the general solution for the stock of financial wealth:

$$A(t) = \tilde{A} + \left[\left(A_0 - \tilde{A}\right) - \Delta_1 D_1 - \Delta_2 D_2\right] e^{r^\star t} + \Delta_1 D_1 e^{\nu_1 t} + \Delta_2 D_2 e^{\nu_2 t}, \tag{471}$$

where A_0 is the initial stock of financial wealth and we set

$$\begin{aligned} \Lambda_K &= \left.\Lambda_K\right|_{\text{P fixed}} + \Lambda_P P_K, &(472a)\\ A_Q &= \Lambda_P P_Q, &(472b)\\ M_i &= \Lambda_K + \Lambda_Q \omega_2^i, &(472c)\\ \Delta_i &= \frac{M_i}{\nu_i - r^\star}. &(472d)\end{aligned}$$

The linearized version of the representative household's intertemporal solvency condition is:

$$\tilde{A} - A_0 = \Delta_1\left(\tilde{K} - K_0\right), \tag{473}$$

where K_0 is the initial stock of physical capital.

F.6 The Steady-State

In the next section, we use a specific procedure to solve for the steady-state which allows us to summarize graphically the long-run equilibrium. Below, we characterize the whole steady-state and use tilde to denote long-run values. Setting $\dot{K} = \dot{P} = \dot{B} = 0$ into (453a), (453b) and (457a), and inserting short-run static solutions for k^N, Y^N and Y^T, C^N and C^T derived above, the steady-state can be summarized by four equations:

$$Z^T \left(1-\theta^T\right) \left[k^T \left(\tilde{K}, \tilde{P}, \bar{\lambda}\right)\right]^{-\theta^T} = P_J \left(\tilde{P}\right) \left(r^\star + \delta\right), \tag{474a}$$

$$Y^N \left(\tilde{K}, \tilde{P}, \bar{\lambda}\right) = C^N \left(\tilde{P}, \bar{\lambda}\right) + P_J' \left(\tilde{P}\right) \delta_K \tilde{K} + G^N, \tag{474b}$$

$$r^\star \tilde{B} + Y^T \left(\tilde{K}, \tilde{P}, \bar{\lambda}\right) = C^T \left(\tilde{P}, \bar{\lambda}\right) + \left(1-\alpha_J\right) P_J \left(\tilde{P}\right) \delta_K \tilde{K} + G^T, \tag{474c}$$

$$\tilde{B} - B_0 = \Psi_1 \left(\tilde{K} - K_0\right). \tag{474d}$$

These four equations jointly determine $\tilde{P}$, $\tilde{K}$, $\tilde{B}$ and $\bar{\lambda}$.

G Solving for the Steady-State

In this section, we characterize the long-run equilibrium graphically.

G.1 Rewriting the Steady-State

In order to summarize graphically the long-run equilibrium and to build up intuition on the long-run effects of fiscal shocks, it is convenient to rewrite the steady-state as follows:

$$\frac{\tilde{C}^T}{\tilde{C}^N} = \frac{\varphi}{1-\varphi} \tilde{P}^{\phi}, \tag{475a}$$

$$\frac{\tilde{L}^T}{\tilde{L}^N} = \frac{\vartheta}{1-\vartheta} \tilde{\omega}^{-\epsilon}, \tag{475b}$$

$$\frac{\tilde{Y}^T \left(1 + \upsilon_B - \upsilon_{J^T} + \upsilon_{G^T}\right)}{\tilde{Y}^N \left(1 - \upsilon_{J^N} - \upsilon_{G^N}\right)} = \frac{\tilde{C}^T}{\tilde{C}^N}, \tag{475c}$$

$$\tilde{P} \left(1-\theta_N\right) \left(\tilde{k}^N\right)^{-\theta_N} = P_J \left(\tilde{P}\right) \left(r^\star + \delta\right), \tag{475d}$$

$$Z^T \left(1-\theta_T\right) \left(\tilde{k}^T\right)^{-\theta_T} = \tilde{P} Z^N \left(1-\theta_N\right) \left(\tilde{k}^N\right)^{-\theta_N} = \tilde{R}, \tag{475e}$$

$$\theta_T \left(\tilde{k}^T\right)^{1-\theta_T} = \tilde{W}^T, \tag{475f}$$

$$P \theta_N \left(\tilde{k}^N\right)^{1-\theta_N} = \tilde{W}^N, \tag{475g}$$

where $\tilde{\Omega} = \tilde{W}^N / \tilde{W}^T$ is the steady-state relative wage and $\tilde{R} = P_J \left(r^\star + \delta\right)$ is the steady-state value of the capital rental cost. We denote by $\upsilon_{J^N} \equiv \frac{\tilde{J}^N}{\tilde{Y}^N}$ ($\upsilon_{J^T} \equiv \frac{\tilde{J}^T}{\tilde{Y}^T}$) the ratio of non traded (traded) investment to non traded (traded) output, by $\upsilon_B \equiv \frac{r^\star \tilde{B}}{\tilde{Y}^T}$ the ratio of interest receipts to traded output, by $\upsilon_{G^j} \equiv \frac{G^j}{\tilde{Y}^j}$ the ratio of government spending in good $j = T, N$ to output of sector $j = T, N$.

Before analyzing the long-run effects of a rise in G^N, we characterize the steady state graphically. We denote the logarithm of variables with lower-case letters. Because we restrict ourselves to the analysis of the long-run run equilibrium, the tilde is suppressed for the purposes of clarity. The steady state can be described by considering alternatively the goods or the labor market.

G.2 Goods Market Equilibrium

To begin with, we characterize the goods market equilibrium. The steady state can be summarized graphically in Figure 52. The figure traces out two schedules in the $(y^T - y^N, p)$-space which are derived below. To avoid unnecessary complications, we normalize sectoral TFPs, i.e., Z^T and Z^N, to 1.

Combining (475a) and the market clearing condition (475c) yields:

$$\frac{C^T}{C^N} = \frac{\varphi}{1-\varphi} P^{\phi} = \frac{Y^T \left(1 + \upsilon_B - \upsilon_{J^T} - \upsilon_{G^T}\right)}{Y^N \left(1 - \upsilon_{J^N} - \upsilon_{G^N}\right)}. \tag{476}$$

The ratio of traded output to non traded output is:

$$\frac{Y^T}{Y^N} = \frac{\left(1 - \upsilon_{J^N} - \upsilon_{G^N}\right)}{\left(1 + \upsilon_B - \upsilon_{J^T} + \upsilon_{G^T}\right)} \frac{\varphi}{1-\varphi} P^{\phi}. \tag{477}$$

Taking logarithm yields the GME-equilibrium:

$$\left(y^T - y^N\right)\Big|^{GME} = \phi p + x', \tag{478}$$

where $x' = \ln\left(\frac{\varphi}{1-\varphi}\right) + \ln\left(\frac{1-\upsilon_{I^N}-\upsilon_{G^N}}{1+\upsilon_B-\upsilon_{J^T}-\upsilon_{G^T}}\right)$. According to (478), the goods market equilibrium is upward-sloping in the $(y^T - y^N, p)$-space and the slope of the GME-schedule is equal to $1/\phi$.

In order to facilitate the interpretation of analytical results, it is useful to rewrite the market clearing condition described by eq. (475c). To do so, take logarithm to $\left(\frac{1-\upsilon_{J^N}-\upsilon_{G^N}}{1+\upsilon_B-\upsilon_{J^T}-\upsilon_{G^T}}\right)$ which gives $\ln\left(1 + \upsilon_B - \upsilon_{J^T} - \upsilon_{G^T}\right) - \ln\left(1 - \upsilon_{J^N} - \upsilon_{G^N}\right)$, use a Taylor approximation at a first order which implies $\ln\left(1 + \upsilon_B - \upsilon_{J^T} - \upsilon_{G^T}\right) - \ln\left(1 - \upsilon_{J^N} - \upsilon_{G^N}\right) \simeq \upsilon_B - \upsilon_{J^T} - \upsilon_{G^T} + \upsilon_{I^N} + \upsilon_{G^N}$. Remembering that at the steady state the traded good market clearing condition is $r^{\star}B + Y^T - J^T - C^T - G^T = 0$, denoting net exports by NX with $NX = Y^T - J^T - C^T - G^T$ or alternatively $-NX = r^{\star}B$. Dividing the LHS and the RHS by Y^T leads to the ratio of net exports to traded output, $\upsilon_B = -\upsilon_{NX}$. Totally differentiating eq. (478) and remembering that government spending in non tradables is restored to its initial level so that $d\upsilon_{G^N} = 0$, leads to:

$$\left(\hat{y}^T - \hat{y}^N\right)\Big|^{GME} = \phi\hat{p} + \left(d\upsilon_{NX} - d\upsilon_{J^N} + d\upsilon_{J^T}\right). \tag{479}$$

In the long-run, investment expenditure are higher and thus, $d\upsilon_{J^j} > 0$ since government spending has returned to its initial level while consumption expenditure are lowered due to the negative wealth effect. In the long-run, the ratio of net exports to traded output increases, i.e., $d\upsilon_{NX} > 0$. Furthermore, the improvement in the trade balance must exceed the investment boom in the non traded sector because along the transitional path, the current account deficit caused by reduced savings more than offsets the fall in investment. The deterioration in the net foreign position in the long-run must be offset by a rise in net exports for the intertemporal solvency condition to hold. Hence, a temporary rise in government spending biased toward non tradables, shifts to the right the GME-schedule in the long-run.

To obtain closed-form solutions, we assume that the aggregator function for inputs of the investment good is Cobb-Douglas since data suggest that the elasticity of substitution ϕ_J is equal to one.

Combining (475b) with the steady-state relative wage given by (475f)-(475g), and using the production functions for the traded sector and non traded sectors which imply $L^T = \frac{Y^T}{\left(k^T\right)^{1-\theta^T}}$ and $L^N = \frac{Y^N}{\left(k^N\right)^{1-\theta^N}}$, yields:

$$\frac{Y^T}{Y^N} = P^{-\epsilon}\left(\frac{\theta^T}{\theta^N}\right)^{\epsilon}\left[\frac{\left(k^T\right)^{1-\theta^T}}{\left(k^N\right)^{1-\theta^N}}\right]^{1+\epsilon}.$$

Combining (475d) and (475e) yields:

$$\frac{\left(k^N\right)^{1-\theta_N}}{\left(k^T\right)^{1-\theta_T}} = P^{\frac{1-\theta_N}{\theta_N}}\left[P_J\left(r^{\star} + \delta_K\right)\right]^{\frac{1-\theta_T}{\theta_T} - \frac{1-\theta_N}{\theta_N}} \frac{\left[(1-\theta_N)\right]^{\frac{1-\theta_N}{\theta_N}}}{\left[(1-\theta_T)\right]^{\frac{1-\theta_T}{\theta_T}}}. \tag{480}$$

Inserting (480) to eliminate sectoral capital-labor ratios yields the LME-schedule:

$$\frac{Y^T}{Y^N} = P^{-\left[\epsilon+\left(\frac{1-\theta_N}{\theta_N}\right)(1+\epsilon)\right]} P_J^{\left(\frac{\theta_T-\theta_N}{\theta_T\theta_N}\right)(1+\epsilon)}\Pi, \tag{481}$$

where we set

$$\Pi = \frac{\vartheta}{1-\vartheta}\left(r^{\star}+\delta\right)^{\left(\frac{\theta_T-\theta_N}{\theta_T\theta_N}\right)(1+\epsilon)} \frac{\left[(\theta_T)^{\epsilon\theta_T}\left(1-\theta_T\right)^{(1-\theta_T)(1+\epsilon)}\right]^{1/\theta_T}}{\left[(\theta_N)^{\epsilon\theta_N}\left(1-\theta_N\right)^{(1-\theta_N)(1+\epsilon)}\right]^{1/\theta_N}} > 0. \tag{482}$$

Taking logarithm, (481) can be rewritten as follows:

$$\left(y^T - y^N\right)\Big|^{LME} = -\left\{\epsilon + (1+\epsilon)\left[\left(\frac{1-\theta_N}{\theta_N}\right) - (1-\varphi_J)\left(\frac{\theta_T-\theta_N}{\theta_T\theta_N}\right)\right]\right\} p + \ln\Pi, \tag{483}$$

where Π is given by (482).

In a model abstracting from physical capital, we have $\theta^T = 1$, so that the LME-schedule described by eq. (483) reduces to:

$$\left(y^T - y^N\right)\Big|^{LME}_{\theta^T=1} = -\epsilon p + \ln\Pi. \tag{484}$$

In a model with physical capital (i.e., $0 < \theta^T < 1$) but abstracting from traded investment (i.e., $\varphi_J = 0$), the GME-schedule described by eq. (481) reduces to:

$$\left(y^T - y^N\right)\Big|^{LME}_{\varphi_J=0} = -\left[\epsilon + \left(\frac{1-\theta^T}{\theta^T}\right)(1+\epsilon)\right] p + \ln\Pi. \tag{485}$$

If $\theta^T < 1$, the LME-schedule becomes flatter than that in a model abstracting from physical capital in the $(y^T - y^N, p)$-space. The LME-schedule is downward-sloping in the $(y^T - y^N, p)$-space with a slope equal to $-1/\left[\epsilon + \left(\frac{1-\theta^T}{\theta^T}\right)(1+\epsilon)\right]$. A rise in the relative price of non tradables p allows the non traded sector to pay higher wages. Because the relative wage ω rises, workers are encouraged to shift hours worked from the traded to the non traded sector. As a result, the ratio of sectoral outputs Y^T/Y^N declines. Introducing capital rotates to the left the LME-schedule due to the shift of capital across sectors triggered by a change in P. Following an appreciation in P, the non traded sector experiences a capital inflow which amplifies the expansionary effect on non traded output triggered by the reallocation of labor, which results in a flatter LME-schedule.

G.3 The Labor Market

The steady-steady can be characterized alternatively by focusing on the labor market in the $(l^T - l^N, \omega)$-space.

Taking logarithm to (475b) yields the labor supply-schedule (henceforth LS-schedule):

$$\left(l^T - l^N\right)\Big|^{LS} = -\epsilon\ln\omega + d, \tag{486}$$

where $d = \ln\left(\frac{\vartheta}{1-\vartheta}\right)$. According to (486), as in the model without capital, a rise in the non traded wage-traded wage ratio ω provides an incentive to shift labor supply from the traded sector towards the non traded sector. Hence the LS-schedule is downward-sloping in the $(l^T - l^N, \omega)$-space where the slope is equal to $-1/\epsilon$.

We turn to the derivation of the labor demand-schedule (henceforth LD-schedule). Dividing (475g) by (475f) yields:

$$\frac{P\theta^N\left(\tilde{k}^N\right)^{1-\theta^N}}{\theta^T\left(\tilde{k}^T\right)^{1-\theta^T}} = \Omega. \tag{487}$$

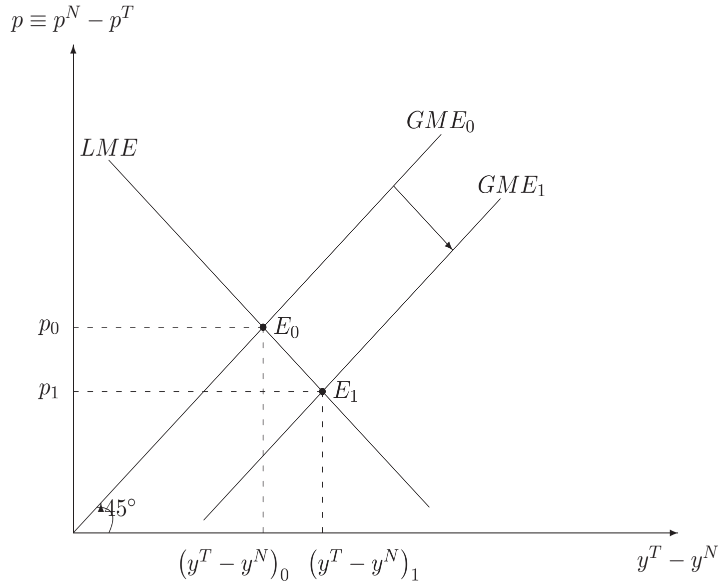


Figure 52: Steady-State Effects of an Unanticipated Temporary Rise in Government Spending in the $(y^T - y^N, p)$-space.

To eliminate the sectoral capital-labor ratios, we use eqs. (475d)-(475e), i.e.

$$\frac{\left(k^N\right)^{1-\theta^N}}{\left(k^T\right)^{1-\theta^T}} = P^{\frac{1-\theta^T}{\theta^T}} \left(r^\star + \delta\right)^{\frac{1-\theta^T}{\theta^T} - \frac{1-\theta^N}{\theta^N}} \frac{\left[\left(1-\theta^N\right)\right]^{\frac{1-\theta^N}{\theta^N}}}{\left[\left(1-\theta^T\right)\right]^{\frac{1-\theta^T}{\theta^T}}}. \tag{488}$$

To eliminate the relative price of non tradables, we combine the market-clearing condition (475c) and the demand for tradables in terms of non traded goods (475a) together with production functions (420):

$$P = \left[\frac{1-\varphi}{\varphi} \frac{1+\upsilon_B - \upsilon_{J^T} + \upsilon_{G^T}}{1-\upsilon_{J^N} - \upsilon_{G^N}} \frac{L^T \left(k^T\right)^{1-\theta^T}}{L^N \left(k^N\right)^{1-\theta^N}}\right]^{\frac{1}{\phi}}. \tag{489}$$

Substituting (489) into (488) yields:

$$\begin{aligned} \frac{\left(k^N\right)^{1-\theta^N}}{\left(k^T\right)^{1-\theta^T}} &= \left(r^\star + \delta\right)^{\frac{\phi\left(\theta^N - \theta^T\right)}{\theta^N\left[1+\theta^T(\phi-1)\right]}} \left[\frac{1-\varphi}{\varphi} \frac{1+\upsilon_B - \upsilon_{J^T} + \upsilon_{G^T}}{1-\upsilon_{J^N} - \upsilon_{G^N}} \frac{L^T}{L^N}\right]^{\frac{\left(1-\theta^T\right)}{\left[1+\theta^T(\phi-1)\right]}} \\ &\times \left[\frac{\left(1-\theta^N\right)^{\frac{\left(1-\theta^N\right)\theta^T}{\theta^N}}}{\left(1-\theta^T\right)^{\left(1-\theta^T\right)}}\right]^{\frac{\phi}{\left[1+\theta^T(\phi-1)\right]}}. \end{aligned} \tag{490}$$

Plugging (490) into (487) allows us to relate the relative labor demand to the relative wage:

$$\frac{L^T}{L^N} \Theta \left(\frac{1+\upsilon_B - \upsilon_{J^T} + \upsilon_{G^T}}{1-\upsilon_{J^N} - \upsilon_{G^N}}\right) = \Omega^{\left[1+\theta^T(\phi-1)\right]}, \tag{491}$$

where we set

$$\Theta = \left(r^\star + \delta\right)^{\frac{\left(\theta^N - \theta^T\right)(\phi-1)}{\theta^N}} \left(\frac{1-\varphi}{\varphi}\right) \left(\frac{\theta^N}{\theta^T}\right)^{\left[1+\theta^T(\phi-1)\right]} \left[\frac{\left(1-\theta^N\right)^{\left(1-\theta^N\right)\frac{\theta^T}{\theta^N}}}{\left(1-\theta^T\right)^{\left(1-\theta^T\right)}}\right]^{(\phi-1)}. \tag{492}$$

Taking logarithm to (491) yields the LD-schedule:

$$\left(l^T - l^N\right)\Big|^{LD} = \left[1+\theta^T(\phi-1)\right]\omega + \ln \frac{\left(1-\upsilon_{I^N} - \upsilon_{G^N}\right)}{\left(1+\upsilon_B - \upsilon_{J^T} + \upsilon_{G^T}\right)} - \ln \Theta. \tag{493}$$

Eq. (493) states that the LD-schedule is upward-sloping in the $(l^T - l^N, \omega)$-space since an increase in ω induces non traded producers to set higher prices, increasing the demand for traded goods and therefore labor demand in that sector relative to the non traded sector. When $\theta^T < 1$, the LD-schedule is steeper or flatter than that in a model abstracting from physical capital (i.e., when $\theta^T = 1$) depending on whether ϕ is larger or smaller than one. In both cases, following an increased non tradable labor cost, the non traded sector is induced to use more capital which raises non traded output and thereby produces a decline in p. Depending on whether ϕ is larger or smaller than one, the share of non tradables in total expenditure increases or decreases, as a result of the shift of capital towards the non traded sector. Hence, a given rise in ω produces a smaller or a larger expansionary effect on labor demand in the traded sector depending on whether ϕ exceeds or falls below unity.

Adopting the same methodology described above, the LD-schedule given by eq. (493) can be rewritten in percentage deviation from the initial steady-state in order to facilitate the discussion of the effects of a fiscal shock:

$$\left(\hat{l}^T - \hat{l}^N\right)\Big|^{LD} = \left[1 + \theta^T (\phi - 1)\right]\hat{\omega} + \left(d\upsilon_{NX} + d\upsilon_{J^T} - d\upsilon_{J^N}\right). \tag{494}$$

As mentioned previously, a fiscal shock deteriorates the current account in the short-run. The short-run current account deficit must be matched in the long-run by a rise in net exports which shifts the LD-schedule to the right, as captured by an increase in υ_{NX} by such an amount that $d\upsilon_{NX} + d\upsilon_{J^T} - d\upsilon_{J^N} > 0$. At the final steady-state, the relative wage Ω is lower while the ratio L^T/L^N is higher.

H Solving for Temporary Fiscal Shocks

In this section, we provide the main steps for the derivation of formal solutions following a temporary fiscal shock.

H.1 The Government Spending Shock

Because the endogenous response of government spending to an exogenous fiscal shock is hump-shaped, we assume that government consumption as a percentage of GDP evolves according to the following dynamic equation:

$$\frac{dG(t)}{\tilde{Y}} \equiv \frac{G(t) - \tilde{G}}{\tilde{Y}} = \left[e^{-\xi t} - (1-g)\, e^{-\chi t}\right], \tag{495}$$

where $\xi > 0$ and $\chi > 0$ are (positive) parameters which are set in order to capture the endogenous response of $G(t)$. Setting $t = 0$ into (495) yields:

$$\frac{dG(0)}{\tilde{Y}} \equiv \frac{G(0) - \tilde{G}}{\tilde{Y}} = g. \tag{496}$$

In the quantitative analysis, we set $g = 0.01$ so that government consumption increases initially by 1 percentage point of initial GDP, $\tilde{Y}$.

In the quantitative analysis we assume that the rise in government consumption is split between non traded and traded goods in accordance with their respective shares, $\omega_{G^N} = \frac{PG^N}{G}$ and $\omega_{G^T} = \frac{G^T}{G}$, respectively. Formally, we thus have:

$$\frac{dG(t)}{\tilde{Y}} = \omega_{G^N}\frac{dG}{\tilde{Y}} + \omega_{G^T}\frac{dG}{\tilde{Y}}.$$

Totally differentiating the balanced budget condition, government expenditure in good $j = T, N$ can be solved for overall government consumption as follows:

$$G^N(t) = \mathsf{G}^N\left(G(t)\right), \quad G^T = \mathsf{G}^T\left(G(t)\right), \tag{497}$$

where $\frac{\partial G^N}{\partial G} = \frac{\omega_{G^N}}{\tilde{P}}$ and $\frac{\partial G^T}{\partial G} = \omega_{G^T}$ with ω_{G^j} corresponding to the share of expenditure on good j in total government spending.

H.2 Formal Solutions for $K(t)$ and $Q(t)$

The adjustment of the open economy towards the steady-state is described by a dynamic system which comprises two equations. Inserting first the short-term static solution for the relative price of non tradables (449) together with (497) into (452), the accumulation equation for physical capital that clears the non-traded goods market along the transitional path can be rewritten as follows:

$$\begin{aligned}\dot{K} \equiv \Upsilon\left(K, Q, G\right) &= \frac{Y^N\left(\bar{\lambda}, K, P(.)\right) - C^N\left(\bar{\lambda}, P(.)\right) - \mathsf{G}^N\left(G\right)}{P_J'\left(P(.)\right)} - \delta_K K \\ &- \frac{K(t)}{2\kappa}\left[\frac{Q}{P_J'\left(P(.)\right)} - 1\right]^2, \end{aligned} \tag{498}$$

where $P = P\left(\bar{\lambda}, K, Q, G\right)$. Inserting first the optimal choice for the investment rate (443) and the short-term static solution for the relative price of non tradables (449) together with (497) into (405e), the dynamic equation for the shadow price of investment that equalizes the return on domestic capital and traded bonds $r^\star$ can be rewritten as follows:

$$\dot{Q} \equiv \Sigma\left(K, Q, G\right) = \left(r^\star + \delta_K\right) Q - \left[R\left(K, P(.)\right) + P_J(.)\frac{\kappa}{2}v(.)\left(v(.) + 2\delta_K\right)\right], \tag{499}$$

where $P = P\left(\bar{\lambda}, K, Q, G\right)$ and $v(.) = \frac{1}{\kappa}\left(\frac{Q}{P_J(P(.))} - 1\right)$ (see eq. (444)).

The linearized system can be written in a matrix form:

$$\begin{pmatrix} \dot{K}(t) \\ \dot{Q}(t) \end{pmatrix} = \begin{pmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{pmatrix}\begin{pmatrix} K(t) - \tilde{K} \\ Q(t) - \tilde{Q} \end{pmatrix} + \begin{pmatrix} \varepsilon_K\left(G(t) - \tilde{G}\right) \\ \varepsilon_Q\left(G(t) - \tilde{G}\right) \end{pmatrix}, \tag{500}$$

where the coefficients of the Jacobian matrix are given by (457) which we repeat for convenience:

$$a_{11} = \Upsilon_K = \left(\frac{Y_K^N}{P_J'} - \delta_K\right) + \left[\left(Y_P^N - C_P^N\right) + \frac{\tilde{I}^N\phi_J\left(1-\alpha_J\right)}{\tilde{P}}\right]\frac{P_K}{P_J'} \lessgtr 0, \tag{501a}$$

$$a_{12} = \Upsilon_Q = \left[\left(Y_P^N - C_P^N\right) + \frac{\tilde{I}^N\phi_J\left(1-\alpha_J\right)}{\tilde{P}}\right]\frac{P_Q}{P_J'} > 0, \tag{501b}$$

$$a_{21} = \Sigma_K = -R_K - \left(R_P + P_J\kappa v_P\delta_K\right)P_K > 0, \tag{501c}$$

$$a_{22} = \Sigma_Q = r^\star - \left(R_P + P_J\kappa v_P\delta_K\right)P_Q > 0, \tag{501d}$$

and the direct effects of an exogenous change in government consumption on K and Q are described by:

$$\varepsilon_K = \left\{\left[\left(Y_P^N - C_P^N\right) + \frac{\tilde{I}^N\phi_J\left(1-\alpha_J\right)}{\tilde{P}}\right]\frac{P_{G^N}}{P_J'} - \frac{1}{P_J'}\right\}\frac{\omega_{G^N}}{\tilde{P}}, \tag{502a}$$

$$\varepsilon_Q = -\left(R_P + P_J\kappa v_P\delta_K\right)\frac{P_{G^N}\omega_{G^N}}{\tilde{P}}, \tag{502b}$$

where we used the fact that $\frac{\partial G^N}{\partial G} = \frac{\omega_{G^N}}{\tilde{P}}$. **Eq. (500) corresponds to eq. (22) in the main text.**

We denote by $V = \left(V^1, V^2\right)$ the matrix of eigenvectors (given by (459)) with $V^{i,\prime} = \left(1, \omega_2^i\right)$ and we denote by V^{-1} the inverse matrix of V. Let us define:

$$\begin{pmatrix} X_1(t) \\ X_2(t) \end{pmatrix} \equiv V^{-1}\begin{pmatrix} K(t) - \tilde{K} \\ Q(t) - \tilde{Q} \end{pmatrix}. \tag{503}$$

Differentiating w.r.t. time, one obtains:

$$\begin{aligned}\begin{pmatrix} \dot{X}_1(t) \\ \dot{X}_2(t) \end{pmatrix} &= \begin{pmatrix} \nu_1 & 0 \\ 0 & \nu_2 \end{pmatrix}\begin{pmatrix} X_1(t) \\ X_2(t) \end{pmatrix} + V^{-1}\begin{pmatrix} \varepsilon_K dG(t) \\ \varepsilon_Q dG(t) \end{pmatrix}, \\ &= \begin{pmatrix} \nu_1 X_1(t) \\ \nu_2 X_2(t) \end{pmatrix} + \frac{1}{\nu_1 - \nu_2}\begin{pmatrix} \Phi_1 dG(t) \\ -\Phi_2 dG(t) \end{pmatrix}, \end{aligned} \tag{504}$$

where $dG(t) = G(t) - \tilde{G}$ and we set

$$\Phi_1 = \left[(a_{11} - \nu_2)\,\varepsilon_K + a_{12}\varepsilon_Q\right], \tag{505a}$$
$$\Phi_2 = \left[(a_{11} - \nu_1)\,\varepsilon_K + a_{12}\varepsilon_Q\right]. \tag{505b}$$

As will be useful later, in order to express solutions in a compact form, we set:

$$\Gamma_1 = -\frac{\Phi_1\tilde{Y}}{\nu_1 - \nu_2}\frac{1}{\nu_1 + \xi}, \tag{506a}$$
$$\Gamma_2 = -\frac{\Phi_2\tilde{Y}}{\nu_1 - \nu_2}\frac{1}{\nu_2 + \xi}, \tag{506b}$$
$$\Theta_1 = (1-g)\,\frac{\nu_1 + \xi}{\nu_1 + \chi}, \tag{506c}$$
$$\Theta_2 = (1-g)\,\frac{\nu_2 + \xi}{\nu_2 + \chi}. \tag{506d}$$
$$\tag{506e}$$

Solving for $X_1(t)$ gives:

$$\begin{aligned} X_1(t) &= e^{\nu_1 t}\left\{X_1(0) + \frac{\Phi_1}{\nu_1 - \nu_2}\int_0^t dG(\tau)e^{-\nu_1\tau}d\tau\right\}, \\ &= e^{\nu_1 t}\left\{X_1(0) + \frac{\Phi_1\tilde{Y}}{\nu_1 - \nu_2}\int_0^t \left[e^{-(\xi+\nu_1)\tau} - (1-g)\,e^{-(\chi+\nu_1)\tau}\right]d\tau\right\}, \\ &= e^{\nu_1 t}X_1(0) + \frac{\Phi_1\tilde{Y}}{\nu_1 - \nu_2}\left[\left(\frac{e^{\nu_1 t} - e^{-\xi t}}{\nu_1 + \xi}\right) - (1-g)\left(\frac{e^{\nu_1 t} - e^{-\chi t}}{\nu_1 + \chi}\right)\right], \\ &= e^{\nu_1 t}\left[X_1(0) - \Gamma_1\,(1 - \Theta_1)\right] + \Gamma_1\left(e^{-\xi t} - \Theta_1 e^{-\chi t}\right), \end{aligned} \tag{507}$$

where Γ_1 and Θ_1 are given by (506a) and (506c), respectively.

Solving for $X_2(t)$ gives:

$$X_2(t) = e^{\nu_2 t}\left\{X_2(0) - \frac{\Phi_2}{\nu_1 - \nu_2}\int_0^t dG(\tau)e^{-\nu_2\tau}d\tau\right\}. \tag{508}$$

Because $\nu_2 > 0$, for the solution to converge to the steady-state, the term in brackets must be nil when we let t tend toward infinity:

$$\begin{aligned} X_2(0) &= \frac{\Phi_2\tilde{Y}}{\nu_1 - \nu_2}\int_0^\infty \left[e^{-(\xi+\nu_2)\tau} - (1-g)\,e^{-(\chi+\nu_2)\tau}\right]d\tau, \\ &= \frac{\Phi_2\tilde{Y}}{\nu_1 - \nu_2}\left[\frac{1}{\xi + \nu_2} - (1-g)\,\frac{1}{\chi + \nu_2}\right], \\ &= -\Gamma_2\,(1 - \Theta_2), \end{aligned} \tag{509}$$

where Γ_2 and Θ_2 are given by (506b) and (506d), respectively.

Inserting first $X_2(0)$, the 'stable' solution for $X_2(t)$, i.e., consistent with convergence toward the steady-state when t tends toward infinity, is thus given by:

$$\begin{aligned} X_2(t) &= e^{\nu_2 t}\frac{\Phi_2\tilde{Y}}{\nu_1 - \nu_2}\int_t^\infty \left[e^{-(\xi+\nu_2)\tau} - (1-g)\,e^{-(\chi+\nu_2)\tau}\right]d\tau, \\ &= e^{\nu_2 t}\frac{\Phi_2\tilde{Y}}{\nu_1 - \nu_2}\left[\frac{e^{-(\xi+\nu_2)t}}{\xi + \nu_2} - (1-g)\,\frac{e^{-(\chi+\nu_2)t}}{\chi + \nu_2}\right], \\ &= -\Gamma_2\left(e^{-\xi t} - \Theta_2 e^{-\chi t}\right). \end{aligned} \tag{510}$$

Eq. (510) corresponds to eq. (25b) in the main text.

Using the definition of $X_i(t)$ (with $i = 1, 2$) given by (503), we can recover the solutions for $K(t)$ and $Q(t)$:

$$K(t) - \tilde{K} = X_1(t) + X_2(t), \tag{511a}$$
$$Q(t) - \tilde{Q} = \omega_2^1 X_1(t) + \omega_2^2 X_2(t). \tag{511b}$$

Eqs. (511) correspond to eqs. (24) in the main text.

Setting $t = 0$ into (511a) gives $X_1(0) = \left(K(0) - \tilde{K}\right) - X_2(0)$; inserting (509) leads to:

$$X_1(t) = e^{\nu_1 t}\left[\left(K(0) - \tilde{K}\right) + \Gamma_2\left(1 - \Theta_2\right) - \Gamma_1\left(1 - \Theta_1\right)\right] + \Gamma_1\left(e^{-\xi t} - \Theta_1 e^{-\chi t}\right). \quad (512)$$

Eq. (512) corresponds to eq. (25a) in the main text.

H.3 Formal Solution for the Net Foreign Asset Position, $B(t)$

To determine the formal solution for the net foreign asset position, we first linearize the current account equation (460) in the neighborhood of the steady-state and substitute the solutions for $K(t)$ and $Q(t)$:

$$\dot{B}(t) = r^\star\left(B(t) - \tilde{B}\right) + N_1 X_1(t) + N_2 X_2(t) + \Xi_G dG(t), \quad (513)$$

where N_i (with $i = 1, 2$) is given by (463b), and Ξ_G is given by:

$$\Xi_G = \left\{\left[\Xi_P P_{G^N} + \left(\frac{1-\alpha_J}{\alpha_J}\right)\tilde{P}\right]\frac{\omega_{G^N}}{\tilde{P}} - \omega_{G^T}\right\}, \quad (514)$$

where $\Xi_P < 0$ and $P_{G^N} > 0$ are given by (461b) and (450c), respectively.

Substituting $X_1(t)$ given by eq. (512) and $X_2(t)$ given by eq. (510) into (513) leads to:

$$\begin{aligned}\dot{B}(t) &= r^\star\left(B(t) - \tilde{B}\right) + \omega_B^1 e^{\nu_1 t} + N_1\Gamma_1\left(e^{-\xi t} - \Theta_1 e^{-\chi t}\right) \\ &- N_2\Gamma_2\left(e^{-\xi t} - \Theta_2 e^{-\chi t}\right) + \Xi_G\tilde{Y}\left(e^{-\xi t} - (1-g)\,e^{-\chi t}\right), \quad (515)\end{aligned}$$

where Γ_1 and Γ_2 are given by (506a) and (506b), respectively, and we set:

$$\omega_B^1 = N_1\left[\left(K(0) - \tilde{K}\right) + \Gamma_2\left(1 - \Theta_2\right) - \Gamma_1\left(1 - \Theta_1\right)\right]. \quad (516)$$

Pre-multiplying by $e^{-r^\star\tau}$ and integrating over $(0, t)$ allow us to obtain the general solution for $B(t)$:

$$\begin{aligned}B(t) - \tilde{B} &= \left\{\left(B_0 - \tilde{B}\right) - \frac{\omega_B^1}{\nu_1 - r^\star} + \frac{\Xi_G\tilde{Y}}{\xi + r^\star}\left(1 - \Theta'\right) + \frac{N_1\Gamma_1}{\xi + r^\star}\left(1 - \Theta_1'\right) - \frac{N_2\Gamma_2}{\xi + r^\star}\left(1 - \Theta_2'\right)\right\} e^{r^\star t} \\ &+ \frac{\omega_B^1}{\nu_1 - r^\star}e^{\nu_1 t} - \frac{\Xi_G\tilde{Y}}{\xi + r^\star}\left(e^{-\xi t} - \Theta' e^{-\chi t}\right) - \frac{N_1\Gamma_1}{\xi + r^\star}\left(e^{-\xi t} - \Theta_1' e^{-\chi t}\right) \\ &+ \frac{N_2\Gamma_2}{\xi + r^\star}\left(e^{-\xi t} - \Theta_2' e^{-\chi t}\right), \quad (517)\end{aligned}$$

where we set:

$$\begin{aligned}\Theta' &= (1-g)\frac{\xi + r^\star}{\chi + r^\star}, \quad (518a) \\ \Theta_1' &= \Theta_1\frac{\xi + r^\star}{\chi + r^\star}, \quad (518b) \\ \Theta_2' &= \Theta_2\frac{\xi + r^\star}{\chi + r^\star}. \quad (518c)\end{aligned}$$

Invoking the transversality condition, one obtains the 'stable' solution for the stock of foreign assets so that $B(t)$ converges toward its steady-state value $\tilde{B}$:

$$\begin{aligned}B(t) - \tilde{B} &= \frac{\omega_B^1}{\nu_1 - r^\star}e^{\nu_1 t} - \frac{\Xi_G\tilde{Y}}{\xi + r^\star}\left(e^{-\xi t} - \Theta' e^{-\chi t}\right) - \frac{N_1\Gamma_1}{\xi + r^\star}\left(e^{-\xi t} - \Theta_1' e^{-\chi t}\right) \\ &+ \frac{N_2\Gamma_2}{\xi + r^\star}\left(e^{-\xi t} - \Theta_2' e^{-\chi t}\right). \quad (519)\end{aligned}$$

Eq. (518) corresponds to eq. (27) in the main text.

Eq. (519) gives the trajectory for $B(t)$ consistent with the intertemporal solvency condition:

$$\left(\tilde{B} - B_0\right) = -\frac{\omega_B^1}{\nu_1 - r^\star} + \frac{\omega_B^2}{\xi + r^\star} \tag{520}$$

where we set

$$\omega_B^2 = \Xi_G \tilde{Y} \left(1 - \Theta'\right) + N_1 \Gamma_1 \left(1 - \Theta_1'\right) - N_2 \Gamma_2 \left(1 - \Theta_2'\right). \tag{521}$$

Eq. (520) corresponds to eq. (28) in the main text.

Differentiating (511a) w.r.t. time gives the trajectory for the current account along the transitional path when government spending follows the temporal path given by eq. (495):

$$\begin{aligned} \dot{B}(t) &= \nu_1 \frac{\omega_B^1}{\nu_1 - r^\star} e^{\nu_1 t} + \frac{\Xi_G \tilde{Y}}{\xi + r^\star} \left(\xi e^{-\xi t} - \chi \Theta' e^{-\chi t}\right) + \frac{N_1 \Gamma_1}{\xi + r^\star} \left(\xi e^{-\xi t} - \chi \Theta_1' e^{-\chi t}\right) \\ &- \frac{N_2 \Gamma_2}{\xi + r^\star} \left(\xi e^{-\xi t} - \chi \Theta_2' e^{-\chi t}\right). \end{aligned} \tag{522}$$

H.4 Formal Solution for the Stock of Financial Wealth, $A(t)$

To determine the formal solution for the stock of financial wealth, we first linearize the private savings equation (465) in the neighborhood of the steady-state and substitute the solutions for $K(t)$ and $Q(t)$:

$$\dot{A}(t) = r^\star \left(A(t) - \tilde{A}\right) + M_1 X_1(t) + M_2 X_2(t) + A_G dG(t), \tag{523}$$

where M_i (with $i = 1, 2$) is given by (472c), and A_G is given by:

$$A_G = \Lambda_P \frac{P_G^N \omega_{G^N}}{\tilde{P}} - 1, \tag{524}$$

where Λ_P is given by eq. (470b).

Substituting $X_1(t)$ given by eq. (512) and X_2 given by eq. (510) into (523) leads to:

$$\begin{aligned} \dot{A}(t) &= r^\star \left(A(t) - \tilde{A}\right) + \omega_A^1 e^{\nu_1 t} + M_1 \Gamma_1 \left(e^{-\xi t} - \Theta_1 e^{-\chi t}\right) \\ &- M_2 \Gamma_2 \left(e^{-\xi t} - \Theta_2 e^{-\chi t}\right) + A_G \tilde{Y} \left(e^{-\xi t} - (1 - g) e^{-\chi t}\right), \end{aligned} \tag{525}$$

where Γ_1 and Γ_2 are given by (501c) and (501d), respectively, and we set:

$$\omega_A^1 = M_1 \left[\left(K(0) - \tilde{K}\right) + \Gamma_2 \left(1 - \Theta_2\right) - \Gamma_1 \left(1 - \Theta_1\right)\right]. \tag{526}$$

Pre-multiplying by $e^{-r^\star \tau}$ and integrating over $(0, t)$ allow us to obtain the general solution for $A(t)$:

$$\begin{aligned} A(t) - \tilde{A} &= \left\{\left(A_0 - \tilde{A}\right) - \frac{\omega_A^1}{\nu_1 - r^\star} + \frac{A_G \tilde{Y}}{\xi + r^\star} \left(1 - \Theta'\right) + \frac{M_1 \Gamma_1}{\xi + r^\star} \left(1 - \Theta_1'\right) - \frac{M_2 \Gamma_2}{\xi + r^\star} \left(1 - \Theta_2'\right)\right\} e^{r^\star t} \\ &+ \frac{\omega_A^1}{\nu_1 - r^\star} e^{\nu_1 t} - \frac{A_G \tilde{Y}}{\xi + r^\star} \left(e^{-\xi t} - \Theta' e^{-\chi t}\right) - \frac{M_1 \Gamma_1}{\xi + r^\star} \left(e^{-\xi t} - \Theta_1' e^{-\chi t}\right) \\ &+ \frac{M_2 \Gamma_2}{\xi + r^\star} \left(e^{-\xi t} - \Theta_2' e^{-\chi t}\right), \end{aligned} \tag{527}$$

where Θ', Θ_1', Θ_2' are given by (518)-(518).

Invoking the transversality condition, one obtains the 'stable' solution for the stock of financial wealth so that $A(t)$ converges toward its steady-state value $\tilde{A}$:

$$\begin{aligned} A(t) - \tilde{A} &= \frac{\omega_A^1}{\nu_1 - r^\star} e^{\nu_1 t} - \frac{A_G \tilde{Y}}{\xi + r^\star} \left(e^{-\xi t} - \Theta' e^{-\chi t}\right) - \frac{M_1 \Gamma_1}{\xi + r^\star} \left(e^{-\xi t} - \Theta_1' e^{-\chi t}\right) \\ &+ \frac{M_2 \Gamma_2}{\xi + r^\star} \left(e^{-\xi t} - \Theta_2' e^{-\chi t}\right). \end{aligned} \tag{528}$$

Eq. (528) gives the trajectory for for $A(t)$ consistent with the intertemporal solvency condition:

$$\left(\tilde{A} - A_0\right) = -\frac{\omega_A^1}{\nu_1 - r^\star} + \frac{\omega_A^2}{\xi + r^\star} \tag{529}$$

where we set

$$\omega_A^2 = A_G \tilde{Y}\left(1 - \Theta'\right) + M_1\Gamma_1\left(1 - \Theta_1'\right) - M_2\Gamma_2\left(1 - \Theta_2'\right). \tag{530}$$

Differentiating (528) w.r.t. time gives the trajectory for the current account along the transitional path when government spending follows the temporal path given by eq. (495):

$$\begin{aligned}\dot{A}(t) &= \nu_1 \frac{\omega_A^1}{\nu_1 - r^\star} e^{\nu_1 t} + \frac{A_G\tilde{Y}}{\xi + r^\star}\left(\xi e^{-\xi t} - \chi\Theta' e^{-\chi t}\right) + \frac{M_1\Gamma_1}{\xi + r^\star}\left(\xi e^{-\xi t} - \chi\Theta_1' e^{-\chi t}\right) \\ &- \frac{M_2\Gamma_2}{\xi + r^\star}\left(\xi e^{-\xi t} - \chi\Theta_2' e^{-\chi t}\right). \end{aligned} \tag{531}$$

I Introducing Non-Separability between Consumption and Labor

In this section, we consider a more general form for preferences taken from Shimer [2011]. Since such preferences do not affect the first-order conditions from profit maximization, we do not repeat them and indicate major changes when solving the model.

In the baseline model, we assume that preferences are separable in consumption and leisure. We relax this assumption which implies that consumption and leisure can be substitutes. In particular, this more general specification implies that consumption can be affected by the wage rate while labor supply can be influenced by the change in the relative price of non tradables. As previously, the household's period utility function is increasing in its consumption C and decreasing in its labor supply L, with functional form:

$$\frac{C^{1-\sigma}V(L)^\sigma - 1}{1-\sigma}, \quad \text{if} \quad \sigma \neq 1, \quad V(L) \equiv \left(1 + (\sigma - 1)\gamma\frac{\sigma_L}{1+\sigma_L}L^{\frac{1+\sigma_L}{\sigma_L}}\right), \tag{532}$$

and

$$\log C - \gamma\frac{\sigma_L}{1+\sigma_L}L^{\frac{1+\sigma_L}{\sigma_L}}, \quad \text{if} \quad \sigma = 1. \tag{533}$$

These preferences are characterized by two pivotal parameters: σ_L which is the Frisch elasticity of labor supply, and $\sigma > 0$ that determines the substitutability between consumption and leisure; it is worth noticing that if $\sigma > 1$, the marginal utility of consumption is increasing in hours worked.

The representative household maximizes lifetime utility subject to the flow budget constraint (396) and the accumulation of physical capital (397). Denoting the co-state variables associated with (396) and (397) by λ and Q', respectively, the first-order conditions characterizing the representative household's optimal plans are:

$$C^{-\sigma}V(L)^\sigma = P_C\lambda, \tag{534a}$$

$$C^{1-\sigma}\sigma\gamma L^{1/\sigma_L}V(L)^{\sigma-1} = W\lambda, \tag{534b}$$

along with (405c)-(405e) and transversality conditions.

First-order conditions (534a) and (534b) can be solved for consumption and labor as follows:

$$C = C\left(\bar{\lambda}, P, W\right), \quad L = L\left(\bar{\lambda}, P, W\right). \tag{535}$$

To derive the partial derivatives, we take logarithm and totally differentiate the system which yields in matrix form:

$$\begin{pmatrix} -\sigma & \sigma\left(\frac{1+\sigma_L}{\sigma_L}\right)\left[\frac{V(L)-1}{V(L)}\right] \\ (1-\sigma) & \left\{\frac{1}{\sigma_L} + (\sigma-1)\left(\frac{1+\sigma_L}{\sigma_L}\right)\left[\frac{V(L)-1}{V(L)}\right]\right\} \end{pmatrix} \begin{pmatrix} \hat{C} \\ \hat{L} \end{pmatrix} \begin{pmatrix} \hat{\bar{\lambda}} + \alpha_C\hat{P} \\ \hat{\bar{\lambda}} + \hat{W} \end{pmatrix}, \tag{536}$$

where we denote by a hat the deviation in percentage.

Partial derivatives are:

$$\frac{\hat{C}}{\hat{\bar{\lambda}}} = \frac{(1+\sigma_L)}{\sigma}\left[\frac{V(L)-1}{V(L)}\right] - \frac{1}{\sigma} < 0, \tag{537a}$$

$$\frac{\hat{L}}{\hat{\bar{\lambda}}} = \frac{\sigma_L}{\sigma} > 0, \tag{537b}$$

$$\frac{\hat{C}}{\hat{W}} = (1+\sigma_L)\left[\frac{V(L)-1}{V(L)}\right] > 0, \tag{537c}$$

$$\frac{\hat{L}}{\hat{W}} = \sigma_L > 0, \tag{537d}$$

$$\frac{\hat{C}}{\hat{P}} = -\frac{\alpha_C}{\sigma}\left\{1+(\sigma-1)(1+\sigma_L)\left[\frac{V(L)-1}{V(L)}\right]\right\} < 0, \tag{537e}$$

$$\frac{\hat{L}}{\hat{P}} = -\alpha_C\frac{(\sigma-1)\,\sigma_L}{\sigma} < 0. \tag{537f}$$

Using the fact that $W = W\left(W^T, W^N\right)$ with $\frac{\partial W}{\partial W^T}\frac{W^T}{W} = (1-\alpha_L)$ and $\frac{\partial W}{\partial W^N}\frac{W^N}{W} = \alpha_L$, we get:

$$L = L\left(\bar{\lambda}, P, W^T, W^N\right), \tag{538}$$

where

$$\frac{\hat{L}}{\hat{W}^T} = (1-\alpha_L)\,\sigma_L > 0, \tag{539a}$$

$$\frac{\hat{L}}{\hat{W}^N} = \sigma_L\alpha_L > 0. \tag{539b}$$

Inserting first the short-run static solution for consumption given by (535) into $C^N = P_C' C$ and $C^T = \left[P_C - P P_C'\right] C$, one can solve for C^T and C^N as follows:

$$C^T = C^T\left(\bar{\lambda}, P, W^T, W^N\right), \quad C^N = C^N\left(\bar{\lambda}, P, W^T, W^N\right), \tag{540}$$

where partial derivatives are given by:

$$C_P^T = \frac{C^T}{P}\left(\alpha_C\phi + \frac{C_P P}{C}\right) \lesseqgtr 0, \tag{541a}$$

$$C_P^N = -\frac{C^N}{P}\left[(1-\alpha_C)\,\phi - \frac{C_P P}{C}\right] < 0, \tag{541b}$$

$$C_{W^T}^T = \frac{C^T}{W^T}(1-\alpha_L)\,\frac{C_W W}{C} > 0, \tag{541c}$$

$$C_{W^T}^N = \frac{C^N}{W^T}(1-\alpha_L)\,\frac{C_W W}{C} > 0, \tag{541d}$$

$$C_{W^N}^T = \frac{C^T}{W^N}\alpha_L\frac{C_W W}{C} > 0, \tag{541e}$$

$$C_{W^N}^N = \frac{C^N}{W^N}\alpha_L\frac{C_W W}{C} > 0. \tag{541f}$$

Inserting first the short-run solution for labor (538), into $L^T = \frac{\partial W\left(W^T, W^N\right)}{\partial W^T} L$ and $L^N = \frac{\partial W\left(W^T, W^N\right)}{\partial W^N} L$, allows us to solve for L^T and L^N:

$$L^T = L^T\left(\bar{\lambda}, W^T, W^N, P\right), \quad L^N = L^N\left(\bar{\lambda}, W^T, W^N, P\right), \tag{542}$$

where partial derivatives w.r.t. W^T and W^N are given by (169) and partial derivatives w.r.t. P are:

$$\frac{\hat{L}^T}{\hat{P}} = \frac{L^T}{P}\alpha_C(1-\sigma)\,\frac{\sigma_L}{\sigma} > 0, \tag{543a}$$

$$\frac{\hat{L}^N}{\hat{P}} = \frac{L^N}{P}\alpha_C(1-\sigma)\,\frac{\sigma_L}{\sigma} > 0. \tag{543b}$$

(543c)

I.1 Solving the Model

Plugging the short-run static solutions for L^T and L^N given by (542) into the resource constraint for capital (422), the system of four equations which comprises (421a)-(421c) together with (422) can be solved for sectoral wages and sectoral capital-labor ratios. Taking logarithm and differentiating (421a)-(421c) and (422) yields in matrix form:

$$\begin{pmatrix} -\theta^T & \theta^N & 0 & 0 \\ \left(1-\theta^T\right) & 0 & -1 & 0 \\ 0 & \left(1-\theta^N\right) & 0 & -1 \\ (1-\xi) & \xi & \Psi_{W^T} & \Psi_{W^N} \end{pmatrix} \begin{pmatrix} \hat{k}^T \\ \hat{k}^N \\ \hat{W}^T \\ \hat{W}^N \end{pmatrix} = \begin{pmatrix} \hat{P} \\ 0 \\ -\hat{P} \\ \hat{K} - \Psi_{\bar{\lambda}}\hat{\bar{\lambda}} - \Psi_P \hat{P} \end{pmatrix}, \tag{544}$$

where Ψ_{W^T} and Ψ_{W^N} are given by (430a) and (430b), respectively, $\xi \equiv \frac{k^N L^N}{K}$ and we set:

$$\Psi_P = (1-\xi)\frac{L^T_P P}{L^T} + \xi \frac{L^N_P P}{L^N} = -\alpha_C \frac{(\sigma-1)\,\sigma_L}{\sigma} < 0. \tag{545}$$

Only the partial derivatives w.r.t. P are modified when preferences are non separable in consumption and leisure. Hence, we thus restrict attention to these partial derivatives. Short-run static solutions for sectoral wages are:

$$W^T = W^T\left(\bar{\lambda}, K, P, Z^T, Z^N\right), \quad W^N = W^N\left(\bar{\lambda}, K, P, Z^T, Z^N\right), \tag{546}$$

with

$$\frac{\hat{W}^T}{\hat{P}} = -\frac{\left(1-\theta^T\right)\left(\Psi_{W^N} + \theta^N \Psi_P + \xi\right)}{G} < 0, \tag{547a}$$

$$\frac{\hat{W}^N}{\hat{P}} = -\frac{\left\{1 + \left(1-\theta^T\right)\Psi_{W^T} - \left(1-\theta^T\right)\xi - \theta^T\left(1-\theta^N\right)\Psi_P\right\}}{G} > 0, \tag{547b}$$

and sectoral capital-labor ratios:

$$k^T = k^T\left(\lambda, K, P, Z^T, Z^N\right), \quad k^N = k^N\left(\bar{\lambda}, K, P, Z^T, Z^N\right), \tag{548}$$

with

$$\frac{\hat{k}^T}{\hat{P}} = \frac{\Psi_{W^N} + \xi + \theta^N \Psi_P}{G} < 0, \tag{549a}$$

$$\frac{\hat{k}^N}{\hat{P}} = \frac{\left\{\theta^T\left(\Psi^{W^N} + \Psi_P\right) - \left[\left(1-\theta^T\right)\Psi_{W^T} + (1-\xi)\right]\right\}}{G} > 0, \tag{549b}$$

(549c)

To solve the model, insert first short-run static solutions for sectoral wages (546) into sectoral labor (542), then substitute the resulting solutions for sectoral labor and capital-labor ratios (549), production functions can be solved for sectoral outputs.

J Solving the Model with Public Debt

This section extends the two-sector model with imperfect mobility of labor to public debt. In order to avoid confusion, we denote by:

- K is the stock of physical capital;
- QK is the shadow value of the stock of physical capital;
- D is the stock of (traded) bonds issued by the government;
- B is the stock of traded bonds;
- $N = B - D$ is the net foreign asset position;
- $A = QK + N$ is the national non human wealth equal to the shadow value of the stock of physical capital plus the net foreign asset position which gives national savings $\dot{A}$;
- $\mathcal{A} = A + D = QK + N + D$ is non human wealth held by households which gives private savings $\dot{\mathcal{A}}$.

J.1 Government

The government issues traded bonds, D, in order to finance the excess of interest payments, $r^\star D$, government spending, and transfers, $Z(t)$, over taxes, $T(t)$:

$$\dot{D}(t) = r^\star D(t) + G(t) + Z(t) - T(t) \tag{550}$$

where we assume that the government raises taxes on labor:

$$T(t) = \tau(t) W(t) L(t). \tag{551}$$

with τ the wage tax levied on households' wage income.

J.2 Households

At each instant of time, the representative household consumes traded and non traded goods denoted by C^T and C^N, respectively, which are aggregated by means of a CES function:

$$C = \left[\varphi^{\frac{1}{\phi}} \left(C^T\right)^{\frac{\phi-1}{\phi}} + (1-\varphi)^{\frac{1}{\phi}} \left(C^N\right)^{\frac{\phi-1}{\phi}}\right]^{\frac{\phi}{\phi-1}}, \tag{552}$$

where $0 < \varphi < 1$ is the weight of the traded good in the overall consumption bundle and ϕ corresponds to the elasticity of substitution between traded goods and non traded goods.

As in De Cordoba and Kehoe [2000], the investment good is produced using inputs of the traded good and the non traded good according to a constant-returns-to-scale function which is assumed to take a CES form:

$$J \equiv J\left(J^T, J^N\right) = \left[\varphi_J^{\frac{1}{\phi_J}} \left(J^T\right)^{\frac{\phi_J-1}{\phi_J}} + (1-\varphi_J)^{\frac{1}{\phi_J}} \left(J^N\right)^{\frac{\phi_J-1}{\phi_J}}\right]^{\frac{\phi_J}{\phi_J-1}}, \tag{553}$$

where φ_J is the weight of the investment traded input ($0 < \varphi_J < 1$) and ϕ_J corresponds to the intratemporal elasticity of substitution in investment between traded and non traded inputs.

Following Horvath [2000], we assume that hours worked in the traded and the non traded sectors are aggregated by means of a CES function:

$$L = \left[\vartheta^{-1/\epsilon} \left(L^T\right)^{\frac{\epsilon+1}{\epsilon}} + (1-\vartheta)^{-1/\epsilon} \left(L^N\right)^{\frac{\epsilon+1}{\epsilon}}\right]^{\frac{\epsilon}{\epsilon+1}}, \tag{554}$$

and $0 < \vartheta < 1$ is the weight of labor supply to the traded sector in the labor index $L(.)$ and ϵ measures the ease with which hours worked can be substituted for each other and thereby captures the degree of labor mobility across sectors.

The representative household chooses consumption, decides on labor supply, and investment that maximizes his/her lifetime utility:

$$U = \int_0^\infty \left\{ \frac{1}{1-\frac{1}{\sigma_C}} C(t)^{1-\frac{1}{\sigma_C}} - \frac{1}{1+\frac{1}{\sigma_L}} L(t)^{1+\frac{1}{\sigma_L}} \right\} e^{-\beta t} \mathrm{d}t, \tag{555}$$

subject to the flow budget constraint:

$$\dot{B}(t) = r^\star B(t) + R(t)K(t) + W(t)\left(1-\tau\right)L(t) + Z(t) - P_C\left(P(t)\right)C(t) - P_J\left(P(t)\right)J(t), \tag{556}$$

and capital accumulation which evolves as follows:

$$\dot{K}(t) = I(t) - \delta_K K(t), \tag{557}$$

where I is investment and $0 \leq \delta_K < 1$ is a fixed depreciation rate. The first term on the RHS of (556) $r^\star B(t) + R(t)K(t) + W(t)\left(1-\tau\right)L(t) + Z(t)$ is the representative household's real disposable income while the second term on the RHS $P_C\left(P(t)\right)C(t) + P_J\left(P(t)\right)J(t)$ corresponds to consumption and investment expenditure including capital installation costs.

More specifically, we assume that capital accumulation is subject to increasing and convex cost of net investment (see (399)-(400)):

$$J(t) = I(t) + \frac{\kappa}{2}\left(\frac{I(t)}{K(t)} - \delta_K\right)^2 K(t), \tag{558}$$

Denoting the co-state variables associated with (556) and (557) by λ and Q', respectively, the first-order conditions characterizing the representative household's optimal plans are:

$$C(t) = \left(P_C(t)\lambda\right)^{-\sigma_C}, \tag{559a}$$

$$L(t) = \left(W(t)\left(1-\tau\right)\lambda\right)^{\sigma_L}, \tag{559b}$$

$$Q(t) = P_J(t)\left[1 + \kappa\left(\frac{I(t)}{K(t)} - \delta_K\right)\right], \tag{559c}$$

$$\dot{\lambda}(t) = \lambda\left(\beta - r^\star\right), \tag{559d}$$

$$\dot{Q}(t) = \left(r^\star + \delta_K\right)Q(t) - \left\{R(t) + P_J(t)\frac{\kappa}{2}\left(\frac{I(t)}{K(t)} - \delta_K\right)\left(\frac{I(t)}{K(t)} + \delta_K\right)\right\}, \tag{559e}$$

and the transversality conditions $\lim_{t\to\infty} \bar{\lambda}B(t)e^{-\beta t} = 0$ and $\lim_{t\to\infty} Q(t)K(t)e^{-\beta t} = 0$; to derive (559c) and (559e), we used the fact that $Q(t) = Q'(t)/\lambda(t)$.

Once households decided on aggregate consumption, they decide on the allocation of expenditure between traded and non traded goods:

$$C^N = (1-\varphi)\left(\frac{P}{P_C}\right)^{-\phi} C, \tag{560a}$$

$$C^T = \varphi\left(\frac{1}{P_C}\right)^{-\phi} C, \tag{560b}$$

where the consumption price index is:

$$P_C = \left[\varphi + (1-\varphi)P^{1-\phi}\right]^{\frac{1}{1-\phi}}. \tag{561}$$

As will be useful later, the percentage change in the consumption price index is proportional to the appreciation in the relative price of non tradables:

$$\hat{P}_C = \alpha_C \hat{P}, \tag{562}$$

where α_C is the non tradable content of consumption expenditure.

Once households decided on aggregate investment expenditure, they decide on the allocation between traded and non traded inputs:

$$J^N = (1-\varphi_J)\left(\frac{P}{P_J}\right)^{-\phi_J} J, \tag{563a}$$

$$J^T = \varphi\left(\frac{1}{P_J}\right)^{-\phi_J} J, \tag{563b}$$

where the investment price index is:

$$P_J = \left[\varphi_J + (1-\varphi_J)P^{1-\phi_J}\right]^{\frac{1}{1-\phi_J}}. \tag{564}$$

As will be useful later, the percentage change in the investment price index is proportional to the appreciation in the relative price of non tradables:

$$\hat{P}_J = \alpha_J \hat{P}, \tag{565}$$

where α_J is the non tradable content of investment expenditure.

Once households decided on aggregate labor supply, they allocate hours worked to the traded and the non traded sector

$$L^N = (1-\vartheta)\left(\frac{W^N}{W}\right)^{\epsilon} L, \tag{566a}$$

$$L^T = \vartheta\left(\frac{W^T}{W}\right)^{\epsilon} L, \tag{566b}$$

where the aggregate wage index is:

$$W = \left[\vartheta\left(W^T\right)^{\epsilon+1} + (1-\vartheta)\left(W^N\right)^{\epsilon+1}\right]^{\frac{1}{\epsilon+1}}. \tag{567}$$

As will be useful later, the percentage change in the aggregate wage index is a weighted average of percentage changes in sectoral wages:

$$\hat{W} = \alpha_L \hat{W}^N + (1-\alpha_L)\hat{W}^T, \tag{568}$$

where α_L is the non tradable content of aggregate labor compensation.

J.3 Firms

Both the traded and non-traded sectors use physical capital, K^j, and labor, L^j, according to constant returns to scale production functions $Y^j = Z^j F\left(K^j, L^j\right)$ which are assumed to take a Cobb-Douglas form:

$$Y^j = Z^j\left(L^j\right)^{\theta^j}\left(K^j\right)^{1-\theta^j}, \tag{569}$$

where θ^j is the labor income share in sector j and Z^j corresponds to the total factor productivity index which is introduced for calibration purposes. Both sectors face two cost components: a capital rental cost equal to R, and a labor cost equal to the wage rate, i.e., W^T in the traded sector and W^N in the non traded sector.

Both sectors are assumed to be perfectly competitive and thus choose capital and labor by taking prices as given:

$$\max_{K^j,L^j} \Pi^j = \max_{K^j,L^j}\left\{P^j Y^j - W^j L^j - RK^j\right\}. \tag{570}$$

Since capital can move freely between the two sectors, the value of marginal products in the traded and non traded sectors equalizes while costly labor mobility implies a wage differential across sectors:

$$Z^T\left(1-\theta^T\right)\left(k^T\right)^{-\theta^T} = PZ^N\left(1-\theta^N\right)\left(k^N\right)^{-\theta^N} \equiv R, \tag{571a}$$

$$Z^T\theta^T\left(k^T\right)^{1-\theta^T} \equiv W^T, \tag{571b}$$

$$PZ^N\theta^N\left(k^N\right)^{1-\theta^N} \equiv W^N, \tag{571c}$$

where $k^j \equiv K^j/L^j$ denotes the capital-labor ratio for sector $j = T, N$.

The resource constraint for capital is:

$$K^T + K^N = K. \tag{572}$$

J.4 Solving the Model

Before linearizing, we have to determine short-run static solutions. First-order conditions (559a) and (559b) can be solved for consumption and aggregate labor supply which of course must hold at any point of time:

$$C = C\left(\bar{\lambda}, P\right), \quad L = L\left(\bar{\lambda}, W^T, W^N, \tau\right), \tag{573}$$

with partial derivatives given by

$$\hat{C} = -\sigma_C\hat{\bar{\lambda}} - \sigma_C\alpha_C\hat{P}, \tag{574a}$$

$$\hat{L} = \sigma_L\hat{\bar{\lambda}} + \sigma_L\alpha_L\hat{W}^N + \sigma_L(1-\alpha_L)\hat{W}^T - \sigma_L\frac{d\tau}{1-\tau}. \tag{574b}$$

Inserting first the solution for consumption (575) into (560) allows us to solve for C^T and C^N:

$$C^T = C^T\left(\bar{\lambda}, P\right), \quad C^N = C^N\left(\bar{\lambda}, P\right), \tag{575}$$

with partial derivatives given by

$$\hat{C}^N = -\left[(1-\alpha_C)\phi + \alpha_C\sigma_C\right]\hat{P} - \sigma_C\hat{\bar{\lambda}}, \tag{576a}$$

$$\hat{C}^N = \alpha_C\left(\phi - \sigma_C\right)\hat{P} - \sigma_C\hat{\bar{\lambda}}. \tag{576b}$$

Inserting first the solution for labor (575) into (566) allows us to solve for L^T and L^N:

$$L^T = L^T\left(\bar{\lambda}, W^T, W^N, \tau\right), \quad L^N = L^N\left(\bar{\lambda}, W^T, W^N, \tau\right), \tag{577}$$

with partial derivatives given by:

$$\hat{L}^T = \left[\epsilon\alpha_L + \sigma_L\left(1-\alpha_L\right)\right]\hat{W}^T + \alpha_L\left(\sigma_L - \epsilon\right)\hat{W}^N + \sigma_L\hat{\bar{\lambda}} - \sigma_L\frac{d\tau}{1-\tau}, \tag{578a}$$

$$\hat{L}^N = \left[\epsilon\left(1-\alpha_L\right) + \sigma_L\alpha_L\right]\hat{W}^N + \left(1-\alpha_L\right)\left(\sigma_L - \epsilon\right)\hat{W}^T + \sigma_L\hat{\bar{\lambda}} - \sigma_L\frac{d\tau}{1-\tau}. \tag{578b}$$

Plugging the short-run static solutions for L^T and L^N given by (577) into the resource constraint for capital (574), the system of four equations consisting of (571a)-(571c) together with (574) can be solved for sectoral wages W^j and sectoral capital-labor ratios k^j. Keeping TFPs unchanged, denoting by $\xi^N \equiv K^N/K$ the share of non traded capital in the aggregate stock of physical capital and log-differentiating (421a)-(421c) and (422) yields in matrix form:

$$\begin{pmatrix} -\theta^T & \theta^N & 0 & 0 \\ \left(1-\theta^T\right) & 0 & -1 & 0 \\ 0 & \left(1-\theta^N\right) & 0 & -1 \\ \left(1-\xi^N\right) & \xi^N & \Psi_{W^T} & \Psi_{W^N} \end{pmatrix} \begin{pmatrix} \hat{k}^T \\ \hat{k}^N \\ \hat{W}^T \\ \hat{W}^N \end{pmatrix}$$

$$= \begin{pmatrix} \hat{P} \\ 0 \\ -\hat{P} \\ \hat{K} - \Psi_{\bar{\lambda}}\hat{\bar{\lambda}} - \Psi_\tau\frac{d\tau}{1-\tau} \end{pmatrix}, \tag{579}$$

where we set:

$$\Psi_{W^T} = \left(1-\xi^N\right)\frac{L^T_{W^T}W^T}{L^T} + \xi^N\frac{L^N_{W^T}W^T}{L^N}, \tag{580a}$$

$$\Psi_{W^N} = \left(1-\xi^N\right)\frac{L^T_{W^N}W^N}{L^T} + \xi^N\frac{L^N_{W^N}W^N}{L^N}, \tag{580b}$$

$$\xi^N \equiv \frac{k^N L^N}{K}, \tag{580c}$$

$$\Psi_{\bar{\lambda}} = \left(1-\xi^N\right)\sigma_L + \xi^N\sigma_L = \sigma_L. \tag{580d}$$

The short-run static solutions for sectoral wages and capital-labor ratios are:

$$W^j = W^j\left(\bar{\lambda}, K, P, \tau\right), \quad k^j = k^j\left(\bar{\lambda}, K, P, \tau\right). \tag{581}$$

Inserting first sectoral wages (581), sectoral employment (577) can be solved as functions of the shadow value of wealth, the capital stock and the relative price of non tradables:

$$L^j = L^j\left(\bar{\lambda}, K, P, \tau\right). \tag{582}$$

Finally, plugging solutions for sectoral labor (582) and sector capital-labor ratios (581), the production functions (569) can be solved for sectoral output:

$$Y^j = Y^j\left(\bar{\lambda}, K, P, \tau\right). \tag{583}$$

The Return on Domestic Capital, R

The return on domestic capital is:

$$R = Z^T \left(1-\theta^T\right) \left(k^T\right)^{-\theta^T}. \tag{584}$$

Inserting first the short-run static solution for the capital-labor ratio k^T given by (581), eq. (584) can be solved for the return on domestic capital:

$$R = R\left(\bar{\lambda}, K, P, \tau\right). \tag{585}$$

The Relative Price of Non Tradables, P

Finally, we have to solve for the relative price of non tradables by using the non traded goods market clearing condition:

$$Y^N = C^N + G^N + J^N. \tag{586}$$

Remembering that the non traded input J^N used to produce investment goods is equal to $P_J' J$, inserting solutions for C^N and Y^N given by (575) and (583), respectively, and substituting (446), the non traded goods market clearing condition (586) can be rewritten as follows:

$$Y^N\left(\bar{\lambda}, K, P, \tau\right) = C^N\left(\bar{\lambda}, P\right) + G^N + P_J' K\left[v(.) + \delta_K + \frac{\kappa}{2}\left(v(.)\right)^2\right]. \tag{587}$$

Eq. (587) can be solved for the relative price of non tradables:

$$P = P\left(\bar{\lambda}, K, Q, G^N, \tau\right), \tag{588}$$

with partial derivatives given by:

$$P_K = \frac{\partial P}{\partial K} = \frac{-\frac{Y_K^N}{P_J'} + \frac{J}{K}}{\Psi^P} \lessgtr 0, \tag{589a}$$

$$P_Q = \frac{\partial P}{\partial Q} = \frac{K v_Q \left[1 + \kappa v(.)\right]}{\Psi^P} > 0, \tag{589b}$$

$$P_{G^N} = \frac{1}{P_J' \Psi^P} > 0, \tag{589c}$$

$$P_\tau = -\frac{Y_\tau^N}{P_J' \Psi^P} > 0, \tag{589d}$$

where we set

$$\Psi^P = \left[\left(Y_P^N - C_P^N\right) + \frac{J^N \phi_J \left(1-\alpha_J\right)}{P}\right]\frac{1}{P_J'} - K v_P \left[1 + \kappa v(.)\right] > 0. \tag{590}$$

J.5 Formal Solutions for public debt $D(t)$

Like Gali, Lopez-Salido and Vallès [2007], we assume a fiscal policy rule of the (linearized) form:

$$dT(t) = \phi_D dD(t) + \phi_G dG(t), \tag{591}$$

where $dT(t) = T(t) - \tilde{T}$, $dD(t) = D(t) - \tilde{D}$, and $dG(t) = G(t) - \tilde{G}$. Linearizing first the government budget constraint (550), inserting the fiscal rule (591) and collecting terms yields:

$$\begin{aligned} \dot{D}t &= r^\star\left(D(t) - \tilde{D}\right) + \left(G(t) - \tilde{G}\right) - \left(T(t) - \tilde{T}\right), \\ &= \left(r^\star - \phi_D\right)\left(D(t) - \tilde{D}\right) + \left(1 - \phi_G\right)\left(G(t) - \tilde{G}\right). \end{aligned} \tag{592}$$

Inserting the dynamic equation for $\frac{dG(t)}{Y}$ given by eq. (495) into (592) and solving the differential equation leads to:

$$\frac{\left(D(t) - \tilde{D}\right)}{Y} = \left[\frac{\left(D_0 - \tilde{D}\right)}{Y} + \Theta_D\right] e^{-\delta t} - \left[\Theta_1 e^{-\xi t} - \Theta_2 e^{-\chi t}\right], \tag{593}$$

where we set

$$\Theta_D = (1-\phi_G)\left[\frac{1}{\xi + r^\star - \phi_D} - \frac{(1-g)}{\chi + r^\star - \phi_D}\right], \quad (594a)$$

$$\Theta_1 = \frac{(1-\phi_G)}{\xi + r^\star - \phi_D}, \quad (594b)$$

$$\Theta_2 = \frac{(1-\phi_G)(1-g)}{\chi + r^\star - \phi_D}, \quad (594c)$$

$$\delta = r^\star - \phi_D. \quad (594d)$$

We assume that initial public debt is nil, i.e., $D_0 = 0$. Since public debt is back to its initial level in the long-run following a temporary rise in government spending, we have $\tilde{D} = 0$. Inserting (593) into (591) along with the dynamic equation for government spending (495) leads to the temporal path for taxes in percentage point of GDP:

$$\begin{aligned}\frac{dT(t)}{Y} &= \phi_D \Theta_D e^{-\delta t} - \phi_D\left[\Theta_1 e^{-\xi t} - \Theta_2 e^{-\chi t}\right] + \phi_G\left[e^{-\xi t} - (1-g)\, e^{-\chi t}\right], \\ &= \phi_D \Theta_D e^{-\delta t} - \left\{\left[\phi_D \Theta_1 - \phi_G\right] e^{-\delta t} - \left[\phi_D \Theta_2 - \phi_G (1-g)\right] e^{-\chi t}\right\}. \quad (595)\end{aligned}$$

Dividing (551) by GDP and denoting by θ_L the aggregate labor income share, we have:

$$\frac{T(t)}{Y} = \theta_L(t)\tau(t). \quad (596)$$

Because the aggregate labor income share is a weighted average of sectoral labor income shares, i.e., $\theta_L = \frac{P(t)Y^N(t)}{Y(t)}\theta^N + \frac{Y^T(t)}{Y(t)}\theta^T$, θ_L varies over time. In order to avoid unnecessary complications, we assume that θ_L is fixed, i.e., $\theta_L(t) = \theta_L$, and thus the adjustment in tax receipts is achieved through changes in the labor tax rate only. Linearizing first (596) and substituting (595), the deviation of the labor tax relative to its initial value is:

$$\begin{aligned}d\tau(t) &= \frac{1}{\theta_L}\frac{dT(t)}{Y}, \\ &= \Omega_D e^{-\delta t} - \left(\Omega_1 e^{-\xi t} - \Omega_2 e^{-\chi t}\right), \quad (597)\end{aligned}$$

where we set

$$\Omega_D = \frac{\phi_D \Theta_D}{\theta_L}, \quad (598a)$$

$$\Omega_1 = \frac{\phi_D \Theta_1 - \phi_G}{\theta_L}, \quad (598b)$$

$$\Omega_2 = \frac{\phi_D \Theta_2 - \phi_G (1-g)}{\theta_L}. \quad (598c)$$

J.6 Formal Solutions for $K(t)$ and $Q(t)$

Remembering that the non traded input J^N used to produce the capital good is equal to $P_J' J$, using the fact that $J^N = Y^N - C^N - G^N$ and inserting $I = \dot{K} + \delta_K$, the capital accumulation equation can be rewritten as follows:

$$\dot{K} = \frac{Y^N - C^N - G^N}{P_J'} - \delta_K K - \frac{\kappa}{2}\left(\frac{I}{K} - \delta_K\right)^2 K. \quad (599)$$

Using the fact that $\frac{\partial G^N}{\partial G} = \frac{\omega_{G^N}}{P}$, inserting short-run static solutions for non traded output (583), consumption in non tradables (575), and optimal investment decision (443) into the physical capital accumulation equation (591) and the dynamic equation for the shadow value (559e), the dynamic system is:

$$\begin{aligned}\dot{K} \equiv \Upsilon\left(K, P(.), Q, G, \tau\right) &= \frac{Y^N\left(K, P(.), \bar{\lambda}\right) - C^N\left(\bar{\lambda}, P(.)\right) - G^N}{P_J'\left(P(.)\right)} \\ &\quad -\delta_K K - \frac{K}{2\kappa}\left[\frac{Q}{P_J\left(P(.)\right)} - 1\right]^2, \quad (600a) \\ \dot{Q} \equiv \Sigma\left(K, P, Q, G, \tau\right) &= \left(r^\star + \delta_K\right) Q - \left[R\left(K, P(.)\right) + P_J \frac{\kappa}{2} v(.)\left(v(.) + 2\delta_K\right)\right] (600b)\end{aligned}$$

The linearized system can be written in a matrix form:

$$\begin{pmatrix} \dot{K}(t) \\ \dot{Q}(t) \end{pmatrix} = \begin{pmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{pmatrix} \begin{pmatrix} K(t) - \tilde{K} \\ Q(t) - \tilde{Q} \end{pmatrix} + \begin{pmatrix} \varepsilon_K^G dG(t) + \varepsilon_K^\tau d\tau(t) \\ \varepsilon_Q^G dG(t) + \varepsilon_Q^\tau d\tau(t) \end{pmatrix}, \tag{601}$$

where the coefficients of the Jacobian matrix are given by (501) and the direct effects of changes in government consumption captured by the terms ε_K^G and ε_Q^G are described by (502). The direct effects of changes in the labor tax rate on K and Q are described by:

$$\varepsilon_K^\tau = \frac{Y_\tau^N}{P_J'} + \Upsilon_P P_\tau, \tag{602a}$$

$$\varepsilon_Q^\tau = -R_\tau + \Sigma_P P_\tau, \tag{602b}$$

where $\Upsilon_P = \Upsilon_P\left(\tilde{K}, \tilde{Q}, \tilde{G}, \tilde{\tau}\right)$ and $\Sigma_P = \Sigma_P\left(\tilde{K}, \tilde{Q}, \tilde{G}, \tilde{\tau}\right)$.

Denoting the negative eigenvalue by ν_1 and the positive eigenvalue by ν_2, the general solutions for K and Q can be written as follows:

$$K(t) - \tilde{K} = X_1(t) + X_2(t), \quad Q(t) - \tilde{Q} = \omega_2^1 X_1(t) + \omega_2^2 X_2(t). \tag{603}$$

where $X_1(t)$ and $X_2(t)$ characterize the trajectory of physical capital and the shadow value of capital. To express these terms in compact form, we set:

$$\Phi_1^l = \left[(a_{11} - \nu_2)\,\varepsilon_K^l + a_{12}\varepsilon_Q^l\right], \tag{604a}$$

$$\Phi_2^l = \left[(a_{11} - \nu_1)\,\varepsilon_K^l + a_{12}\varepsilon_Q^l\right]. \tag{604b}$$

where $l = G, \tau$, along with

$$\Gamma_i^G = -\frac{\Phi_i^G \tilde{Y}}{(\nu_1 - \nu_2)(\nu_i + \xi)}, \tag{605a}$$

$$\Theta_i^G = (1-g)\frac{(\xi + \nu_i)}{(\chi + \nu_i)}, \tag{605b}$$

$$\Gamma_i^D = -\frac{\Phi_i^\tau \Omega_D}{(\nu_1 - \nu_2)(\nu_i + \delta)}, \tag{605c}$$

$$\Gamma_i^\tau = -\frac{\Phi_i^\tau \Omega_1}{(\nu_1 - \nu_2)(\nu_i + \xi)}, \tag{605d}$$

$$\Theta_i^\tau = \frac{\Omega_2}{\Omega_1}\left(\frac{\xi + \nu_i}{\chi + \nu_i}\right). \tag{605e}$$

where $i = 1, 2$.

Adopting the same procedure as in section H.2, solutions for $X_1(t)$ and $X_2(t)$ are given by:

$$\begin{aligned} X_1(t) &= e^{\nu_1 t}\left\{X_1(0) - \Gamma_1^G\left(1 - \Theta_1^G\right) - \Gamma_1^D + \Gamma_1^\tau\left(1 - \Theta_1^\tau\right)\right\} \\ &+ \Gamma_1^G\left(e^{-\xi t} - \Theta_1^G e^{-\chi t}\right) + \Gamma_1^D e^{-\delta t} - \Gamma_1^\tau\left(e^{-\xi t} - \Theta_1^\tau e^{-\chi t}\right), \end{aligned} \tag{606a}$$

$$X_2(t) = -\Gamma_2^G\left(e^{-\xi t} - \Theta_2^G e^{-\chi t}\right) - \Gamma_2^D e^{-\delta t} + \Gamma_2^\tau\left(e^{-\xi t} - \Theta_2^\tau e^{-\chi t}\right), \tag{606b}$$

where

$$X_1(0) = K_0 - \tilde{K} - X_2(0). \tag{607}$$

J.7 Formal Solutions for the Net Foreign Asset Position $N(t)$

To determine the dynamic equation for the net foreign asset position, $N(t)$, we differentiate $N(t) = B(t) - D(t)$ w.r.t. time and substitute the dynamic equations for the stock of traded bonds (556) and for the public debt (550):

$$\begin{aligned} \dot{N}(t) &= \dot{B}(t) - \dot{D}(t), \\ &= r^\star N(t) + R(t)K(t) + W(t)L(t) - P_C(P(t))C(t) - P_J(P(t))J(t) - G(t) \end{aligned} \tag{608}$$

Inserting the market clearing condition for non tradables (586) and remembering that $J^T = (1-\alpha_J) P_J J$, the current account equation is given by:

$$\begin{aligned}
\dot{N} &\equiv \Xi(N, K, Q, G), \\
&= r^\star N + Y^T - C^T - G^T - (1-\alpha_J) P_J J, \\
&= r^\star B + Y^T - C^T - G^T - \left(\frac{1-\alpha_J}{\alpha_J}\right) P \left(Y^N - C^N - G^N\right),
\end{aligned} \tag{609}$$

where we used the fact that $P_J' J = Y^N - C^N - G^N$.

Linearizing first the current account equation (609) in the neighborhood of the steady-state and substitute the solutions for $K(t)$ and $Q(t)$ leads to:

$$\dot{N}(t) = r^\star dN(t) + N_1 X_1(t) + N_2 X_2(t) + \Xi_G dG(t) + \Xi_\tau d\tau(t), \tag{610}$$

where $N_i = \Xi_K + \Xi_Q \omega_2^i$ (with $i = 1, 2$), Ξ_G is given by (514) and Ξ_τ reads as follows:

$$\Xi_\tau = \Xi_P P_\tau + Y_\tau^T - \left(\frac{1-\alpha_J}{\alpha_J}\right) \tilde{P} Y_\tau^N, \tag{611}$$

where $\Xi_P < 0$ is given by (461b).

Substituting $X_1(t)$ given by eq. (512) and $X_2(t)$ given by eq. (606a) into (606b) leads to:

$$\begin{aligned}
\dot{N}(t) &= r^\star dN(t) + \omega_N^1 e^{\nu_1 t} + N_1 \Gamma_1^G \left(e^{-\xi t} - \Theta_1^G e^{-\chi t}\right) + N_1 \Gamma_1^D e^{-\delta t} \\
&- N_1 \Gamma_1^\tau \left(e^{-\xi t} - \Theta_1^\tau e^{-\chi t}\right) - N_2 \Gamma_2^G \left(e^{-\xi t} - \Theta_2^G e^{-\chi t}\right) - N_2 \Gamma_2^D e^{-\delta t} + N_2 \Gamma_2^\tau \left(e^{-\xi t} - \Theta_2^\tau e^{-\chi t}\right) \\
&+ \Xi_G \tilde{Y} \left(e^{-\xi t} - (1-g) e^{-\chi t}\right) + \Xi_\tau \Omega_D e^{-\delta t} - \Xi_\tau \left(\Omega_1 e^{-\xi t} - \Omega_2 e^{-\chi t}\right),
\end{aligned} \tag{612}$$

where Γ_i^l (with $l = G, \tau, D$, and $i = 1, 2$) is given by (605a), (605b), (605c) and we set:

$$\begin{aligned}
\omega_N^1 &= N_1 \Big[\left(K(0) - \tilde{K}\right) + \Gamma_2^G \left(1 - \Theta_2^G\right) + \Gamma_2^D - \Gamma_2^\tau \left(1 - \Theta_2^\tau\right) \\
&- \Gamma_1^G \left(1 - \Theta_1^G\right) - \Gamma_1^D + \Gamma_1^\tau \left(1 - \Theta_2^\tau\right) \Big].
\end{aligned} \tag{613}$$

Solving the differential equation (612) yields the general solution for the net foreign asset position:

$$\begin{aligned}
N(t) - \tilde{N} &= \Bigg\{ \left(N_0 - \tilde{N}\right) - \frac{\omega_N^1}{\nu_1 - r^\star} + \frac{\Xi_G \tilde{Y}}{\xi + r^\star} \left(1 - \Theta^{G,\prime}\right) + \frac{\Xi_\tau \Omega_D}{\delta + r^\star} - \frac{\Xi_\tau \Omega_1}{\xi + r^\star} \left(1 - \Theta^{\tau,\prime}\right) \\
&+ \frac{N_1 \Gamma_1^G}{\xi + r^\star} \left(1 - \Theta_1^{G,\prime}\right) + \frac{N_1 \Gamma_1^D}{\delta + r^\star} - \frac{N_1 \Gamma_1^\tau}{\xi + r^\star} \left(1 - \Theta_1^{\tau,\prime}\right) \\
&- \frac{N_2 \Gamma_2^G}{\xi + r^\star} \left(1 - \Theta_2^{G,\prime}\right) - \frac{N_2 \Gamma_2^D}{\delta + r^\star} + \frac{N_2 \Gamma_2^\tau}{\xi + r^\star} \left(1 - \Theta_2^{\tau,\prime}\right) \Bigg\} e^{r^\star t} \\
&+ \frac{\omega_N^1}{\nu_1 - r^\star} e^{\nu_1 t} - \frac{\Xi_G \tilde{Y}}{\xi + r^\star} \left(e^{-\xi t} - \Theta^{G,\prime} e^{-\chi t}\right) - \frac{\Xi_\tau \Omega_D}{\delta + r^\star} e^{-\delta t} + \frac{\Xi_\tau \Omega_1}{\xi + r^\star} \left(e^{-\xi t} - \Theta^{\tau,\prime} e^{-\chi t}\right) \\
&- \frac{N_1 \Gamma_1^G}{\xi + r^\star} \left(e^{-\xi t} - \Theta_1^{G,\prime} e^{-\chi t}\right) - \frac{N_1 \Gamma_1^D}{\delta + r^\star} + \frac{N_1 \Gamma_1^\tau}{\xi + r^\star} \left(e^{-\xi t} - \Theta_1^{\tau,\prime} e^{-\chi t}\right) \\
&+ \frac{N_2 \Gamma_2^G}{\xi + r^\star} \left(1 - \Theta_2^{G,\prime}\right) + \frac{N_2 \Gamma_2^D}{\delta + r^\star} - \frac{N_2 \Gamma_2^\tau}{\xi + r^\star} \left(1 - \Theta_2^{\tau,\prime}\right),
\end{aligned} \tag{614}$$

where we set:

$$\Theta^{G,\prime} = (1-g)\frac{\xi+r^\star}{\chi+r^\star}, \tag{615a}$$

$$\Theta_1^{G,\prime} = \Theta_1^G\frac{\xi+r^\star}{\chi+r^\star}, \tag{615b}$$

$$\Theta_2^{G,\prime} = \Theta_2^G\frac{\xi+r^\star}{\chi+r^\star}, \tag{615c}$$

$$\Theta^{\tau,\prime} = \frac{\Omega_2}{\Omega_1}\frac{\xi+r^\star}{\chi+r^\star}, \tag{615d}$$

$$\Theta_1^{\tau,\prime} = \Theta_1^\tau\frac{\xi+r^\star}{\chi+r^\star}, \tag{615e}$$

$$\Theta_2^{\tau,\prime} = \Theta_2^\tau\frac{\xi+r^\star}{\chi+r^\star}. \tag{615f}$$

Invoking the transversality condition, one obtains the 'stable' solution for the stock of net foreign assets so that $N(t)$ converges toward its steady-state value $\tilde{N}$:

$$\begin{aligned} N(t)-\tilde{N} &= \frac{\omega_N^1}{\nu_1-r^\star}e^{\nu_1 t} - \frac{\Xi_G\tilde{Y}}{\xi+r^\star}\left(e^{-\xi t}-\Theta^{G,\prime}e^{-\chi t}\right) - \frac{\Xi_\tau\Omega_D}{\delta+r^\star}e^{-\delta t} + \frac{\Xi_\tau\Omega_1}{\xi+r^\star}\left(e^{-\xi t}-\Theta^{\tau,\prime}e^{-\chi t}\right) \\ &- \frac{N_1\Gamma_1^G}{\xi+r^\star}\left(e^{-\xi t}-\Theta_1^{G,\prime}e^{-\chi t}\right) - \frac{N_1\Gamma_1^D}{\delta+r^\star}e^{-\delta t} + \frac{N_1\Gamma_1^\tau}{\xi+r^\star}\left(e^{-\xi t}-\Theta_1^{\tau,\prime}e^{-\chi t}\right) \\ &+ \frac{N_2\Gamma_2^G}{\xi+r^\star}\left(e^{-\xi t}-\Theta_2^{G,\prime}e^{-\chi t}\right) + \frac{N_2\Gamma_2^D}{\delta+r^\star}e^{-\delta t} - \frac{N_2\Gamma_2^\tau}{\xi+r^\star}\left(e^{-\xi t}-\Theta_2^{\tau,\prime}e^{-\chi t}\right). \end{aligned} \tag{616}$$

Eq. (616) gives the trajectory for for $N(t)$ consistent with the intertemporal solvency condition:

$$\left(\tilde{N}-N_0\right) = -\frac{\omega_N^1}{\nu_1-r^\star} + \frac{\omega_N^G}{\xi+r^\star} + \frac{\omega_N^D}{\delta+r^\star} + \frac{\omega_N^\tau}{\xi+r^\star}, \tag{617}$$

where ω_N^1 is given by (613) and we set

$$\omega_N^G = \Xi_G\tilde{Y}\left(1-\Theta^{G,\prime}\right) + N_1\Gamma_1^G\left(1-\Theta_1^{G,\prime}\right) - N_2\Gamma_2^G\left(1-\Theta_2^{G,\prime}\right), \tag{618a}$$

$$\omega_N^D = \Xi_\tau\Omega_D - N_1\Gamma_1^D + N_2\Gamma_2^D, \tag{618b}$$

$$\omega_N^\tau = -\Xi_\tau\Omega_1\left(1-\Theta^{\tau,\prime}\right) - N_1\Gamma_1^\tau\left(1-\Theta_1^{\tau,\prime}\right) + N_2\Gamma_2^\tau\left(1-\Theta_2^{\tau,\prime}\right). \tag{618c}$$

Differentiating (616) w.r.t. time gives the trajectory for the current account along the transitional path when government spending follows the temporal path given by eq. (495) and the labor tax rate is governed by the dynamic equation (597)

$$\begin{aligned} \dot{N}(t) &= \nu_1\frac{\omega_N^1}{\nu_1-r^\star}e^{\nu_1 t} + \frac{\Xi_G\tilde{Y}}{\xi+r^\star}\left(\xi e^{-\xi t}-\chi\Theta^{G,\prime}e^{-\chi t}\right) + \delta\frac{\Xi_\tau\Omega_D}{\delta+r^\star}e^{-\delta t} - \frac{\Xi_\tau\Omega_1}{\xi+r^\star}\left(\xi e^{-\xi t}-\chi\Theta^{\tau,\prime}e^{-\chi t}\right) \\ &+ \frac{N_1\Gamma_1^G}{\xi+r^\star}\left(\xi e^{-\xi t}-\chi\Theta_1^{G,\prime}e^{-\chi t}\right) + \delta\frac{N_1\Gamma_1^D}{\delta+r^\star}e^{-\delta t} - \frac{N_1\Gamma_1^\tau}{\xi+r^\star}\left(\xi e^{-\xi t}-\chi\Theta_1^{\tau,\prime}e^{-\chi t}\right) \\ &- \frac{N_2\Gamma_2^G}{\xi+r^\star}\left(\xi e^{-\xi t}-\chi\Theta_2^{G,\prime}e^{-\chi t}\right) + \frac{N_2\Gamma_2^D}{\delta+r^\star}e^{-\delta t} + \frac{N_2\Gamma_2^\tau}{\xi+r^\star}\left(\xi e^{-\xi t}-\chi\Theta_2^{\tau,\prime}e^{-\chi t}\right). \end{aligned} \tag{619}$$

J.8 Formal Solution for the Stock of Non Human Wealth, $A(t)$

Remembering that the stock of national non human wealth $A(t)$ is equal to $N(t)+Q(t)K(t)$, differentiating w.r.t. time, i.e., $\dot{A}(t) = \dot{B}(t) - \dot{D}(t) + \dot{Q}(t)K(t) + Q(t)\dot{K}(t)$, plugging the dynamic equation for the shadow value of capital (559e), inserting the accumulation equations for physical capital (557), traded bonds (556), traded bonds issued by the government (550) and using the specification of capita adjustment costs (558) along with the first order condition (559d) yields the accumulation equation for the stock of national non human wealth or the dynamic equation for national savings:

$$\dot{A}(t) = r^\star A(t) + W(t)L(t) - P_C\left(P(t)\right)C(t) - G(t). \tag{620}$$

We first determine short-run static solutions for aggregate labor supply and aggregate wage index. Inserting solutions for sectoral wages (581) into the solution for aggregate labor supply (575), one can solve for total hours worked:

$$L = L\left(\bar{\lambda}, K, P, \tau\right), \tag{621}$$

where partial derivatives are given by

$$\begin{aligned} L_K &\equiv \frac{\partial L}{\partial K} = L_{W^T} W_K^T + L_{W^N} W_K^N, &(622a)\\ L_P &\equiv \frac{\partial L}{\partial P} = L_{W^T} W_P^T + L_{W^N} W_P^N, &(622b)\\ L_\tau &\equiv \frac{\partial L}{\partial \tau} = L_{W^T} W_\tau^T + L_{W^N} W_\tau^N. &(622c)\end{aligned}$$

Substituting solutions for sectoral wages (433) into the aggregate wage index $W \equiv W\left(W^T, W^N\right)$, we can solve for the aggregate wage index:

$$W = W\left(\bar{\lambda}, K, P, \tau\right), \tag{623}$$

where partial derivatives are given by

$$\begin{aligned} W_K &\equiv \frac{\partial W}{\partial K} = W_{W^T} W_K^T + W_{W^N} W_K^N, &(624a)\\ W_P &\equiv \frac{\partial W}{\partial P} = W_{W^T} W_P^T + W_{W^N} W_P^N, &(624b)\\ W_\tau &\equiv \frac{\partial W}{\partial P} = W_{W^T} W_\tau^T + W_{W^N} W_\tau^N, &(624c)\end{aligned}$$

with $W_{W^T} = \left(W/W^T\right)(1-\alpha_L)$ and $W_{W^N} = \left(W/W^N\right)\alpha_L$.

Inserting solutions for aggregate labor supply (621), plugging the solutions for aggregate wage index (623) and for consumption (575) into the accumulation equation of financial wealth (620), linearizing around the steady-state leads to:

$$\dot{A}(t) = r^\star dA(t) + \Lambda_K dK(t) + \Lambda_Q dQ(t) + \Lambda_G dG(t) + \Lambda_\tau d\tau(t), \tag{625}$$

where partial derivatives evaluated at the steady-state are given by

$$\begin{aligned} \Lambda_P &= \left(W_P \tilde{L} + \tilde{W} L_P\right) - \left(\tilde{C}^N + P_C C_P\right), &(626a)\\ \Lambda_K\Big|_{\text{P fixed}} &= W_K \tilde{L} + \tilde{W} L_K, &(626b)\\ \Lambda_G\Big|_{\text{P fixed}} &= -1, &(626c)\\ \Lambda_\tau\Big|_{\text{P fixed}} &= W_\tau \tilde{L} + \tilde{W} L_\tau. &(626d)\end{aligned}$$

Substituting the solutions for $K(t)$ and $Q(t)$ into (625) leads to:

$$\dot{A}(t) = r^\star dA(t) + M_1 X_1(t) + M_2 X_2(t) + \Lambda_G dG(t) + \Lambda_\tau d\tau(t), \tag{627}$$

where $M_i = \Lambda_K + \Lambda_Q \omega_2^i$ (with $i = 1, 2$).

Substituting the equation that governs the endogenous response of government consumption to an exogenous fiscal shock (495) along with the equation that governs the endogenous response of the labor tax rate (597) into (627) and solving yields the general solution for the stock of national non human wealth:

$$
\begin{aligned}
A(t)-\tilde{A} &= \left\{\left(A_0-\tilde{A}\right)-\frac{\omega_A^1}{\nu_1-r^\star}+\frac{\Lambda_G\tilde{Y}}{\xi+r^\star}\left(1-\Theta^{G,\prime}\right)+\frac{\Lambda_\tau\Omega_D}{\delta+r^\star}-\frac{\Lambda_\tau\Omega_1}{\xi+r^\star}\left(1-\Theta^{\tau,\prime}\right)\right.\\
&+ \frac{M_1\Gamma_1^G}{\xi+r^\star}\left(1-\Theta_1^{G,\prime}\right)+\frac{M_1\Gamma_1^D}{\delta+r^\star}-\frac{M_1\Gamma_1^\tau}{\xi+r^\star}\left(1-\Theta_1^{\tau,\prime}\right)\\
&- \left.\frac{M_2\Gamma_2^G}{\xi+r^\star}\left(1-\Theta_2^{G,\prime}\right)-\frac{M_2\Gamma_2^D}{\delta+r^\star}+\frac{M_2\Gamma_2^\tau}{\xi+r^\star}\left(1-\Theta_2^{\tau,\prime}\right)\right\}e^{r^\star t}\\
&+ \frac{\omega_A^1}{\nu_1-r^\star}e^{\nu_1 t}-\frac{\Lambda_G\tilde{Y}}{\xi+r^\star}\left(e^{-\xi t}-\Theta^{G,\prime}e^{-\chi t}\right)-\frac{\Lambda_\tau\Omega_D}{\delta+r^\star}e^{-\delta t}+\frac{\Lambda_\tau\Omega_1}{\xi+r^\star}\left(e^{-\xi t}-\Theta^{\tau,\prime}e^{-\chi t}\right)\\
&- \frac{M_1\Gamma_1^G}{\xi+r^\star}\left(e^{-\xi t}-\Theta_1^{G,\prime}e^{-\chi t}\right)-\frac{M_1\Gamma_1^D}{\delta+r^\star}+\frac{M_1\Gamma_1^\tau}{\xi+r^\star}\left(e^{-\xi t}-\Theta_1^{\tau,\prime}e^{-\chi t}\right)\\
&+ \frac{M_2\Gamma_2^G}{\xi+r^\star}\left(1-\Theta_2^{G,\prime}\right)+\frac{M_2\Gamma_2^D}{\delta+r^\star}-\frac{M_2\Gamma_2^\tau}{\xi+r^\star}\left(1-\Theta_2^{\tau,\prime}\right), \qquad (628)
\end{aligned}
$$

where we set:

$$
\omega_A^1 = M_1\left[\left(K_0-\tilde{K}\right)-X_2(0)-\Gamma_1^G\left(1-\Theta_1^G\right)-\Gamma_1^D+\Gamma_1^\tau\left(1-\Theta_1^\tau\right)\right]. \qquad (629)
$$

Invoking the transversality condition, one obtains the 'stable' solution for the stock of national non human wealth so that $A(t)$ converges toward its steady-state value $\tilde{A}$:

$$
\begin{aligned}
A(t)-\tilde{A} &= \frac{\omega_A^1}{\nu_1-r^\star}e^{\nu_1 t}-\frac{\Lambda_G\tilde{Y}}{\xi+r^\star}\left(e^{-\xi t}-\Theta^{G,\prime}e^{-\chi t}\right)-\frac{\Lambda_\tau\Omega_D}{\delta+r^\star}e^{-\delta t}+\frac{\Lambda_\tau\Omega_1}{\xi+r^\star}\left(e^{-\xi t}-\Theta^{\tau,\prime}e^{-\chi t}\right)\\
&- \frac{M_1\Gamma_1^G}{\xi+r^\star}\left(e^{-\xi t}-\Theta_1^{G,\prime}e^{-\chi t}\right)-\frac{M_1\Gamma_1^D}{\delta+r^\star}e^{-\delta t}+\frac{M_1\Gamma_1^\tau}{\xi+r^\star}\left(e^{-\xi t}-\Theta_1^{\tau,\prime}e^{-\chi t}\right)\\
&+ \frac{M_2\Gamma_2^G}{\xi+r^\star}\left(e^{-\xi t}-\Theta_2^{G,\prime}e^{-\chi t}\right)+\frac{M_2\Gamma_2^D}{\delta+r^\star}e^{-\delta t}-\frac{M_2\Gamma_2^\tau}{\xi+r^\star}\left(e^{-\xi t}-\Theta_2^{\tau,\prime}e^{-\chi t}\right). \qquad (630)
\end{aligned}
$$

Eq. (630) gives the trajectory for for $N(t)$ consistent with the intertemporal solvency condition:

$$
\left(\tilde{A}-A_0\right) = -\frac{\omega_A^1}{\nu_1-r^\star}+\frac{\omega_A^G}{\xi+r^\star}+\frac{\omega_A^D}{\delta+r^\star}+\frac{\omega_A^\tau}{\xi+r^\star}, \qquad (631)
$$

where ω_A^1 is given by (629) and we set

$$
\omega_A^G = \Lambda_G\tilde{Y}\left(1-\Theta^{G,\prime}\right)+M_1\Gamma_1^G\left(1-\Theta_1^{G,\prime}\right)-M_2\Gamma_2^G\left(1-\Theta_2^{G,\prime}\right), \qquad (632a)
$$

$$
\omega_A^D = \Lambda_\tau\Omega_D-M_1\Gamma_1^D+M_2\Gamma_2^D, \qquad (632b)
$$

$$
\omega_A^\tau = -\Lambda_\tau\Omega_1\left(1-\Theta^{\tau,\prime}\right)-M_1\Gamma_1^\tau\left(1-\Theta_1^{\tau,\prime}\right)+M_2\Gamma_2^\tau\left(1-\Theta_2^{\tau,\prime}\right). \qquad (632c)
$$

Differentiating (630) w.r.t. time gives the trajectory for the national non human wealth along the transitional path when government spending follows the temporal path given by eq. (495) and the labor tax rate is governed by the dynamic equation (597)

$$
\begin{aligned}
\dot{A}(t) &= \nu_1\frac{\omega_A^1}{\nu_1-r^\star}e^{\nu_1 t}+\frac{\Lambda_G\tilde{Y}}{\xi+r^\star}\left(\xi e^{-\xi t}-\chi\Theta^{G,\prime}e^{-\chi t}\right)+\delta\frac{\Lambda_\tau\Omega_D}{\delta+r^\star}e^{-\delta t}-\frac{\Lambda_\tau\Omega_1}{\xi+r^\star}\left(\xi e^{-\xi t}-\chi\Theta^{\tau,\prime}e^{-\chi t}\right)\\
&+ \frac{M_1\Gamma_1^G}{\xi+r^\star}\left(\xi e^{-\xi t}-\chi\Theta_1^{G,\prime}e^{-\chi t}\right)+\delta\frac{M_1\Gamma_1^D}{\delta+r^\star}e^{-\delta t}-\frac{M_1\Gamma_1^\tau}{\xi+r^\star}\left(\xi e^{-\xi t}-\chi\Theta_1^{\tau,\prime}e^{-\chi t}\right)\\
&- \frac{M_2\Gamma_2^G}{\xi+r^\star}\left(\xi e^{-\xi t}-\chi\Theta_2^{G,\prime}e^{-\chi t}\right)+\frac{M_2\Gamma_2^D}{\delta+r^\star}e^{-\delta t}+\frac{M_2\Gamma_2^\tau}{\xi+r^\star}\left(\xi e^{-\xi t}-\chi\Theta_2^{\tau,\prime}e^{-\chi t}\right). \qquad (633)
\end{aligned}
$$

K Solving the Model with Endogenous Markups

This section extends the two-sector model with imperfect mobility of labor to an imperfectly competitive non traded sector with endogenous markups. We maintain the assumption capital installation costs. There are two sectors. A traded sector produced a good that can be consumed by the private, C^T, and the public sector, G^T, invested, J^T, or exported. A non traded sector produces a good for domestic absorption only. The non traded good can be consumed by the private, C^N, and the public sector, G^N, or invested, J^N. The final non-traded output, Y^N, is produced in a competitive retail sector with constant-returns-to-scale production which aggregates a continuum measure one of sectoral non-traded goods. We denote the elasticity of substitution between any two different sectoral non traded goods by $\eta > 0$. In each industry, there are $N > 1$ firms producing differentiated goods that are aggregated into a sectoral non-traded good. The elasticity of substitution between any two varieties within an industry is denoted by $\rho > 0$, and we assume that this is higher than the elasticity of substitution across non traded industries, i.e. $\rho > \eta$ (see Jaimovich and Floetotto [2008]). The number of firms is large enough so that we can ignore the strategic effects but not so large that the effect of entry on the firm's demand curve is minuscule. Consequently, the price elasticity of demand faced by a single firm is no longer constant and equal to the elasticity of substitution between any two varieties, but rather a function of the number of firms N. We further assume instantaneous entry, which implies that the producers make zero profits. Since the household's maximization problem is identical to that described in section 2, we restrict our attention to the firms' maximization problem. More technical details can be found in the working paper version of the paper by Cardi and Restout [2004], [2015].

K.1 Introducing Endogenous Markups

Within each industry, there is monopolistic competition; each firm that produces one variety is a price setter. Output $\mathcal{X}_{i,j}$ of firm i in industry j is produced using capital and labor, i.e. $\mathcal{X}_{i,j} = H\left(\mathcal{K}_{i,j}, \mathcal{L}_{i,j}\right)$. Each firm chooses capital and labor by equalizing markup-adjusted marginal products to the marginal cost of inputs, i. e. $PH_K/\mu = R$, and $PH_L/\mu = W^N$, where μ is the markup over the marginal costs. At a symmetric equilibrium, non-traded output is equal to $Y^N = N\mathcal{X} = H\left(K^N, L^N\right)$ where $L_N = N\mathcal{L}_N$ and $K_N = N\mathcal{K}_N$.

Taking into account the fact that output of one variety does not affect the price of final non-traded output, but influences the sectoral price level, in a symmetric equilibrium, the resulting price elasticity of demand is:

$$e\left(N\right) = \rho - \frac{\left(\rho - \eta\right)}{N}, \quad N \in \left(1, \infty\right). \tag{634}$$

Assuming that $\rho > \eta$, the price elasticity of demand faced by one single firm is an increasing function of the number of firms N within a sector:

$$\frac{\partial e}{\partial N} = \frac{\rho - \eta}{N^2} > 0, \tag{635}$$

where the positive sign of the partial derivative follows from the assumption $\rho > \eta$. Henceforth, the markup defined as follows

$$\mu\left(N\right) = \frac{e}{e-1} \tag{636}$$

decreases as the number of competitors increases, i.e. $\mu_N < 0$.

We assume instantaneous entry, which implies that the zero-profit condition holds at each instant of time:

$$\begin{aligned} \pi^N &= H\left(\mathcal{K}^N, \mathcal{L}^N\right) - R\mathcal{K}^N - W^N\mathcal{L}^N - P\psi, \\ &= P\left[\frac{Y^N}{N}\left(1 - \frac{1}{\mu}\right) - \psi\right] = 0, \end{aligned} \tag{637}$$

where we denote fixed costs by ψ; we used the fact that $\frac{P}{\mu}\frac{\partial \mathcal{X}}{\partial \mathcal{K}^N} = R$ and $\frac{P}{\mu}\frac{\partial \mathcal{X}}{\partial \mathcal{L}^N} = W^N$ and $\frac{\partial \mathcal{X}}{\partial \mathcal{K}^N}\mathcal{K}^N + \frac{\partial \mathcal{X}}{\partial \mathcal{L}^N}\mathcal{L}^N = \mathcal{X}$. The zero-profit condition $\pi^N = 0$ can be solved for the number of firms.

Since capital can move freely between the two sectors while the shift of labor across sectors is costly, only marginal products of capital in the traded and the non traded sector equalize:

$$Z^T\left(1-\theta^T\right)\left(k^T\right)^{-\theta^T} = \frac{P}{\mu}Z^N\left(1-\theta^N\right)\left(k^N\right)^{-\theta^N} \equiv R, \tag{638a}$$

$$Z^T\theta^T\left(k^T\right)^{1-\theta^T} \equiv W^T, \tag{638b}$$

$$\frac{P}{\mu}Z^N\theta^N\left(k^N\right)^{1-\theta^N} \equiv W^N, \tag{638c}$$

where the capital-labor ratio for sector $j = T, N$ is denoted by $k^j \equiv K^j/L^j$. These static efficiency conditions state that the value of the marginal product of labor in sector j is equal to the labor cost W^j while the value of the marginal product of capital in the traded and the non traded sector must be equal to the capital rental cost, R.

Aggregating over the two sectors gives us the resource constraint for capital:

$$K^T + K^N = K. \tag{639}$$

K.2 Solving the Model with Endogenous Markups

Plugging the short-run static solutions for L^T and L^N given by (427) into the resource constraint for capital (639), the system of four equations consisting of (638a)-(638c) together with (639) can be solved for the sectoral wage rates W^j and sectoral capital-labor ratios k^j. Keeping TFPs unchanged, and differentiating (638a)-(638c) together with (639) yields in matrix form:

$$\begin{pmatrix} -\frac{\theta^T}{k^T} & \frac{\theta^N}{k^N} & 0 & 0 \\ \frac{\left(1-\theta^T\right)}{k^T} & 0 & -\frac{1}{W^T} & 0 \\ 0 & \frac{\left(1-\theta^N\right)}{k^N} & 0 & -\frac{1}{W^N} \\ L^T & L^N & \Psi_{W^T} & \Psi_{W^N} \end{pmatrix} \begin{pmatrix} dk^T \\ dk^N \\ dW^T \\ dW^N \end{pmatrix}$$
$$= \begin{pmatrix} \frac{dP}{P} - \frac{d\mu}{\mu} \\ 0 \\ -\frac{dP}{P} + \frac{d\mu}{\mu} \\ dK - \Psi_{\bar{\lambda}}d\bar{\lambda} \end{pmatrix}, \tag{640}$$

where we set:

$$\Psi_{W^T} = k^T L^T_{W^T} + k^N L^N_{W^T}, \tag{641a}$$
$$\Psi_{W^N} = k^T L^T_{W^N} + k^N L^N_{W^N}, \tag{641b}$$
$$\Psi_{\bar{\lambda}} = k^T L^T_{\bar{\lambda}} + k^N L^N_{\bar{\lambda}}. \tag{641c}$$

The short-run static for sectoral wages and sectoral capital-labor ratios are:

$$W^j = W^j\left(\bar{\lambda}, K, P, \mu\right), \quad k^j = k^j\left(\bar{\lambda}, K, P, \mu\right). \tag{642}$$

Inserting first solutions for sectoral wages (642) into (427), sectoral hours worked can be solved as functions of the shadow value of wealth, the capital stock, the relative price of non tradables and the markup

$$L^j = L^j\left(\bar{\lambda}, K, P, \mu\right). \tag{643}$$

Production functions (16) can be rewritten as follows:

$$Y^j = Z^j L^j \left(k^j\right)^{1-\theta^j}, \quad j = T, N. \tag{644}$$

Inserting first short-run static solutions for sectoral capital-labor ratios (642) and sectoral labor (643) into the production functions yields:

$$Y^j = Y^j\left(\bar{\lambda}, K, P, \mu\right). \tag{645}$$

It is worth noticing that a rise in the markup μ produces opposite effects to those induced by an appreciation in P.

The Return on Domestic Capital, R

The return on domestic capital is:

$$R = Z^T \left(1 - \theta^T\right) \left(k^T\right)^{-\theta^T}. \quad (646)$$

Inserting first the short-run static solution for the capital-labor ratio k^T given by (642), eq. (646) can be solved for the return on domestic capital:

$$R = R\left(\bar{\lambda}, K, P, \mu\right). \quad (647)$$

Optimal Investment Decision, I/K

Eq. (405c) can be solved for the investment rate:

$$\frac{I}{K} = v\left(\frac{Q}{P_I(P)}\right) + \delta_K, \quad (648)$$

where

$$v\left(.\right) = \frac{1}{\kappa}\left(\frac{Q}{P_J} - 1\right), \quad (649)$$

The Number of Firms within each Non Traded Industry, N

Substituting the short-run solution for non traded output (144a) and using the fact that $\mu = \mu\left(N\right)$ (see (634)-(636)), the zero-profit condition (637) can be rewritten as:

$$Y^N\left(\bar{\lambda}, K, P, \mu\left(N\right)\right)\left(1 - \frac{1}{\mu\left(N\right)}\right) = N\psi. \quad (650)$$

Solving yields the short-run solution for the number of firms:

$$N = N\left(\bar{\lambda}, K, P\right), \quad (651)$$

where partial derivatives are given by:

$$N_x \equiv \frac{\partial N}{\partial x} = -\frac{Y_x^N\left(1 - \frac{1}{\mu}\right)}{\chi} \gtrless 0, \quad (652)$$

where $x = K, P, \bar{\lambda}$ and we set

$$\chi = \frac{\mu_N}{\mu}\left\{\left[Y_\mu^N\left(\mu - 1\right) + \frac{Y^N}{\mu}\right] - \psi\right\}. \quad (653)$$

Inspection of (653) shows that $\chi < 0$ since $\mu_N = \frac{\partial \mu}{\partial N} < 0$ if $Y_\mu^N = \frac{\partial Y^N}{\partial \mu} < 0$ is not too large. This implies that an input inflow in the non-traded sector that raises Y^N and thereby leads to profit opportunities results in firm entry (i.e, N increases) which lowers the markup, μ.

Solutions for Sectoral Production Variables

Since sectoral wages, sectoral capital labor-ratios, sectoral labor and sectoral output depend on the markup and thus on the number of firms, we have to plug back (651) into (642), (643), and (645) in order get the solutions for sectoral wages, sectoral capital labor-ratios, sectoral labor and sectoral output:

$$W^j = W^j\left\{\bar{\lambda}, K, P, \mu\left[N(.)\right]\right\} \equiv W^j\left(\bar{\lambda}, K, P\right), \quad (654a)$$

$$k^j = k^j\left\{\bar{\lambda}, K, P, \mu\left[N(.)\right]\right\} \equiv W^j\left(\bar{\lambda}, K, P\right), \quad (654b)$$

$$L^j = L^j\left\{\bar{\lambda}, K, P, \mu\left[N(.)\right]\right\} \equiv W^j\left(\bar{\lambda}, K, P\right), \quad (654c)$$

$$Y^j = Y^j\left\{\bar{\lambda}, K, P, \mu\left[N(.)\right]\right\} \equiv W^j\left(\bar{\lambda}, K, P\right), \quad (654d)$$

where $Y_X^j = \frac{\partial Y^j}{\partial X} + \frac{\partial Y^j}{\partial \mu}\mu_N N_X$ with $X = \bar{\lambda}, K, P$. The same logic applies to W^j, k^j, L^j.

Sectoral Government Spending, G^j

Making use of (H.1), the budget constraint can be solved for government expenditure in good $j = T, N$ can be solved for overall government consumption as follows:

$$G^N(t) = \mathsf{G}^N\left(G(t)\right), \quad G^T = \mathsf{G}^T\left(G(t)\right), \tag{655}$$

where $\frac{\partial G^N}{\partial G} = \frac{\omega_{GN}}{P}$ and $\frac{\partial G^T}{\partial G} = \omega_{GT}$ with ω_{Gj} corresponding to the share of expenditure on good j in total government spending.

The Relative Price of Non Tradables, P

Finally, we have to solve for the relative price of non tradables by using the non traded goods market clearing condition:

$$Y^N = C^N + G^N + J^N. \tag{656}$$

Remembering that the non traded input J^N used to produce investment goods is equal to $P_J' J$, inserting short-run static solutions for C^N and Y^N given by (425) and (654d), respectively, substituting (446), i.e., $J = K\left[v(.) + \delta_K + \frac{\kappa}{2}\left(v(.)\right)^2\right]$, and inserting the solution for the number of firms described by (651) into the markup, i.e., $\mu = \mu\left[N\left(\bar{\lambda}, K, P\right)\right]$, the non traded goods market clearing condition (656) can be rewritten as follows:

$$\frac{Y^N\left[\bar{\lambda}, K, P, \mu\left(N(.)\right)\right]}{\mu\left(N(.)\right)} = C^N\left(\bar{\lambda}, P\right) + G^N + P_J' K\left[v(.) + \delta_K + \frac{\kappa}{2}\left(v(.)\right)^2\right]. \tag{657}$$

Using eq. (655), eq. (657) can be solved for the relative price of non tradables:

$$P = P\left(\bar{\lambda}, K, Q, G\right), \tag{658}$$

with partial derivatives given by:

$$P_K = \frac{\partial P}{\partial K} = \frac{\left(-\frac{Y_K^N}{\mu} + \frac{Y^N}{\mu}\frac{\mu_N}{\mu}N_K\right)\frac{1}{P_J'} + \frac{J}{K}}{\Psi^{P,\prime}} \lesseqgtr 0, \tag{659a}$$

$$P_Q = \frac{\partial P}{\partial Q} = \frac{K v_Q\left[1 + \kappa v(.)\right]}{\Psi^{P,\prime}} > 0, \tag{659b}$$

$$P_G = \frac{\omega_{GN}}{P P_J' \Psi^{P,\prime}} > 0, \tag{659c}$$

where we set

$$\Psi^{P,\prime} = \left[\left(\frac{Y_P^N}{\mu} - C_P^N\right) + \frac{J^N \phi_J\left(1 - \alpha_J\right)}{P} - \frac{Y^N}{\mu}\frac{\mu_N}{\mu}N_P\right]\frac{1}{P_J'} - K v_P\left[1 + \kappa v(.)\right] > 0. \tag{660}$$

with $\mu_N < 0$ and $N_P > 0$.

K.3 Equilibrium Dynamics

Remembering that the non traded input J^N used to produce the capital good is equal to $P_J' J$, using the fact that $J^N = Y^N - C^N - G^N$ and inserting $I = \dot{K} + \delta_K K$, the capital accumulation equation can be rewritten as follows:

$$\dot{K} = \frac{\frac{Y^N}{\mu} - C^N - G^N}{P_J'} - \delta_K K - \frac{\kappa}{2}\left(\frac{I}{K} - \delta_K\right)^2 K. \tag{661}$$

Inserting short-run solutions for non traded output (654d), consumption in non tradables (425), optimal investment decision (649), and the number of firms (651) into the physical capital accumulation equation (661), and inserting the solution for the return on domestic capital (647) into the dynamic equation for the shadow value of capital stock (405e), the dynamic system reads as follows:

$$\dot{K} \equiv \Upsilon\left(K, P, Q, G\right) = \frac{\frac{Y^N\left[K, P(.), \bar{\lambda}\right]}{\mu\left[N(.)\right]} - C^N\left(\bar{\lambda}, P(.)\right) - \mathsf{G}^N\left(G\right)}{P_J'\left(P(.)\right)} - \delta_K K - \frac{K}{2\kappa}\left[\frac{Q}{P_J\left(P(.)\right)} - 1\right]^2, \tag{662a}$$

$$\dot{Q} \equiv \Sigma\left(K, P, Q, G\right) = \left(r^\star + \delta_K\right) Q - \left[R\left(K, P(.)\right) + P_J \frac{\kappa}{2} v(.)\left(v(.) + 2\delta_K\right)\right]. \tag{662b}$$

where we have inserted the solution for the number of firms (651) into (647) in order to solve for the domestic return of physical capital, i.e., $R = R\left\{\bar{\lambda}, K, P, \mu\left[N(.)\right]\right\} \equiv R\left(\bar{\lambda}, K, P\right)$.

As will be useful, let us denote by Υ_K, Υ_Q, and Υ_P the partial derivatives evaluated at the steady-state of the capital accumulation equation w.r.t. K and Q (for given P), respectively, and P:

$$\Upsilon_K\Big|_{\text{P fixed}} \equiv \frac{\partial \dot{K}}{\partial K}\Big|_{\text{P fixed}} = \left(\frac{Y_K^N}{\mu} - \frac{Y^N}{\mu}\frac{\mu_N}{\mu}N_K\right)\frac{1}{P'_J} - \delta_K > 0, \tag{663a}$$

$$\Upsilon_P \equiv \frac{\partial \dot{K}}{\partial P} = \left[\left(\frac{Y_P^N}{\mu} - \frac{Y^N}{\mu}\frac{\mu_N}{\mu}N_P - C_P^N\right) + \frac{\tilde{I}^N \phi_J\left(1-\alpha_J\right)}{\tilde{P}}\right]\frac{1}{P'_J} > 0, \tag{663b}$$

$$\Upsilon_Q\Big|_{\text{P fixed}} \equiv \frac{\partial \dot{K}}{\partial Q}\Big|_{\text{P fixed}} = 0, \tag{663c}$$

where we used the fact that in the long-run, $\tilde{J}^N = \tilde{I}^N$ and $\tilde{Q} = P_J\left(\tilde{P}\right)$. Partial derivatives evaluated at the steady-state for the marginal value of an additional unit of capital w.r.t. K and Q (for given P), respectively, and P which we denoted by Σ_K, Σ_Q, and Σ_P are identical to (455).

Remembering that $J^T = \left(1-\alpha_J\right)P_J J$, the current account equation is given by:

$$\begin{aligned}
\dot{B} \equiv \Xi\left(B, K, Q, G\right) &= r^\star B + Y^T - C^T - G^T - \left(1-\alpha_J\right)P_J J, \\
&= r^\star B + Y^T - C^T - G^T - \left(\frac{1-\alpha_J}{\alpha_J}\right)P\left(\frac{Y^N}{\mu} - C^N - G^N\right),
\end{aligned} \tag{664}$$

where we used the fact that $P'_J J = Y^N - C^N - G^N$. As will be useful, let us denote by Ξ_K and Ξ_P the partial derivatives of the accumulation equation for traded bonds w.r.t. K (for given P) and P:

$$\Xi_K\big|_{\text{P fixed}} \equiv \frac{\partial \dot{B}}{\partial K}\Big|_{\text{P fixed}} = Y_K^T - \left(\frac{1-\alpha_J}{\alpha_J}\right)\tilde{P}\left(\frac{Y_K^N}{\mu} - \frac{Y^N}{\mu}\frac{\mu_N}{\mu}N_K\right) \geq 0, \tag{665a}$$

$$\begin{aligned}
\Xi_P \equiv \frac{\partial \dot{B}}{\partial P} &= \left(Y_P^T - C_P^T\right) - \left(\frac{1-\alpha_J}{\alpha_J}\right)\tilde{P}\left(\frac{Y_P^N}{\mu} - \frac{Y^N}{\mu}\frac{\mu_N}{\mu}N_P - C_P^N\right) \\
&\quad -\phi_J\left(\frac{1-\alpha_J}{\alpha_J}\right)\tilde{I}^N < 0,
\end{aligned} \tag{665b}$$

where we used the fact that $\frac{\partial\left(\frac{1-\alpha_J}{\alpha_J}\right)}{\partial P} = -\frac{1}{P}\left[\left(\frac{1-\alpha_J}{\alpha_J}\right) - \phi_J\left(\frac{1-\alpha_J}{\alpha_J}\right)\right]$ and at the steady-state, we have $\tilde{J}^N = \tilde{I}^N$ since capital installation costs are absent in the long run. The steps for the derivation of solutions for a temporary government shock are identical to those detailed in section H.

L Calibration Procedure

In this section, we provide more details about the calibration to a representative OECD economy and to data from 16 OECD countries. Section A presents the source and construction of data.

L.1 Initial Steady-State

Normalizing total factor productivity (TFP henceforth) for the non traded sector Z^N to 1, the calibration reduces to 19 parameters: $r^\star$, β, σ_C, σ_L, ϵ, ϑ, ϕ, φ, ϕ_J, φ_J, κ, δ_K, θ^T, θ^N, Z^T, ω_G $(= \frac{G}{Y})$, ω_{G^N} $(= \frac{PG^N}{G})$, ξ, χ, and initial conditions B_0, K_0.

Since we focus on the long-run equilibrium, the tilde is suppressed for the purposes of clarity. The steady-state of the open economy comprises 18 equations:

$$C = \left(P_C \bar{\lambda}\right)^{-\sigma_C}, \tag{666a}$$

$$L = \left(W \bar{\lambda}\right)^{\sigma_L}, \tag{666b}$$

$$C^N = (1-\varphi)\left(\frac{P}{P_C}\right)^{-\phi} C, \tag{666c}$$

$$C^T = (1-\varphi)\left(\frac{1}{P_C}\right)^{-\phi} C, \tag{666d}$$

$$L^N = (1-\vartheta)\left(\frac{W^N}{W}\right)^{\epsilon} L, \tag{666e}$$

$$L^T = \vartheta\left(\frac{W^T}{W}\right)^{\epsilon} L \tag{666f}$$

$$I^N = (1-\varphi_J)\left(\frac{P}{P_J}\right)^{-\phi_J} I, \tag{666g}$$

$$I^T = (1-\varphi_J)\left(\frac{1}{P_J}\right)^{-\phi_J} I, \tag{666h}$$

$$I = \delta_K K, \tag{666i}$$

$$\frac{G}{Y} = \omega_G, \tag{666j}$$

$$Z^T\left(1-\theta^T\right) = P_J\left(r^\star + \delta_K\right), \tag{666k}$$

$$Z^T\left(1-\theta^T\right)\left(k^T\right)^{-\theta^T} = PZ^N\left(1-\theta^N\right)\left(k^N\right)^{-\theta^N}, \tag{666l}$$

$$Z^T\theta^T\left(k^T\right)^{1-\theta^T} = W^T, \tag{666m}$$

$$PZ^N\theta^N\left(k^N\right)^{1-\theta^N} = W^N, \tag{666n}$$

$$k^T L^T + k^N L^N = K, \tag{666o}$$

$$Z^N L^N\left(k^N\right)^{1-\theta^N} = C^N + G^N + I^N, \tag{666p}$$

$$r^\star B + Z^T L^T\left(k^T\right)^{1-\theta^T} - C^T - G^T = 0, \tag{666q}$$

and the intertemporal solvency condition

$$B - B_0 = \Psi_1\left(K - K_0\right), \tag{666r}$$

where we used the fact that at the steady-state $I^j = J^j$ (with $j = T, N$), and we also have

$$G^N = \left(\omega_{G^N}/P\right) G, \tag{667a}$$

$$G^T = \left(1-\omega_{G^N}\right) G, \tag{667b}$$

$$P_C = \left[\varphi + (1-\varphi)(P)^{1-\phi}\right]^{\frac{1}{1-\phi}}, \tag{667c}$$

$$P_J = \left[\varphi_J + (1-\varphi_J) P^{1-\phi_J}\right]^{\frac{1}{1-\phi_J}}, \tag{667d}$$

$$W = \left[\vartheta\left(W^T\right)^{\epsilon+1} + (1-\vartheta)\left(W^N\right)^{\epsilon+1}\right]^{\frac{1}{\epsilon+1}}, \tag{667e}$$

$$Y = Y^T + PY^N = Z^T L^T\left(k^T\right)^{1-\theta^T} + PZ^N L^N\left(k^N\right)^{1-\theta^N}. \tag{667f}$$

Using (667), the system (666) jointly determines the following 18 variables C, L, C^N, C^T, L^N, L^T, I^N, I^T, I, G, k^T, k^N, W^T, W^N, K, P, B, $\bar{\lambda}$.

Some of the values of parameters can be taken directly from data, but others need to be endogenously calibrated to fit a set of an average OECD economy features. Among the 19 parameters, 4 parameters, i.e., φ, φ_J, ϑ, δ_K together with initial conditions (B_0, K_0) must be set in order to match key properties of a typical OECD economy. More precisely, the parameters φ, φ_J, ϑ, δ_K together with the set of initial conditions are set to target α_C, α_J, α_L, υ_{NX}, I/Y. We denote by $\upsilon_{G^j} = G^j/Y^j$ and $\upsilon_{J^j} = J^j/Y^j$ the ratio of government spending and investment expenditure on good j to output in sector j, respectively, and

$\upsilon_B = \frac{r^\star B}{Y^T}$ the ratio of interest receipts from traded bonds holding to traded output. The steady-state can be reduced to the following four equations:

$$\frac{Y^T}{Y^N}\frac{(1+\upsilon_B-\upsilon_{J^T}-\upsilon_{G^T})}{(1-\upsilon_{J^N}-\upsilon_{G^N})} = \frac{\varphi}{1-\varphi}P^{\phi}, \tag{668a}$$

$$\frac{Y^T}{Y^N} = P^{-\left\{\epsilon+(1+\epsilon)\left[\left(\frac{1-\theta_N}{\theta_N}\right)-(1-\varphi_I)\left(\frac{\theta_T-\theta_N}{\theta_T\theta_N}\right)\right]\right\}}\Pi, \tag{668b}$$

$$\left(1-\theta^T\right)\frac{Y^T}{Y}+\left(1-\theta^N\right)\frac{PY^N}{Y} = P^{(1-\varphi_I)}\left(r^\star+\delta_K\right)\frac{K}{Y}, \tag{668c}$$

$$\upsilon_B = \upsilon_{B_0}+r^\star\frac{Y}{Y^T}\Psi_1\left(\frac{K}{Y}-\upsilon_{K_0}\right), \tag{668d}$$

where $\upsilon_{K_0} = \frac{K_0}{Y}$ and Π is a term composed of parameters described by:

$$\begin{aligned}\Pi \quad \equiv \quad & \frac{\left(Z^T\right)^{\frac{1+\epsilon}{\theta^T}}}{\left(Z^N\right)^{\frac{1+\epsilon}{\theta^N}}}\frac{\vartheta}{1-\vartheta}\left(r^\star+\delta_K\right)^{\left(\frac{\theta^T-\theta^N}{\theta^T\theta^N}\right)(1+\epsilon)} \\ \times \quad & \frac{\left[\left(\theta^T\right)^{\epsilon\theta^T}\left(1-\theta^T\right)^{\left(1-\theta^T\right)(1+\epsilon)}\right]^{1/\theta^T}}{\left[\left(\theta^N\right)^{\epsilon\theta^N}\left(1-\theta^N\right)^{\left(1-\theta^N\right)(1+\epsilon)}\right]^{1/\theta^N}}.\end{aligned} \tag{669}$$

The system (668) consisting of four equations determine P, Y^T/Y^N, K/Y and υ_B. The four equations (668a)-(668d) described the goods market equilibrium, the labor market equilibrium, the resource constraint for capital, and the intertemporal solvency condition.

Dividing the market clearing condition for the traded good (666q) by the market clearing condition for the non traded good (666p) and equating the resulting expression with the demand of tradables in terms of non tradables obtained by calculating the ratio of (666d) to (666c), i.e., $\frac{C^T}{C^N} = \frac{\varphi}{1-\varphi}P^{\phi}$, leads to **the goods market equilibrium (668a)**. The derivation of the labor market equilibrium requires more steps. As mentioned below, we assume that the aggregator function for inputs of the investment good is Cobb-Douglas since data suggest that $\phi_J = 1$. In this case, the investment price index simplifies, i.e., $P_J = (P)^{1-\varphi_J}$. First, combining (666k) and (666l) leads to:

$$\begin{aligned}\frac{\left(k^N\right)^{1-\theta^N}}{\left(k^T\right)^{1-\theta^T}} \quad &= \quad P^{\frac{1-\theta_N}{\theta_N}}\left[P_I\left(r^\star+\delta_K\right)\right]^{\frac{1-\theta_T}{\theta_T}-\frac{1-\theta_N}{\theta_N}}\frac{\left[Z^N\left(1-\theta_N\right)\right]^{\frac{1-\theta_N}{\theta_N}}}{\left[Z^T\left(1-\theta_T\right)\right]^{\frac{1-\theta_T}{\theta_T}}}, \\ &= \quad P^{\left[\left(\frac{1-\theta_N}{\theta_N}\right)-(1-\varphi_I)\left(\frac{\theta_T-\theta_N}{\theta_T\theta_N}\right)\right]}\frac{\left[Z^N\left(1-\theta_N\right)\right]^{\frac{1-\theta_N}{\theta_N}}}{\left[Z^T\left(1-\theta_T\right)\right]^{\frac{1-\theta_T}{\theta_T}}}.\end{aligned} \tag{670}$$

Dividing (666f) by (666e) leads to the supply of hours worked in the traded sector relative to the non traded sector, i.e., $\frac{L^T}{L^N} = \frac{\vartheta}{1-\vartheta}\Omega^{-\epsilon}$. Dividing (666n) by (666m) leads to the relative wage, i.e., $\Omega = \frac{PZ^N\theta^N\left(k^N\right)^{1-\theta^N}}{Z^T\theta^T\left(k^T\right)^{1-\theta^T}}$. Inserting the latter expression into the former and using the production functions for the traded sector and non traded sectors which imply $L^T = \frac{Y^T}{Z^T\left(k^T\right)^{1-\theta^T}}$ and $L^N = \frac{Y^N}{Z^N\left(k^N\right)^{1-\theta^N}}$, one obtains:

$$\frac{Y^T}{Y^N} = \frac{\vartheta}{1-\vartheta}\left(\frac{Z^T}{Z^N}\right)^{\epsilon+1}P^{-\epsilon}\left(\frac{\theta^T}{\theta^N}\right)^{\epsilon}\left[\frac{\left(k^T\right)^{1-\theta^T}}{\left(k^N\right)^{1-\theta^N}}\right]^{1+\epsilon}.$$

Inserting (670) into the above expression leads to **the labor market equilibrium (668b)** while we set Π to eq. (669) in order to write the equation in compact form. To determine (668c), use the fact that $K^j = k^jL^j$, multiply both sides of (666o) by $\frac{R}{Y}$ where $R = P_J\left(r^\star+\delta_K\right)$ is the capital rental cost; we get:

$$\frac{RK^T}{Y^T}\frac{Y^T}{Y}+\frac{RK^N}{PY^N}\frac{PY^N}{Y} = \frac{RK}{Y}.$$

Using the fact that the capital income share $\frac{RK^j}{P^jY^j}$ in sector j is equal to $\left(1-\theta^j\right)$ and remembering that the investment price index reduces to $P_J = (P)^{1-\varphi_J}$, one obtains **the resource constraint for capital described by eq. (668c)**. Finally, to get (668d), multiply both sides of (666r) by $\frac{r^\star}{Y^T}$, denote the ratio of interest receipts from the initial stock of traded bonds to traded output by $\upsilon_{B_0} = \frac{r^\star B_0}{Y^T}$ and the ratio of the initial capital stock to GDP by $\upsilon_{K_0} = \frac{K_0}{Y}$ leads to **eq. (668d) that describes the intertemporal solvency condition**.

Because the ratios we wish to target are different from the macroeconomic aggregates, i.e., P, Y^T/Y^N, K/Y and υ_B, that are jointly determined by the system of equations (668), we have to relate the latter ratios with the former. First, the relative price of non tradables P determines the non tradable content of consumption expenditure by setting φ:

$$\alpha_C = \frac{(1-\varphi)\, P^{1-\phi}}{\varphi + (1-\varphi)\, P^{1-\phi}}. \tag{671}$$

The ratio K/Y along with the relative price of non tradables, P, determines the investment-to-GDP ratio $P_J I/Y$ by setting δ_K (see eq. (666i)):

$$\frac{P_J I}{Y} = P_J \frac{\delta_K K}{Y}. \tag{672}$$

The ratio of net interest receipts from traded bonds holding to traded output, i.e., υ_B, determines the ratio of net exports to traded output, i.e. $\upsilon_{NX} = \frac{NX}{Y^T}$ with $NX = Y^T - C^T - G^T - J^T$; dividing both sides of the traded goods market clearing condition (666q) leads to:

$$\upsilon_{NX} = -\upsilon_B. \tag{673}$$

Finally, we show that Y^T/Y^N (together with P) determines L^N/L by setting ϑ. To do so, using the definition of the aggregate wage index (415), the ratio of the aggregate wage to the non traded wage can be rewritten as follows:

$$\begin{aligned}\left(\frac{W}{W^N}\right)^{\epsilon+1} &= \frac{\vartheta\left(W^T\right)^{\epsilon+1} + (1-\vartheta)\left(W^N\right)^{\epsilon+1}}{\left(W^N\right)^{\epsilon+1}},\\ &= \vartheta\left(\frac{W^T}{W^N}\right)^{\epsilon+1} + (1-\vartheta),\end{aligned}$$

and by solving, we get

$$\frac{W}{W^N} = \left[\vartheta\left(\frac{W^T}{W^N}\right)^{\epsilon+1} + (1-\vartheta)\right]^{\frac{1}{\epsilon+1}}. \tag{674}$$

Since θ^j is the labor income share in sector j, the ratio of the traded wage to the non traded wage can be written as follows:

$$\frac{W^T}{W^N} = \frac{\theta^T}{\theta^N}\frac{1}{P}\frac{Y^T}{Y^N}\frac{L^N}{L^T}. \tag{675}$$

Dividing (666f) by (666e) leads to a positive relationship between the supply of hours worked to the traded sector relative to the non traded sector and the traded wage relative to the non traded wage, i.e., $\frac{L^T}{L^N} = \frac{\vartheta}{1-\vartheta}\left(\frac{W^T}{W^N}\right)^{\epsilon}$. Substituting the latter equation, eq. (675) can be solved for W^T/W^N, i.e.,

$$\frac{W^T}{W^N} = \left[\frac{1-\vartheta}{\vartheta}\frac{\theta^T}{\theta^N}\frac{1}{P}\frac{Y^T}{Y^N}\right]^{\frac{1}{\epsilon+1}}. \tag{676}$$

Additionally, since $\alpha_L = \frac{W^N L^N}{WL} = (1-\vartheta)\left(\frac{W^N}{W}\right)^{\epsilon+1}$, the share of hours worked in total hours worked is governed by the following optimal rule:

$$\begin{aligned}\frac{L^N}{L} &= (1-\vartheta)\left(\frac{W^N}{W}\right)^{\epsilon},\\ &= (1-\vartheta)\left(\frac{W}{W^N}\right)^{-\epsilon}.\end{aligned} \tag{677}$$

Inserting (676) into (674) and plugging the resulting expression into (677) gives us a relationship between the non tradable content of labor and the ratio Y^T/Y^N (together with P):

$$\begin{aligned} \frac{L^N}{L} &= (1-\vartheta)\left[\vartheta\left(\frac{\theta^T}{\theta^N}\frac{1}{P}\frac{Y^T}{Y^N}\right)+(1-\vartheta)\right]^{-\frac{\epsilon}{\epsilon+1}}, \\ &= (1-\vartheta)^{\frac{1}{\epsilon+1}}\left[\frac{\theta^T}{\theta^N}\frac{1}{P}\frac{Y^T}{Y^N}+1\right]^{-\frac{\epsilon}{\epsilon+1}}. \end{aligned} \tag{678}$$

According to (678), given Y^T/Y^N and P, setting ϑ allows us to target the ratio L^N/L found in the data.

L.2 Calibration to a Representative OECD Economy

To calibrate our model, we estimated a set of parameters so that the initial steady state is consistent with the key empirical properties of a representative OECD economy. This section provides more details about how we calibrate the model to match the key empirical properties of a representative OECD economy. Because we consider an open economy setup with traded and non traded goods, we calculate the non tradable content of GDP, employment, consumption, gross fixed capital formation, government spending, labor compensation and the productivity in tradables in terms of non tradables, for all countries in our sample, as summarized in Table 5. To capture the key properties a typical OECD economy which is chosen as the baseline scenario, we take unweighted average values shown in the last line of Table 5. Columns 12-14 of Table 5 also report government spending and investment as a share of GDP along with the aggregate labor income share.

We first describe the parameters that are taken directly from the data; we start with the preference parameters shown in panel A of Table 27:

- One period in the model is a year.
- The world interest rate, $r^\star$, equal to the subjective time discount rate, β, is set to 4%.
- We assume that utility for consumption is logarithmic and thus set the intertemporal elasticity of substitution for consumption, σ_C, to 1.
- Next, we turn to the Frisch elasticity of labor supply. We set the intertemporal elasticity of substitution for labor supply σ_L to 0.4, in line with the evidence reported by Fiorito and Zanella [2012], but conduct a sensitivity analysis with respect to this parameter.
- The elasticity of labor supply across sectors, ϵ, which captures the degree of labor mobility is set to 0.75 in line with the average of our estimates shown in the last column of Table 5.[74] Our estimates display a wide dispersion across countries and we therefore conduct a sensitivity analysis with respect to this parameter. Excluding estimates of ϵ for Denmark and Norway which are not statistically significant at 10%, estimates of ϵ range from a low of 0.22 for the Netherlands to a high of 1.39 for the United States and 1.64 for Spain. Hence, we allow for ϵ to vary between 0.22 and 1.64 in the sensitivity analysis.
- Building on our panel data estimations (see section A.3), we set the elasticity of substitution (in consumption) between traded and non traded goods to 0.77 in the baseline calibration, in line with the unweighted average value shown in the last line of column 15 of Table 5.[75]

[74] Section A.4 presents the empirical strategy and contains the details of derivation of the relationship we explore empirically.

[75] We derive a testable equation by combining first-order conditions for relative demand and relative supply for tradables in terms of non tradables. Details of derivation of the equation we explore empirically can be found in section A.3. We explore empirically two variants of the testable equation, considering alternatively the ratio of sectoral value added or the ratio of sectoral labor compensation. Estimates of ϕ

- We set the elasticity of substitution, ϕ_J, in investment between traded and non traded inputs to 1, in line with the empirical findings documented by Bems [2008] for OECD countries.

We also consider a more general specification for preferences which are assumed to be non separable in consumption and labor. The functional form is taken from Shimer [2011]:

$$\frac{C^{1-\sigma}V(L)^{\sigma}-1}{1-\sigma}, \quad \text{if} \quad \sigma \neq 1, \quad V(L) \equiv \left(1+(\sigma-1)\frac{\sigma_L}{1+\sigma_L}L^{\frac{1+\sigma_L}{\sigma_L}}\right). \tag{679}$$

Setting $\sigma = 1$, preferences are separable in consumption and labor, as in (399). When investigating the implications of non separability in preferences, we set $\sigma = 2$ while we keep other parameters unchanged.

We pursue with the non-tradable content of consumption, investment and government expenditure, employment, along with sectoral labor income shares and relative productivity of tradables shown in the last line of Table 5 that reports the average of our estimates while panel B of Table 27 displays the value of parameters we choose to calibrate the model:

- The weight of consumption in non tradables $1-\varphi$ is set to 0.51 to target a non-tradable content in total consumption expenditure (i.e. α_C) of 53%.

- In order to target a non tradable content of labor of 67% which corresponds to the 16 OECD countries' unweighted average shown in the last line of Table 5, we set the weight of labor supply to the traded sector in the labor index $L(.)$, $1-\vartheta$, to 0.68.

- We choose a value for the weight of non traded inputs in the investment aggregator function $J(.)$, $1-\varphi_J$, of 0.64 which allows us to obtain a non tradable content of investment expenditure of 64%.

- In accordance with our estimate shown in the last line of Table 5, we choose a non tradable content of government spending, $\omega_G^N = \frac{PG^N}{G}$, of 90%; by construction, we have a share of government consumption on tradables in total government spending, $\omega_{G^T} = 1 - \omega_{G^N}$, of 10%.

- Columns 9 and 10 of Table 5 give the labor income share of the traded and the non traded sector for the sixteen OECD countries in our sample. Labor income shares θ^T and θ^N average respectively to 0.60 and 0.67. Because average values suggest that the non traded sector is relatively more labor intensive than the traded sector, in the baseline calibration, we choose values for θ^T and θ^N so that $\theta^T < \theta^N$. The figures also show substantial dispersion across countries as the labor income share in the traded sector varies from a low of 0.38 in Norway to a high of 0.71 for Italy. Moreover, the labor income share in the traded sector, θ^T, is higher than that in the non traded sector, θ^N, for two countries, namely France and Italy. Thus, we also conduct a sensitivity analysis by considering a situation where the traded sector is more labor intensive than the non traded sector. When excluding France and Italy, the values of θ^T and θ^N average 0.58 and 0.67, respectively. In the baseline calibration, we set θ^T and θ^N to 0.58 and 0.68 which correspond roughly to the average for countries with $k^T > k^N$ and are consistent with an aggregate labor income share of 64%, as shown in column 14 of Table 5. Formally, the aggregate labor income share, denoted by θ, is a value-weighted average of the sectoral labor income shares, i.e., $\theta = \frac{\theta^T Y^T}{Y} + \frac{\theta^N PY^N}{Y}$. When we consider a traded sector that is relatively more labor intensive than the non traded sector, i.e., $k^N > k^T$, we use reverse but symmetric values and thus set $\theta^T = 0.68$ and $\theta^N = 0.58$.

- We assume that traded firms are 28 percent more productive than non traded firms in line with our estimates; we thus normalize Z^N to 1 and set Z^T to 1.28.

for Italy are negative for both variants while for Belgium, only the estimate of the elasticity of substitution in consumption between tradables and non tradables when exploring empirically the second variant of the testable equation is statistically significant (see Table 4). Excluding estimates of ϕ for Italy which are negative and considering a value of 0.795 for Belgium, the elasticity of substitution ϕ averages to 0.77.

We describe below the choice of parameters displayed in panel C of Table 27 characterizing macroeconomic variables such as investment, government spending and the balance of trade of a typical OECD economy:

- As shown in the last line of column 13 of Table 5, government spending as a percentage of GDP averages 20% and thus we set $\omega_G = \frac{G}{Y}$ to 0.2.
- In order to target an investment-to-GDP ratio, $\omega_J = \frac{P_J I}{Y}$, of 21% as shown in the last line of column 12 of Table 5, we set the rate of physical capital depreciation, δ_K, to 6%.
- We choose the value of parameter κ so that the elasticity of I/K with respect to Tobin's q, i.e., Q/P_J, is equal to the value implied by estimates in Eberly, Rebelo, and Vincent [2008]. The resulting value of κ is equal to 17.[76]
- Finally, we choose initial values for B_0 and K_0 for the ratio of net exports to traded output to be nil at the initial steady-state, i.e., $\upsilon_{NX} \simeq 0$.

Investment- and government spending-to-GDP ratios along with balanced trade endogenously determine the consumption-to-GDP ratio. More precisely, since GDP is equal to the sum if its demand components, remembering that at the steady-state $I = J$, we thus have the following accounting identity, $Y = P_C C + P_J I + G + NX$. Dividing both sides by Y and remembering that net exports are nil, i.e., $NX = 0$, the consumption-to-GDP ratio denoted by $\omega_C = \frac{P_C C}{Y}$ is thus equal to 59%:

$$\omega_C = \frac{P_C C}{Y} = 1 - \left(\omega_J + \omega_G + \frac{NX}{Y}\right) = 59\%, \tag{680}$$

where $\omega_J = \frac{P_J I}{Y} = 21\%$, $\omega_G = \frac{G}{Y} = 20\%$, and $NX = 0$.

It is worthwhile mentioning that the non tradable content of GDP is endogenously determined by the non tradable content of consumption, α_C, of investment, α_J, and of government expenditure, ω_{G^N}, along with the consumption-to-GDP ratio, ω_C, the investment-to-GDP ratio, ω_J, and government spending as a share of GDP, ω_G. More precisely, dividing the non traded good market clearing condition (666p) by GDP, Y, leads to an expression that allows us to calculate the non tradable content of GDP:

$$\frac{Y^N}{Y} = \omega_C \alpha_C + \omega_J \alpha_J + \omega_{G^N} \omega_G = 63\%, \tag{681}$$

where $\omega_C = 59\%$, $\alpha_C = 53\%$, $\omega_J = 21\%$, $\alpha_J = 64\%$, $\omega_{G^N} = 90\%$, and $\omega_G = 20\%$. According to (681), the values we target for the non tradable content of consumption, investment and government spending along with the consumption-, investment-, and government spending-to-GDP ratios are consistent with a non tradable content of GDP of 63% found in the data, as reported in the last line of column 1 of Table 5.

In order to capture the dynamic adjustment of government consumption, we assume that the response of government consumption in percent of GDP is governed by the following dynamic equation:[77]

$$\frac{dG(t)}{\tilde{Y}} \equiv \frac{G(t) - \tilde{G}}{\tilde{Y}} = \left[e^{-\xi t} - (1-g)\, e^{-\chi t}\right], \tag{682}$$

where g parametrizes the exogenous fiscal shock while $\xi > 0$ and $\chi > 0$ parametrize the persistence of the response of government consumption along with the pattern of its dynamic adjustment. We present below the parameters related to the endogenous response of government spending to an exogenous fiscal shock which are summarized in panel D of Table 27:

[76] Eberly, Rebelo, and Vincent [2008] run the regression $I/K = \alpha + \beta \,.\, \ln(q)$ and obtain a point estimate for β of 0.06. In our model, the steady-state elasticity of I/K with respect to Tobin's q is $1/\kappa$. Equating $1/\kappa$ to 0.06 gives a value for κ of 17.

[77] More technical details can be found in section H.1.

- We investigate the effects of a rise in government consumption by 1 percentage point of GDP and thus set g to 0.01.

- We choose values of ξ and χ in order to account for the dynamic adjustment of government consumption. Data indicate that the endogenous response of government spending to an exogenous fiscal shock reaches a maximum at time $t = 1$:

$$\frac{dG(1)}{\tilde{Y}} \equiv \frac{G(1) - \tilde{G}}{\tilde{Y}} = g' = \left[e^{-\xi} - (1-g)\, e^{-\chi}\right]. \tag{683}$$

  Differentiating (682) w.r.t. time leads to:

$$\frac{\dot{G}(t)}{\tilde{Y}} = -\left[\xi e^{-\xi t} - \chi\,(1-g)\, e^{-\chi t}\right]. \tag{684}$$

  When government spending reaches its maximum value, we have $\dot{G}(t) = 0$. Setting $t = 1$ into (684) gives:

$$\frac{\dot{G}(1)}{\tilde{Y}} = -\left[\xi e^{-\xi} - \chi\,(1-g)\, e^{-\chi}\right] = 0 \tag{685}$$

  Using the fact that $g = 0.01$ and $g' = 0.01126548$, the system consisting of eq. (683) and eq. (685) jointly determine the values of ξ and χ which allow us to capture the endogenous response of government spending to an exogenous fiscal shock by $g \times 100$ percentage points of GDP; we set $\xi = 0.408675$ and $\chi = 0.415722$.

- While government purchases both non traded goods, G^N, and traded goods, G^T, our VAR evidence suggest that the rise in government consumption is strongly biased toward non traded goods as the relative size the non traded sector rises significantly. When we simulate the model, we thus consider a rise in government consumption by 1 percentage point of GDP which is split between non tradables and tradables in accordance with their respective share in government expenditure at 90% and 10%, respectively. Formally, we have:

$$\frac{dG(t)}{\tilde{Y}} = \omega_{G^N} \frac{dG^N(t)}{\tilde{Y}} + (1-\omega_{G^N}) \frac{dG^T(t)}{\tilde{Y}}, \tag{686}$$

  where $dG(t) = G(t) - \tilde{G}$ and $dG^j(t) = G^j(t) - \tilde{G}^j$.

M More Numerical Results

In this section, we provide more numerical results:

- First, while in the main text, we restrict attention to impact responses to a government spending shock when we conduct the sensitivity analysis for reasons of space, we provide below more numerical results. In particular, in subsection M.1, we report the cumulative responses over a two-year and a four-year horizon. In order to assess to what extent our results depend on the assumption of separability in preferences between consumption and labor, we also consider a more general specification for preferences. Additionally, while in the main text, we assume that capital can move freely across sectors along with workers' costs of switching across sectors, in subsection M.1, we investigate the implications of imperfect mobility of capital across sectors. Since this feature merely affects quantitatively the responses, we relegate these results in the Technical Appendix as we believe they are secondary.

- Second, in the main text, we contrast the predictions of our baseline model allowing for imperfect mobility of labor across sectors along with adjustment costs to capital accumulation with those obtained in a model imposing perfect mobility of labor and abstracting from capital installation costs. Because both features play a pivotal role,

Table 27: Baseline Parameters (Representative OECD Economy)

Definition	Value		Reference
	OECD	Sensitivity	
Period of time	year	year	data frequency
A.Preferences			
Subjective time discount rate, β	4%	4%	equal to the world interest rate
Intertemporal elasticity of substitution for consumption, σ_C	1	1	logarithmic utility function for consumption
Elasticity of labor supply at the extensive margin, σ_L	0.4	0.2-1	Fiorito and Zanella [2012]
Separability vs. non separability in preferences, σ	1	2	Shimer [2011]
Elasticity of substitution between C^T and C^N, ϕ	0.77	0.77	our estimates (KLEMS [2011], OECD Economic Outlook)
Elasticity of substitution between J^T and J^N, ϕ_J	1	1	Bems [2008]
B.Non tradable share			
Weight of consumption in non traded goods, $1-\varphi$	0.51	0.51	set to target $\alpha_C = 53\%$ (United Nations [2011])
Weight of labor supply to the non traded sector, $1-\vartheta$	0.15	0.15	set to target $L^N/L = 67\%$ (KLEMS [2011])
Weight of non traded investment, $1-\varphi_J$	0.64	0.64	set to target $\alpha_J = 64\%$ (OECD Input-Output database [2012])
Non Tradable content of government expenditure, ω_{G^N}	0.90	0.90	our estimates (COFOG, OECD [2017])
Labor income share in the non traded sector, θ^N	0.68	0.58	our estimates (EU KLEMS [2011] and OECD STAN databases)
Labor income share in the traded sector, θ^T	0.58	0.68	our estimates (EU KLEMS [2011] and OECD STAN databases)
Labor productivity index for the traded sector, Z^T	1.28	1.28	our estimates (KLEMS [2011])
C.GDP demand components			
Physical capital depreciation rate, δ_K	6%	6%	set to target $\omega_J = 21\%$ (Source: OECD Economic Outlook Database)
Parameter governing capital adjustment cost, κ	17	0	set to match the elasticity I/K to Tobin's q (Eberly et al. [2008])
Government spending as a ratio of GDP, ω_G	20%	20%	our estimates (Source: OECD Economic Outlook Database)
D.Government Spending Shock			
Exogenous fiscal shock, g	1%	1%	To generate $dG(0)/Y = 1\%$
Persistence and shape of endogenous response of G, ξ	0.408675	0.408675	set to target $dG(1) = g'$ and $\dot{G}(1) = 0$
Persistence and shape of endogenous response of G, χ	0.415722	0.415722	set to target $dG(1) = g'$ and $\dot{G}(1) = 0$

we report in the main text the impact responses to a government spending shock in a model either imposing perfect mobility of labor across sectors or abstracting from capital installation costs. We report below, in subsection M.2, the dynamic adjustment of a model either imposing perfect mobility of labor across sectors or abstracting from capital installation costs and contrast the predictions with those obtained in the baseline model. The model imposing perfect mobility of labor while assuming capital installation costs or the other way around both fail to account for the evidence at an aggregate and a sectoral level while the latter performs better than the former in reproducing the evidence, in particular for sectoral variables.

- Third, in section 5.3 of the main text, we plot the simulated responses of output shares of tradables and non tradables against the degree of labor mobility across sectors and contrast model's predictions with estimated cross-country relationships for both tradables and non tradables. To look at the cross-country differences in the sectoral impact of a government spending shock empirically, we estimate the same VAR model, i.e., $x_{it}^{S,j}$, as for the whole sample, but for a single a country at a time. To look at the cross-country differences in the sectoral impact of a government spending shock numerically, we calibrate the baseline model to each OECD country in our sample. While in the main text, we only show the scatter-plots, in subsection M.3, we report both estimated and simulated impact responses to a government spending shock of output shares of tradables and non tradables.

M.1 Numerical Results for a Representative OECD Economy

Table 28 reports impact effects while Table 29 shows cumulative responses over a two- and four-year horizon following a rise in government consumption by 1 percentage point of GDP. Column 1 of Tables 28 and 29 shows the effects of a government spending shock from our VAR model for comparison purposes while columns 2-14 report simulated responses. We conduct a sensitivity analysis with respect to a number of parameters, including the labor income share of sector j, θ^j, the elasticity of labor supply across sectors, ϵ, the parameter κ that governs the magnitude of adjustment costs to capital accumulation, the Frisch elasticity of labor supply, σ_L, and the parameter $\sigma > 0$ that determines the substitutability between consumption and leisure. We provide more details below:

- In columns 2 and 3, we impose perfect mobility of labor across sectors, i.e., $\epsilon \to \infty$. In column 2, we abstract from capital installation costs and thus set $\kappa = 0$ while in column 3, we consider adjustment costs to physical capital accumulation and thus sect $\kappa = 17$.

- Column 4 reports results from our baseline model with imperfect mobility of labor across sectors, setting ϵ to 0.75, while capital accumulation is assumed to be subject to adjustments costs with $\kappa = 17$.

- In columns 5 and 6, we keep unchanged κ and investigate the effects of a government spending shock when the degree of labor mobility across sectors is low, i.e., ϵ is set to 0.22, and when the elasticity of labor supply across sectors is high, i.e., ϵ is set to 1.64.

- In column 7, we investigate the sensitivity of our results to the Frisch elasticity of labor supply which is raised from 0.4 to 1.

- Column 8 shows results when we allow for imperfect mobility of labor across sectors, setting ϵ to 0.75, while we abstract from adjustment costs to capital accumulation, and thus set κ to 0.

- Column 9 reports results when we relax the assumption of separability in preferences between consumption and labor, setting σ to 2.

- In column 10 (IMK), we keep unchanged $\epsilon = 0.75$, $\sigma_L = 0.4$, $\sigma = 1$, $\kappa = 17$ and we allow for imperfect mobility of capital across sectors, setting the elasticity of capital supply across sectors, η, to 0.75, and the weight $1-\zeta$ of capital supply to the non traded sector in the aggregate capital index $K(.)$ to 0.68 in order to target a non tradable content of capital income of 58%, in line with our estimates.

- While from column 2 to column 10, we assume that the non traded sector is relatively more labor intensive than the traded sector, and thus set θ^N to 0.68 and θ^T to 0.58, from column 11 to column 13, we explore the case where the non traded sector is relatively more capital intensive and thus choose reverse and symmetric values for the sectoral labor income shares, i.e., we set θ^N to 0.58 and θ^T to 0.68.
- While column 12 reports our baseline model's predictions when $\theta^T > \theta^N$, in column 11, we set $\kappa = 0$ and let ϵ tend toward infinity, and in column 13 (IMK), we allow for both imperfect mobility of labor and capital across sectors, and thus set η to 0.75.

In column 8, we relax the assumption of separability in preferences between consumption and labor by considering a functional form which is taken from Shimer [2011]:

$$\frac{C^{1-\sigma}V(L)^{\sigma}-1}{1-\sigma}, \quad \text{if} \quad \sigma \neq 1, \quad V(L) \equiv \left(1+(\sigma-1)\frac{\sigma_L}{1+\sigma_L}L^{\frac{1+\sigma_L}{\sigma_L}}\right). \tag{687}$$

These preferences are characterized by two crucial parameters: σ_L is the Frisch elasticity of labor supply, and $\sigma > 0$ determines the substitutability between consumption and leisure; if $\sigma > 1$, the marginal utility of consumption increases in hours worked. In contrast, setting $\sigma = 1$ implies that preferences are separable in consumption and labor, as in (6). When we investigate the implications of non separability in preferences, we set $\sigma = 2$ while keeping other parameters unchanged.

Column 9 shows results when σ is set to 2. As can be seen in column 9, non separability in preferences between consumption and labor amplifies the rise in the real consumption wage while hours and real GDP increase less. Additionally, the open economy runs a larger current account deficit. Intuitively, because non separability in preferences between consumption and labor increases the disutility from working, agents are less willing to supply labor while demanding higher wages. Because consumption increases with the aggregate wage, agents lower their expenditure less. Thus, private savings decline further, which in turn amplifies the decline in the current account. As the crowding out of private consumption is less, the relative price of non tradables appreciates by a larger amount, thus amplifying the responses of sectoral output shares. While the extension of the baseline model to non separability in preferences somewhat improves its performance in reproducing the responses of several sectoral variables, the extended model tends to substantially overstate the contraction in the traded sector and to overpredict the rise in the relative wage. In contrast, all simulated impact responses from the baseline model assuming separability in preferences lie within the confidence interval.

In the last three columns of Table 2, we investigate whether our conclusions hold if we assume a non traded sector that is more capital intensive than the traded sector. While the predictions of the model are very sensitive to sectoral labor income shares if we let ϵ tend toward infinity, results are almost unaffected for the baseline model whether $\theta^T < \theta^N$ or $\theta^T > \theta^N$. As shown in column 11, the model imposing perfect mobility of labor fails to account for the evidence along a number of dimensions. In particular, the simulated responses of sectoral output shares are more than four times greater than those reported from the VAR model. The reason is that imposing perfect mobility makes labor and thus sectoral output highly sensitive to a change in relative price. Because investment is crowded in, the subsequent excess demand in the non traded goods market causes the relative price of non tradables to appreciate, thus leading to dramatic changes in the relative size of sectors. Since the model's predictions reported in column 12 are similar to those shown in column 4, they do not merit further comment.

In columns 10 and 13 of Table 28, we extend the baseline model with imperfect mobility of labor along with capital installation costs to imperfect mobility of capital. A shortcut to generate imperfect capital mobility is to assume limited substitutability in capital across sectors. Along the lines of Horvath [2000] who introduce limited substitutability of hours worked, we assume that capital in the traded and the non traded sectors are aggregated by means of a CES function:

$$K\left(K^T, K^N\right) = \left[\zeta^{-\frac{1}{\eta}}\left(K^T\right)^{\frac{\eta+1}{\eta}} + (1-\zeta)^{-\frac{1}{\eta}}\left(K^N\right)^{\frac{\eta+1}{\eta}}\right]^{\frac{\eta}{\eta+1}}, \tag{688}$$

where $0 < \zeta < 1$ is the weight of capital supply to the traded sector in the aggregate capital index $K(.)$ and η measures the ease with which capital in the traded and the non traded sector can be substituted for each other and thereby captures the degree of capital mobility across sectors. The case of perfect capital mobility is nested under the assumption that η tends towards infinity; in this case, (688) reduces to $K = K^T + K^N$ which implies that capital is perfectly substitutable across sectors. When $\eta < \infty$, sectoral capital goods are no longer perfect substitutes. More specifically, as η becomes smaller, capital mobility across sectors becomes lower as investors perceive a higher cost of shifting capital and therefore become more reluctant to reallocate capital across sectors.

Panels A and B of Table 28 show impact effects of a government spending shock for GDP, investment and the current account along with labor market variables such as total hours worked and the real consumption wage. Panels C and D of Table 28 summarize the theoretical responses of sectoral variables for the labor and product markets. Because the results shown in column 10 when we allow for imperfect mobility of capital across sectors do not improve the performance of the model with imperfect mobility of labor in replicating the evidence, or provide major additional information on the fiscal transmission as the conclusions are similar whether we allow or not for imperfect mobility of capital across sectors, to save space we do not present them in the main text and relegate these results in the Technical Appendix. Panels E and F of Table 29 report cumulative responses over a two- and a fourth-year horizon for aggregate and selected sectoral variables.

M.2 Numerical Results for a Representative OECD Economy

In the main text, see section 5.2, we show that the model is successful in replicating both aggregate and sectoral effects of a government spending shock as long as we allow for both imperfect mobility of labor across sectors, captured by ϵ, along with adjustment costs to capital accumulation, captured by the parameter κ. Table 2 contrasts impact effects in the baseline scenario with a number of alternative scenarios where we impose perfect mobility of labor across sectors and abstract from capital installation costs (column 2), we consider capital installation costs along with perfect mobility of labor across sectors (column 3), and we allow for imperfect mobility of labor across sectors but abstract from capital installation costs (column 8). Figures 5 and 6 in the main text display the model predictions for the aggregate and sectoral effects, respectively, of a government spending shock under imperfect (solid black line) and perfect mobility of labor across sectors (dotted black line) together with the respective VAR evidence (solid blue line). For reason of space, we do not contrast the dynamic adjustment of the baseline model with that obtained from a model with perfect mobility of labor while assuming capital installation costs or alternatively from a model assuming imperfect mobility of labor but abstracting from adjustment costs to physical capital accumulation. The results are relegated in this subsection. We emphasize very briefly in what a model either abstracting from capital installation costs or imposing perfect mobility of labor across sectors fails to account for our panel VAR evidence.

The solid black line in Figures 53 and 54 show the predictions of the baseline model while the dotted black line displays the predictions of a model with a difficulty in reallocating labor across sectors but abstracting from capital installation costs. As emphasized in the main text, the conclusion that emerges is that the model without capital adjustment costs tend to overstate the crowding out of investment in the short-run and to understate substantially the current account deficit. Because investment declines more, excess demand in the non traded goods market and thus the appreciation in the relative price of non tradables is much smaller than that found in the data. Because the model without capital installation costs underpredicts the short-run rise in P, it tends to understate the responses of sectoral output shares. The solid black line in Figures 55 and 56 show the predictions of the baseline model while the dotted black line displays the predictions of a model imposing

Table 28: Impact Responses of Aggregate and Sectoral Variables to of a Rise in Government Consumption (in %)

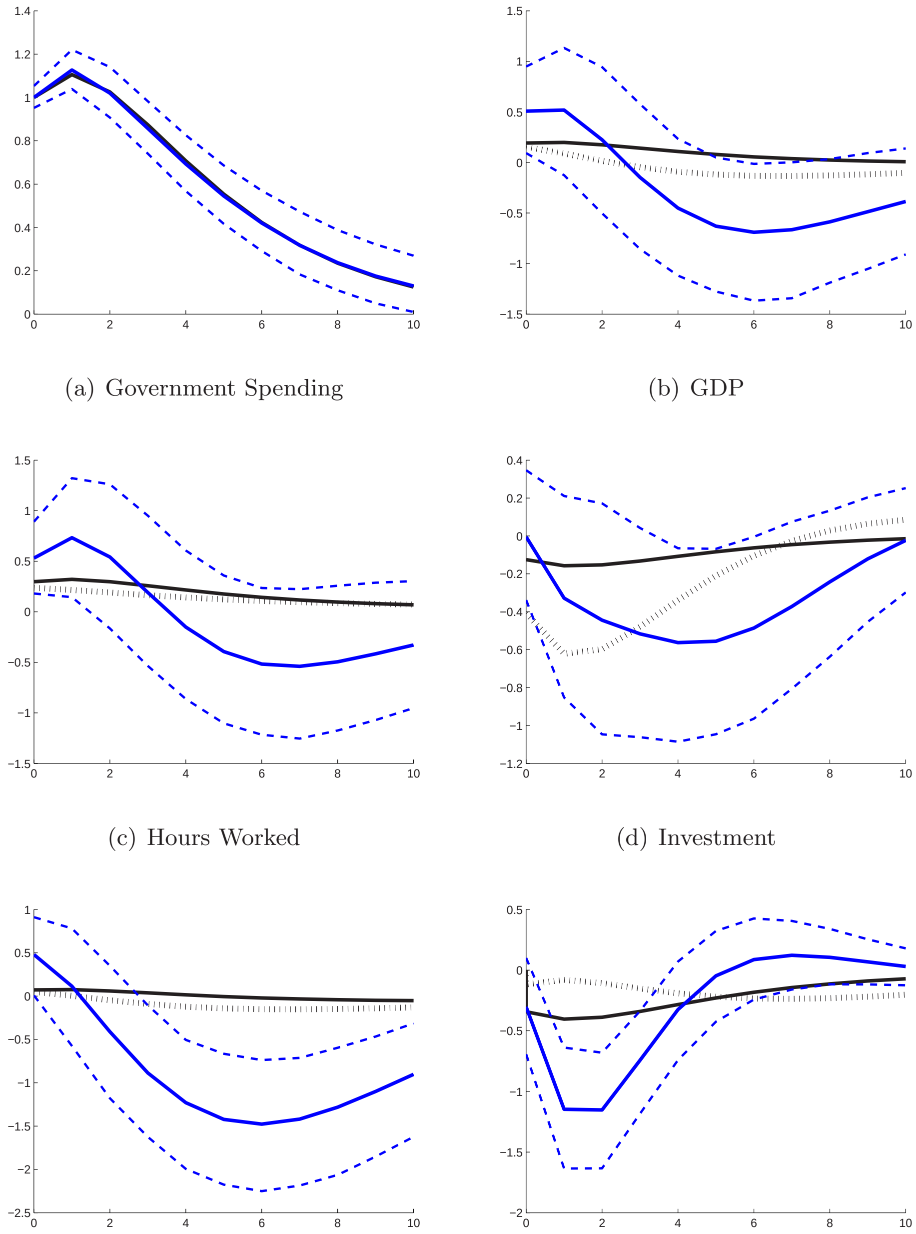
	Data	$1-\theta^T > 1-\theta^N$									$1-\theta^T < 1-\theta^N$		
		Perf. Mob.		Bench	Mobility		Lab. supply	No Adj. Cost.	Non sep.	IMK	Perf. Mob.	IML	IMK
		($\kappa = 0$)	($\kappa = 17$)	($\epsilon = 0.75$)	($\epsilon = 0.22$)	($\epsilon = 1.64$)	($\sigma_L = 1$)	($\kappa = 0$)	($\sigma = 2$)	($\eta = 0.75$)	($\epsilon = \infty$)	($\epsilon = 0.75$)	($\eta = 0.75$)
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)
A.Impact:GDP & Components													
Real GDP, $dY(0)$	0.51	0.07	0.09	0.19	0.22	0.16	0.34	0.15	0.17	0.23	0.00	0.16	0.20
Investment, $dI(0)$	-0.01	-0.84	0.04	-0.13	-0.17	-0.08	-0.14	-0.41	-0.14	-0.19	1.49	-0.22	-0.28
Current Account, $dCA(0)$	-0.30	0.06	-0.75	-0.34	-0.22	-0.46	-0.29	-0.12	-0.50	-0.18	-2.49	-0.35	-0.19
B.Impact: Labor & Real Wage													
Labor, $dL(0)$	0.53	0.11	0.15	0.30	0.34	0.25	0.53	0.24	0.27	0.36	0.00	0.25	0.32
Real wage, $d\left(W/P_C\right)(0)$	0.48	0.00	0.07	0.07	0.08	0.06	-0.04	0.05	0.12	0.10	-0.30	-0.05	-0.01
C.Impact: Sectoral Labor													
Traded labor, $dL^T(0)$	0.01	-0.20	-0.68	-0.14	0.02	-0.29	-0.04	-0.09	-0.19	-0.09	-1.94	-0.17	-0.11
Non traded labor, $dL^N(0)$	0.54	0.30	0.83	0.44	0.32	0.55	0.57	0.33	0.45	0.45	1.95	0.42	0.43
Traded wage, $d\left(W^T/P_C\right)(0)$	0.22	0.00	0.07	-0.89	-1.18	-0.61	-0.91	-0.65	-1.00	-0.76	-0.30	-0.96	-0.81
Non traded wage, $d\left(W^N/P_C\right)(0)$	0.83	0.00	0.07	0.55	0.69	0.42	0.43	0.38	0.66	0.50	-0.30	0.54	0.50
Relative labor, $d\left(L^T/L^N\right)(0)$	-0.71	-0.53	-1.86	-0.52	-0.19	-0.86	-0.50	-0.36	-0.59	-0.44	-5.83	-0.60	-0.53
Relative wage, $d\left(W^N/W^T\right)(0)$	0.93	-0.00	0.00	1.44	1.87	1.03	1.33	1.02	1.66	1.25	-0.00	1.49	1.31
Labor share of T, $d(L^T/L)(0)$	-0.27	-0.23	-0.74	-0.24	-0.09	-0.38	-0.23	-0.17	-0.27	-0.20	-1.94	-0.27	-0.23
Labor share of N, $d(L^N/L)(0)$	0.27	0.23	0.74	0.24	0.09	0.38	0.23	0.17	0.27	0.20	1.94	0.27	0.23
D.Impact: Sectoral Output													
Traded output, $dY^T(0)$	-0.03	-0.22	-0.72	-0.31	-0.19	-0.43	-0.24	-0.21	-0.37	-0.14	-1.87	-0.31	-0.15
Non traded output, $dY^N(0)$	0.70	0.28	0.82	0.50	0.41	0.59	0.58	0.37	0.55	0.37	1.87	0.47	0.34
Relative output, $d\left(Y^T/Y^N\right)(0)$	-1.03	-0.62	-3.16	-0.97	-0.64	-1.30	-0.97	-0.64	-1.07	-0.52	-4.93	-0.88	-0.51
Relative price, $dP(0)$	1.06	-0.00	0.02	0.88	1.13	0.64	0.79	0.62	1.02	1.22	0.08	1.01	1.36
Output share of T, $d(Y^T/Y_R)(0)$	-0.45	-0.24	-0.76	-0.38	-0.26	-0.49	-0.37	-0.27	-0.44	-0.22	-1.87	-0.37	-0.21
Output share of N, $d(Y^N/Y_R)(0)$	0.35	0.24	0.76	0.38	0.26	0.49	0.37	0.27	0.44	0.22	1.87	0.37	0.21

Notes: Effects of an unanticipated and temporary exogenous rise in government consumption by 1% of GDP. Panels A,B,C,D show the initial deviation in percentage relative to steady-state for aggregate and sectoral variables. Market product (aggregate and sectoral) quantities are expressed in percent of initial GDP while labor market (aggregate and sectoral) quantities are expressed in percent of initial total hours worked; θ^T and θ^N are the labor income share in the traded sector and non traded sector, respectively; ϵ measures the degree of substitutability in hours worked across sectors and captures the degree of labor mobility; σ_L is the Frisch elasticity of labor supply; κ governs the magnitude of adjustment costs to capital accumulation; σ determines the substitutability between consumption and leisure when preferences are non separable, η measures the degree of substitutability in capital across sectors and captures the degree of capital mobility. In our baseline calibration we set $\theta^T = 0.58$, $\theta^N = 0.68$, $\epsilon = 0.75$, $\eta \to \infty$, $\phi = 0.77$, $\sigma_L = 0.4$, $\kappa = 17$, $\sigma = 1$.

Table 29: Cumulative Responses of Aggregate and Sectoral Variables to of a Rise in Government Consumption (in %)

	Data	$1-\theta^T > 1-\theta^N$									$1-\theta^T < 1-\theta^N$		
		Perf. Mob.		Bench	Mobility		Lab. supply	No Adj. Cost.	Non sep.	IMK	Perf. Mob.	IML	IMK
		$(\kappa=0)$	$(\kappa=17)$	$(\epsilon=0.75)$	$(\epsilon=0.22)$	$(\epsilon=1.64)$	$(\sigma_L=1)$	$(\kappa=0)$	$(\sigma=2)$	$(\eta=0.75)$	$(\epsilon=\infty)$	$(\epsilon=0.75)$	$(\eta=0.75)$
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)
E.Cumulative: 2 year													
Real GDP, dY_R	1.03	0.07	0.19	0.39	0.45	0.33	0.70	0.24	0.34	0.47	0.14	0.32	0.40
Investment, dI	-0.33	-1.23	0.10	-0.28	-0.39	-0.18	-0.31	-1.03	-0.31	-0.43	1.89	-0.50	-0.63
Current account, dCA	-1.45	-0.47	-1.65	-0.75	-0.48	-1.00	-0.64	-0.20	-1.08	-0.39	-3.90	-0.75	-0.42
Labor, dL	1.26	0.21	0.30	0.62	0.71	0.53	1.11	0.45	0.55	0.74	0.07	0.53	0.67
Real wage, dW/P_C	0.59	0.00	0.15	0.15	0.17	0.13	-0.08	0.05	0.25	0.20	-0.41	-0.11	-0.02
Relative price, dP	3.42	0.00	0.04	1.85	2.39	1.35	1.67	1.22	2.16	2.58	0.11	2.12	2.85
Relative wage, $d\Omega$	2.50	0.00	0.00	3.04	3.94	2.18	2.82	2.04	3.51	2.64	0.00	3.13	2.76
Traded output, dY^T	-0.10	-0.85	-1.54	-0.67	-0.40	-0.92	-0.50	-0.45	-0.80	-0.30	-2.97	-0.66	-0.31
Non traded output, dY^N	1.27	0.92	1.73	1.06	0.85	1.25	1.21	0.69	1.15	0.77	3.12	0.98	0.71
Output share of T, $d(Y^T/Y_R)$	-0.99	-0.87	-1.61	-0.81	-0.56	-1.04	-0.77	-0.54	-0.92	-0.46	-3.03	-0.77	-0.45
Output share of N, $d(Y^N/Y_R)$	0.76	0.87	1.61	0.81	0.56	1.04	0.77	0.54	0.92	0.46	3.03	0.77	0.45
F.Cumulative: 4 year													
Real GDP, dY	1.10	0.05	0.38	0.71	0.81	0.61	1.31	0.21	0.62	0.84	0.50	0.57	0.71
Investment, dI	-1.29	-1.19	0.20	-0.57	-0.79	-0.35	-0.63	-2.11	-0.62	-0.87	1.74	-1.01	-1.27
Current account, dCA	-3.35	-2.15	-3.24	-1.48	-0.95	-1.98	-1.25	-0.46	-2.14	-0.76	-5.44	-1.47	-0.81
Labor, dL	1.99	0.42	0.58	1.17	1.35	1.01	2.10	0.81	1.04	1.40	0.27	1.00	1.26
Real wage, $d(W/P_C)$	-0.70	0.00	0.28	0.24	0.29	0.23	-0.17	-0.09	0.43	0.34	-0.47	-0.23	-0.09
Relative price, dP	7.98	-0.00	0.08	3.51	4.53	2.55	3.16	2.34	4.08	4.89	0.13	4.01	5.40
Relative Wage, $d\Omega$	5.17	-0.00	0.00	5.76	7.49	4.14	5.34	3.99	6.66	5.01	-0.00	5.92	5.22
Traded output, dY^T	-0.79	-2.39	-2.91	-1.28	-0.77	-1.75	-0.96	-0.99	-1.53	-0.59	-4.19	-1.26	-0.60
Non traded output, dY^N	1.88	2.44	3.28	1.98	1.58	2.36	2.28	1.20	2.15	1.43	4.69	1.83	1.31
Output share of T, $d(Y^T/Y_R)$	-2.02	-2.40	-3.05	-1.54	-1.06	-1.98	-1.47	-1.06	-1.75	-0.89	-4.38	-1.46	-0.85
Output share of N, $d(Y^N/Y_R)$	1.77	2.40	3.05	1.54	1.06	1.98	1.47	1.06	1.75	0.89	4.38	1.46	0.85

Notes: Effects of an unanticipated and temporary exogenous rise in government consumption by 1% of GDP. Panels E and F show the cumulative responses over a two- and four-year horizon, respectively. Market product (aggregate and sectoral) quantities are expressed in percent of initial GDP while labor market (aggregate and sectoral) quantities are expressed in percent of initial total hours worked; θ^T and θ^N are the labor income share in the traded sector and non traded sector, respectively; ϵ measures the degree of substitutability in hours worked across sectors and captures the degree of labor mobility; σ_L is the Frisch elasticity of labor supply; κ governs the magnitude of adjustment costs to capital accumulation; σ determines the substitutability between consumption and leisure when preferences are non separable, η measures the degree of substitutability in capital across sectors and captures the degree of capital mobility. In our baseline calibration we set $\theta^T = 0.58$, $\theta^N = 0.68$, $\epsilon = 0.75$, $\eta \to \infty$, $\phi = 0.77$, $\sigma_L = 0.4$, $\kappa = 17$, $\sigma = 1$.



(a) Government Spending

(b) GDP

(c) Hours Worked

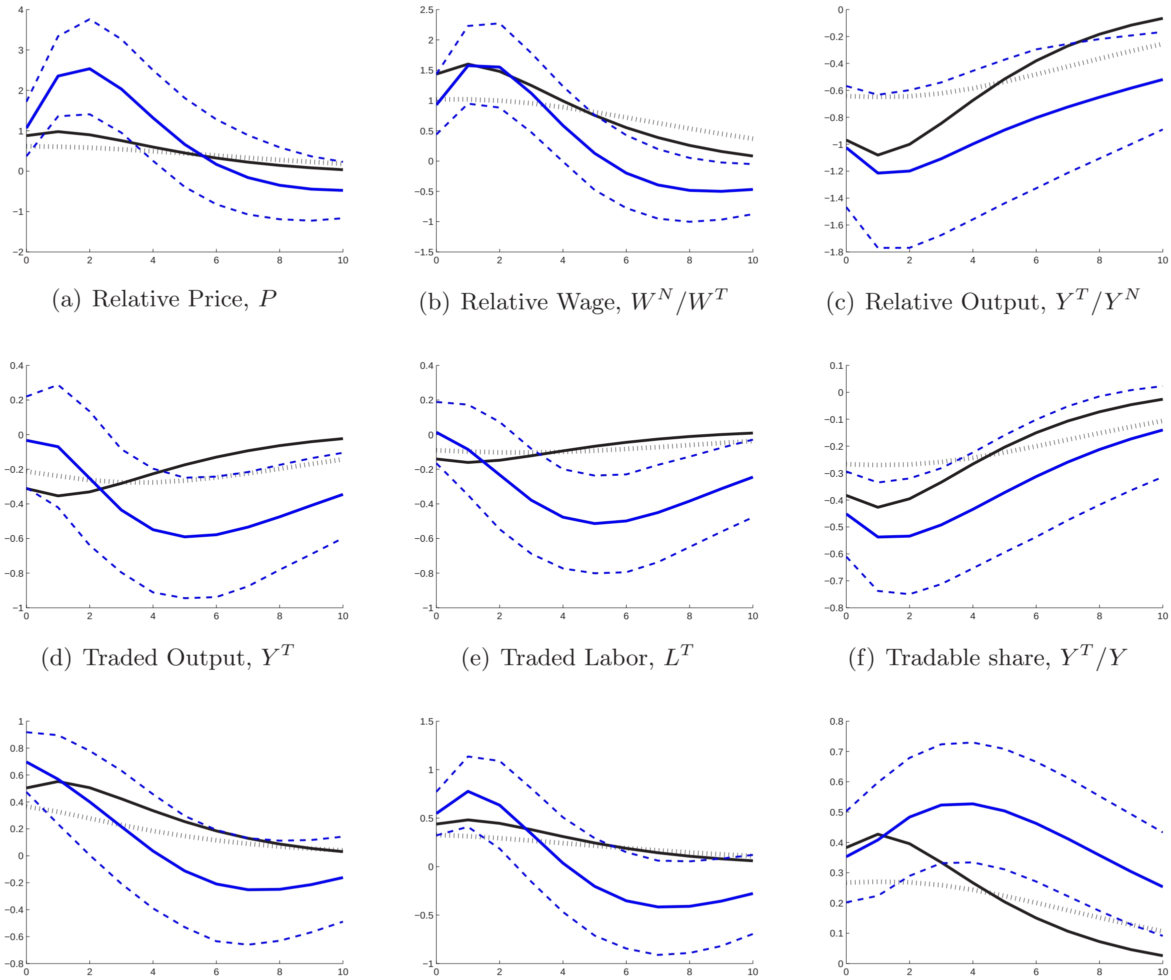
(d) Investment

(e) Aggregate Real Wage

(f) Current Account

Figure 53: Dynamic Adjustment of Aggregate Variables to Unanticipated Government Spending Shock: The Role of Capital Adjustment Costs. Notes: solid blue line display point estimate of VAR with dotted blue lines indicating 90% confidence bounds; the solid black line displays model predictions in the baseline scenario with imperfect mobility of labor across sectors ($\epsilon = 0.75$) and capital installation costs ($\kappa = 17$) while the dotted black line shows results when abstracting from capital adjustment costs ($\kappa = 0$).

perfect mobility of labor across sectors while assuming that capital accumulation is subject to installation costs. First, the model predicts a rise in investment instead of decline, in contradiction with the evidence, and tends to overstate the current account deficit. Turning to the sectoral effects, while assuming capital installation costs restore transitional dynamics for the relative price of non tradables, the model imposing perfect mobility considerably understates the appreciation in the relative price and cannot account for the rise in non traded wages relative to traded wages as sectoral wages equalize. Moreover, while the relative price of non tradables merely appreciates, because labor is extremely sensitive to relative price changes, the consecutive changes in sectoral output shares conflict with the evidence since their magnitude are about twice what is estimated empirically,

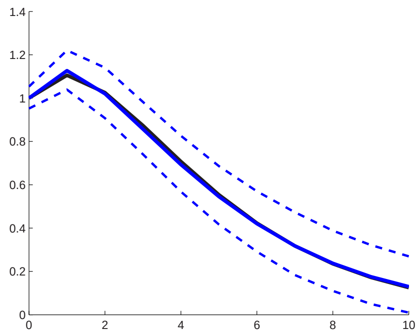


(a) Relative Price, P (b) Relative Wage, W^N/W^T (c) Relative Output, Y^T/Y^N

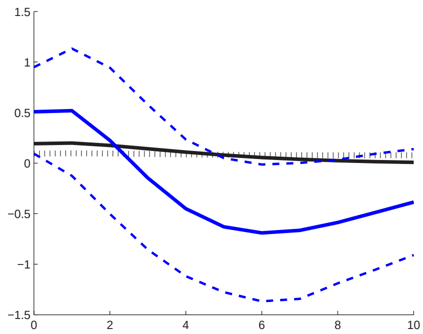
(d) Traded Output, Y^T (e) Traded Labor, L^T (f) Tradable share, Y^T/Y

(g) Non Traded Output, Y^N (h) Non Traded Labor, L^N (i) Non Tradable share, Y^N/Y

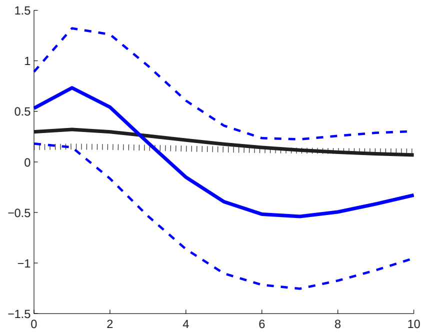
Figure 54: Dynamic Adjustment of Sectoral Variables to Unanticipated Government Spending Shock: The Role of Capital Adjustment Costs. Notes: Solid blue line display point estimate of VAR with dotted blue lines indicating 90% confidence bounds; the solid black line displays model predictions in the baseline scenario with imperfect mobility of labor across sectors ($\epsilon = 0.75$) and capital installation costs ($\kappa = 17$) while the dotted black line shows results when abstracting from capital adjustment costs ($\kappa = 0$).



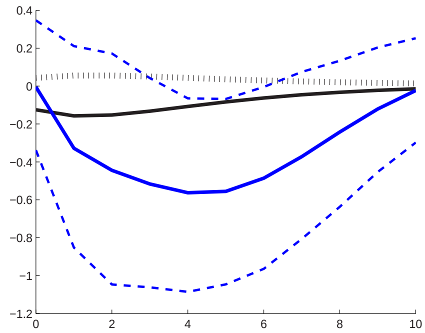
(a) Government Spending



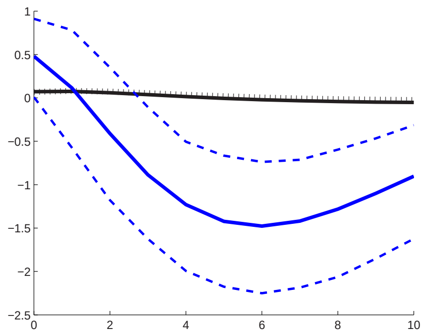
(b) GDP



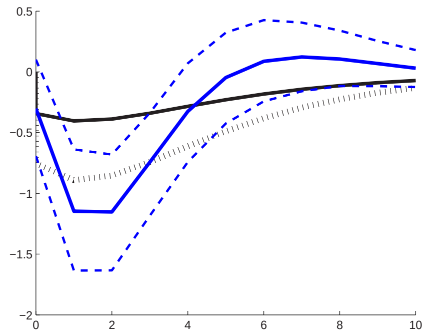
(c) Hours Worked



(d) Investment



(e) Aggregate Real Wage



(f) Current Account

Figure 55: Dynamic Adjustment of Aggregate Variables to Unanticipated Government Spending Shock: The Role of Limited Mobility across Sectors. Notes: solid blue line display point estimate of VAR with dotted blue lines indicating 90% confidence bounds; the solid black line displays model predictions in the baseline scenario with imperfect mobility of labor across sectors ($\epsilon = 0.75$) and capital installation costs ($\kappa = 17$) while the dotted black line shows results when imposing perfect mobility of labor across sectors ($\epsilon \to \infty$).

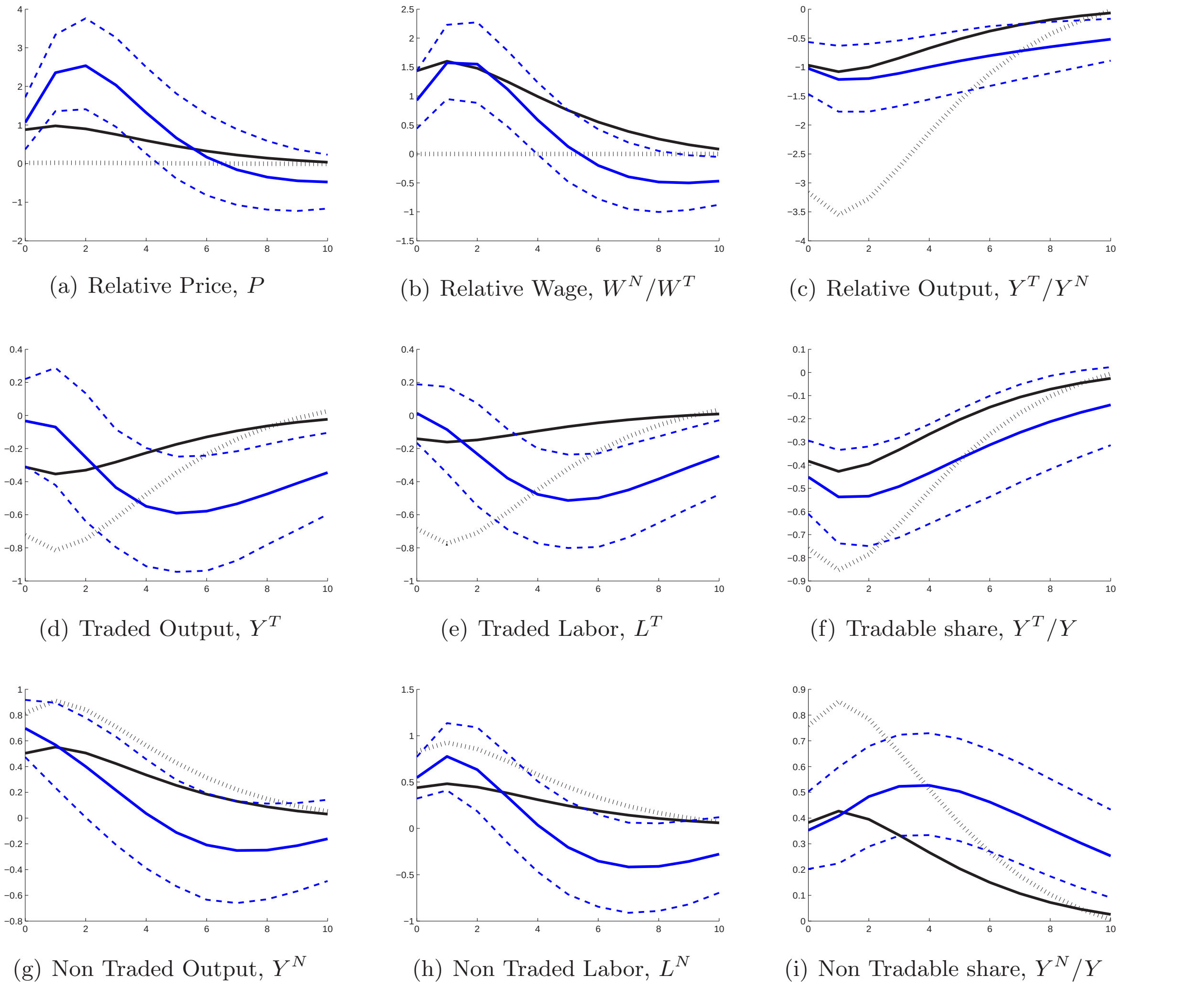


Figure 56: Dynamic Adjustment of Sectoral Variables to Unanticipated Government Spending Shock: The Role of Limited Labor Mobility across Sectors. Notes: Solid blue line display point estimate of VAR with dotted blue lines indicating 90% confidence bounds;the solid black line displays model predictions in the baseline scenario with imperfect mobility of labor across sectors ($\epsilon = 0.75$) and capital installation costs ($\kappa = 17$) while the dotted black line shows results when imposing perfect mobility of labor across sectors ($\epsilon \to \infty$).

M.3 Simulated Responses of Sectoral Output Shares across Countries

We denote by $\nu_i^{Y,j}(t)$ the output (Y) share of sector j, in country i at year t. In terms of our model's notation, the response of the output share of sector j to a government spending shock is measured in total output units and thus is calculated as the product between the growth differential between sectoral output and GDP (both at constant prices) and the content of production of good j in total output. Formally, the response at year t of the sectoral output share to a government spending shock reads as:

$$\hat{\nu}_i^{Y,j}(t) = \frac{P_i^j Y_i^j}{P_i Y_i}\left(\hat{Y}_{it}^j - \hat{Y}_{R,it}\right).$$

To assess the ability of our model to account for our evidence, we calibrate the model to the data of each country in our sample, except for the world interest rate, elasticity of labor supply, and κ that governs the magnitude of capital adjustment costs which are kept unchanged, i.e., $r^\star = 4\%$, $\sigma_L = 0.4$, and $\kappa = 17$. When numerically computing $\hat{\nu}_i^{Y,j}(0)$ for each country i, we set ϕ_i ϵ_i in accordance with their empirical estimates shown the two last columns of Table 5. When we calibrate the model to the whole sample (i.e., a representative OECD economy), we set ϵ to 0.75 and ϕ to 0.77 which correspond to their unweighted average values.

Columns 2 and 4 of Table 30 report the simulated impact responses of the output share of tradables, $\hat{\nu}_i^{Y,T}(0)$, and non tradables, $\hat{\nu}_i^{Y,N}(0)$, respectively, to an exogenous rise in government consumption by 1 percentage point of GDP. Columns 3 and 5 report point estimates from the VAR model for $\hat{\nu}_i^{Y,j}(0)$ for each country and the whole sample as well. In line with our model's predictions, an increase in government consumption gives rise to a contraction in the traded sector and has an expansionary effect on the non traded sector, except for Australia and Ireland. Because in these two economies, the traded sector expands while the non traded sector shrinks, we consider a rise in government consumption by 1 percentage point of GDP triggered by an increase in public purchases on tradables while keeping G^N fixed.

Because the time horizon of the sample is small for each country due to the annual frequency of data, the VAR estimates have to be taken with a grain of salt. More precisely, VAR estimates for $\hat{\nu}_i^{Y,j}(0)$ are significant at 10% for only five countries in our sample. As shown in the last line of Table 30, our model predicts remarkably well the contraction in the traded sector and the expansionary effect in the non traded sector. While our results tends to understate the changes in output shares of both sectors, the predicted values lie within the 90% confidence interval for most of the economies of our sample. More precisely, when we restrict our attention to statistically significant estimates, the model's predictions fall in the range of empirical estimates except for Canada. While we find that the model tends to understate the responses of sectoral output shares for most of the countries, in particular for Japan, Sweden, and the USA, the correlation between predicted and observed series is 0.65 for tradables and 0.69 for non tradables, as shown in the last line of Table 30, which suggest that the model can account reasonably well for cross-country differences in impact responses of sectoral output shares to a government spending shock.

To investigate the relationship between the magnitude of the sectoral impact of a fiscal shock and the degree of labor mobility across sectors, we regress the estimated sectoral output responses, $\hat{\nu}_i^{Y,j}(0)$, on the elasticity of labor supply across sectors, ϵ_i:

$$\hat{\nu}_i^{Y,j}(0) = \beta_0 + \beta_1 .\epsilon_i + \varepsilon_i. \tag{689}$$

According to our estimates reported in Table 31, the regression coefficient, β_1, is negative for tradables and positive for non tradables which suggests that following a rise in government consumption, the output share of tradables falls more while the output share of non tradables rises by a larger amount in countries with a higher labor mobility across sectors. Importantly, the regression coefficients from simulated and estimated values are roughly similar.

M.4 Robustness Check: Additional Numerical Results

In thus subsection, we present results from two extensions of the baseline model:

Table 30: Comparison of Simulated with Estimated Values for Changes in Sectoral Output Shares

Country	Parameter	Impact responses: sectoral output shares			
	(1)	(2)	(3)	(4)	(5)
	Mobility ϵ	$\left(\hat{\nu}_i^{Y,T}(0)\right)^{simul}$	$\left(\hat{\nu}_i^{Y,T}(0)\right)^{estim}$	$\left(\hat{\nu}_i^{Y,N}(0)\right)^{simul}$	$\left(\hat{\nu}_i^{Y,N}(0)\right)^{estim}$
AUS	0.635	$0.09^{\dagger}$	0.49	$-0.09^{\dagger}$	-0.15
AUT	0.548	$-0.32^{\dagger}$	-0.35	$0.32^{\dagger}$	0.22
BEL	0.326	$-0.28^{\dagger}$	-0.12	$0.28^{\dagger}$	0.12
CAN	0.454	-0.37	-1.03	0.37	0.94
DNK	-	-0.31	-0.77	0.31^{*}	0.68
ESP	1.642	$-0.49^{\dagger}$	-0.19	$0.49^{\dagger}$	0.39
FIN	0.544	-0.34^{*}	-0.81	0.34^{*}	0.90
FRA	1.287	$-0.40^{\dagger}$	-0.36	$0.40^{\dagger}$	0.41
GBR	1.008	$-0.42^{\dagger}$	-0.46	$0.42^{\dagger}$	0.55
IRL	0.264	$0.05^{\dagger}$	0.05	$-0.05^{\dagger}$	-0.07
ITA	0.686	$-0.38^{\dagger}$	-0.60	$0.38^{\dagger}$	0.50
JPN	0.993	$-0.41^{\dagger}$	-0.96	$0.41^{\dagger}$	0.89
NLD	0.224	$-0.26^{\dagger}$	-0.18	$0.26^{\dagger}$	0.22
NOR	-	$-0.35^{\dagger}$	0.03	$0.35^{\dagger}$	0.09
SWE	0.443	-0.35^{*}	-0.69	0.35^{*}	0.59
USA	1.387	-0.40^{*}	-1.21	0.40^{*}	0.77
Whole	0.746	-0.38^{*}	-0.43	0.38^{*}	0.33
Corr.			0.63		0.67

Notes: Table provides simulated (*simul*) and estimated (*estim*) responses on impact for $\hat{\nu}_i^{Y,j}(0)$ (with $j = T, N$); responses correspond to the change in sectoral value added at constant prices relative to real GDP measured in total output units; when computing the change in the share of valued added of sector j, we keep relative prices constant so that its change is only triggered by variations in quantities; ϵ is the elasticity of labor supply across sectors; because estimates of ϵ for Denmark and Norway are not statistically significant, their values are left blank. Predicted values for Denmark are obtained when setting ϵ to its value for the whole sample. We denote by superscripts 'simul' and 'estim' the numerically computed values and VAR estimates, respectively; † and * indicate that the predicted value lies within the estimated confidence interval while * indicates that the estimated value is significant at 10%; we calculate 90% confidence intervals based on estimated standard deviations of $\hat{\nu}_i^{Y,j}(0)$ obtained when the VAR model is estimated, for each country and the whole sample as well; 'Corr.' refers to the correlation coefficient between simulated and estimated values.

Table 31: Relationship between Impact Responses of Sectoral Output Shares to a Rise in Government Consumption and the Degree of Labor Mobility across Sectors (OLS estimates)

Variable	β_0	β_1	R^2	N
Y^T/Y				
Data	-0.272 (-1.090)	-0.249 (-0.860)	0.058	14
Model	-0.156^c (-1.904)	-0.207^b (-2.240)	0.295	14
Y^N/Y				
Data	0.274 (1.452)	0.234 (1.072)	0.087	14
Model	0.156^c (1.904)	0.207^b (2.240)	0.295	14

Notes: ^{a}, ^{b} and ^{c} denote significance at 1%, 5% and 10% levels; t-statistics are reported in parentheses.

- While we assume that both the traded and the non traded sector are perfectly competitive, this assumption can be considered as restrictive for the non traded sector which is sheltered from foreign competition and thus consists of industries with higher markups than the traded sector. The fact that markups are high in non traded industries implies that the elasticity of the markup to entry is high as well; as a result, by producing profit profit opportunities and thus encouraging firm entry, a rise in G^N produce a fall in the markup that may modifies quantitatively the size of the change in the share of non tradables in real GDP. In section K, we lay out the model with an imperfectly competitive non traded sector where the markups are endogenous in order to investigate the extent to which firm entry modifies our baseline results.

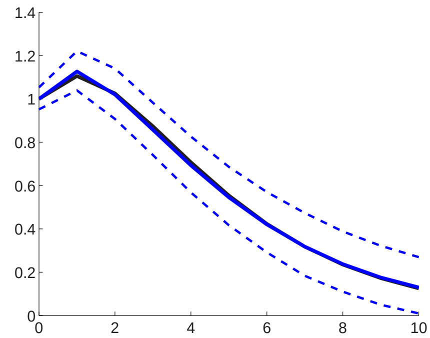
- The second extension is related to our assumption that the government budget is balanced at each instant so that the rise in government spending is financed by an increase in lump-sum taxes. As long as taxes are lump-sum, Ricardian equivalence obtains and the time path of taxes is irrelevant for the real allocation. Thus, whether the government budget is balanced or not affects our results neither qualitatively nor quantitatively. If taxes are distorsionary, then the manner of financing higher spending can influence the results. In section J, we lay out a model with public debt which enables us to analyze the differences between the effects of a government spending shock whether it is either debt-financed or budget-balanced.

Calibration of the Model with Endogenous Markups and Results

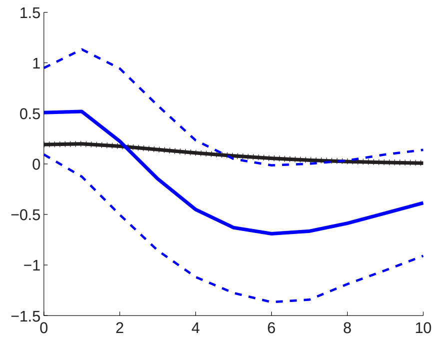
To calibrate our model to a representative OECD economy, we keep the same values for all parameters shown in Table 27 in order to make our results comparable with those obtained for the baseline model. Since we consider an imperfect competitive non traded sector, we have to choose values for the elasticity of substitution between intermediate goods produced non traded industries, η, and the value for the elasticity of substitution between varieties within one non traded industry, ρ. Setting ρ to 4 and η to 1 yields a markup μ charged by the non-traded sector of 1.35, which is close to OECD countries' unweighted average (1970-2004) documented by Cardi and Restout [2015] for 13 OECD countries that includes all countries in our sample except for Australia, Canada, Finland. We choose a value of fixed costs ψ so that the number of competitors is 20 within each non traded industry which is consistent with our assumption according to which the number of firms is large enough so that we can ignore the strategic effects but not so large that the effect of entry on the firm's demand curve is minuscule.

Calibration of the Model with Public Debt and Results

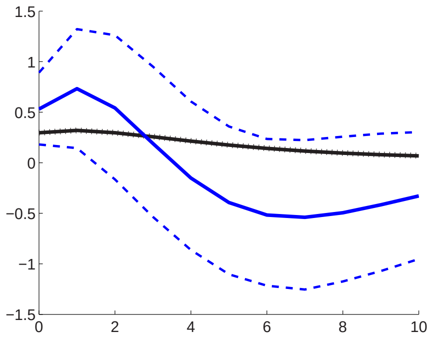
To calibrate the model with public debt to a representative OECD economy, we estimate a VAR model that includes public debt, D, in order to determine the dynamic response of public debt to an exogenous government spending shock. More specifically, the VAR specification includes government consumption, public debt, real GDP, hours worked, non-residential investment, and the real consumption wage. Time series for public debt as



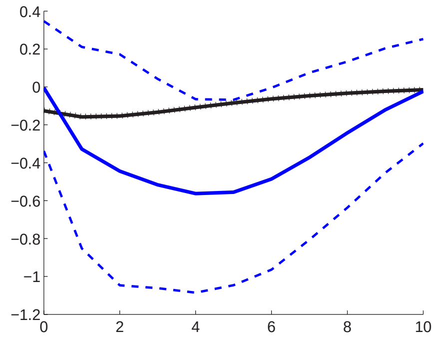
(a) Government Spending



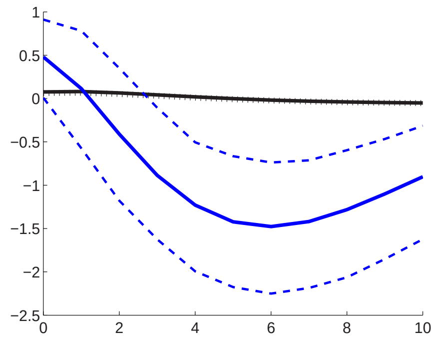
(b) GDP



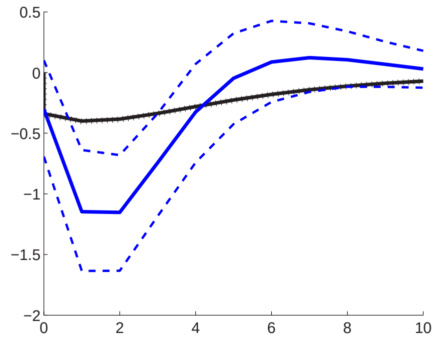
(c) Hours Worked



(d) Investment



(e) Aggregate Real Wage



(f) Current Account

Figure 57: Dynamic Adjustment of Aggregate Variables to Unanticipated Government Spending Shock: The Role of Endogenous Markups. Notes: solid blue line display point estimate of VAR with dotted blue lines indicating 90% confidence bounds; the solid black line displays model predictions in the baseline scenario with imperfect mobility of labor across sectors ($\epsilon = 0.75$) and capital installation costs ($\kappa = 17$) while the dotted black line shows results for the case of endogenous markups.

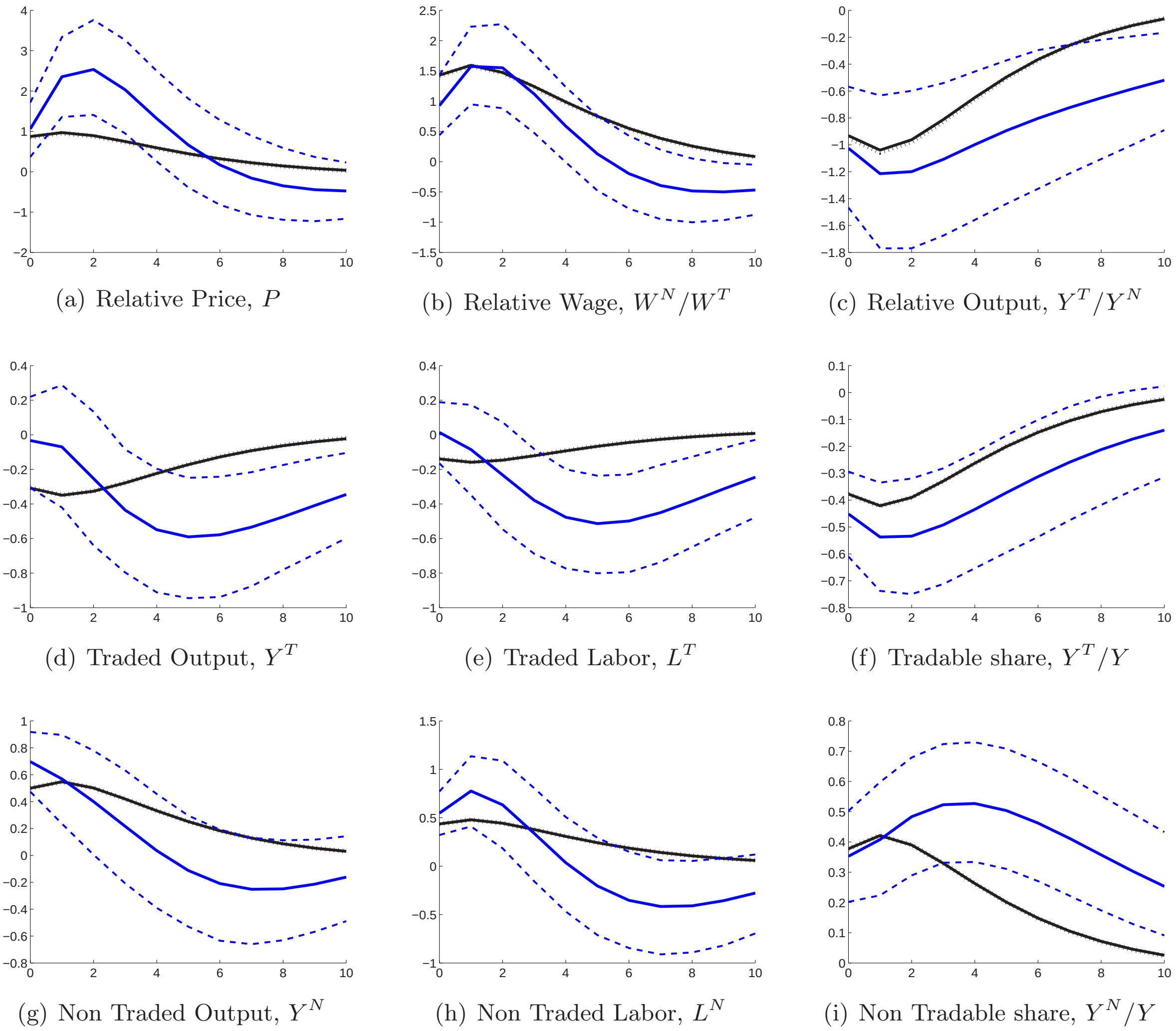


Figure 58: Dynamic Adjustment of Sectoral Variables to Unanticipated Government Spending Shock: The Role of Endogenous Markups. Notes: Solid blue line display point estimate of VAR with dotted blue lines indicating 90% confidence bounds;the solid black line displays model predictions in the baseline scenario with imperfect mobility of labor across sectors ($\epsilon = 0.75$) and capital installation costs ($\kappa = 17$) while the dotted black line shows results for the case of endogenous markups.

a percentage of GDP are taken from the OECD. As displayed in 59(b), the endogenous response of public to an exogenous government spending shock is hump-shaped and displays high persistence. More precisely, public debt reaches a peak at time $t = 6$ and then is restored back toward its initial level after 30 years. Before discussing the calibration of the model, it is convenient to repeat the equations which govern the adjustment of government spending, public debt, and taxes we derive in section J (see eq. (593), (596), (597)):

$$\frac{dG(t)}{Y} = e^{-\xi t} - (1-g)\, e^{-\chi t}, \tag{690a}$$

$$\frac{dD(t)}{Y} = \Theta_D e^{-\delta t} - \Theta_1 e^{-\xi t} + \Theta_2 e^{-\chi t}, \tag{690b}$$

$$\frac{dT(t)}{Y} = \theta_L d\tau(t), \tag{690c}$$

$$d\tau(t) = \Omega_D e^{-\delta t} - \left(\Omega 1 e^{-\xi t} - \Omega_2 e^{-\chi t}\right), \tag{690d}$$

where τ is a distortive labor tax we impose $D_0 = \tilde{D}$ in line with our VAR evidence, i.e., public debt is restored to its initial level. To calibrate the model with public debt, we have to choose values for three new parameters, ϕ_D, ϕ_G, δ. Since $\delta = \phi_D - r^\star$, it leaves us with only two parameters. These two parameters are chosen so as to reproduce the hump-shaped response of the public debt in percentage of GDP. Using the fact that public debt peaks at $\hat{t} = 6$, we solve the system of equations below to determine the values for ϕ_D and ϕ_G:

$$\dot{D}(\hat{t}) = -\delta\Theta_D e^{-\delta\hat{t}} + \xi\Theta_1 e^{-\xi\hat{t}} - \chi\Theta_2 e^{-\chi\hat{t}} = 0, \tag{691a}$$

$$\frac{dD(\hat{t})}{Y} = \Theta_D e^{-\delta\hat{t}} - \Theta_1 e^{-\xi\hat{t}} + \Theta_2 e^{-\chi\hat{t}}. \tag{691b}$$

Using the fact that at $\hat{t} = 6$, we have $\frac{dD(\hat{t})}{Y} = 1.68738$, solving yields $\phi_G = 0.485728$ and $\phi_D = 0.169004$.

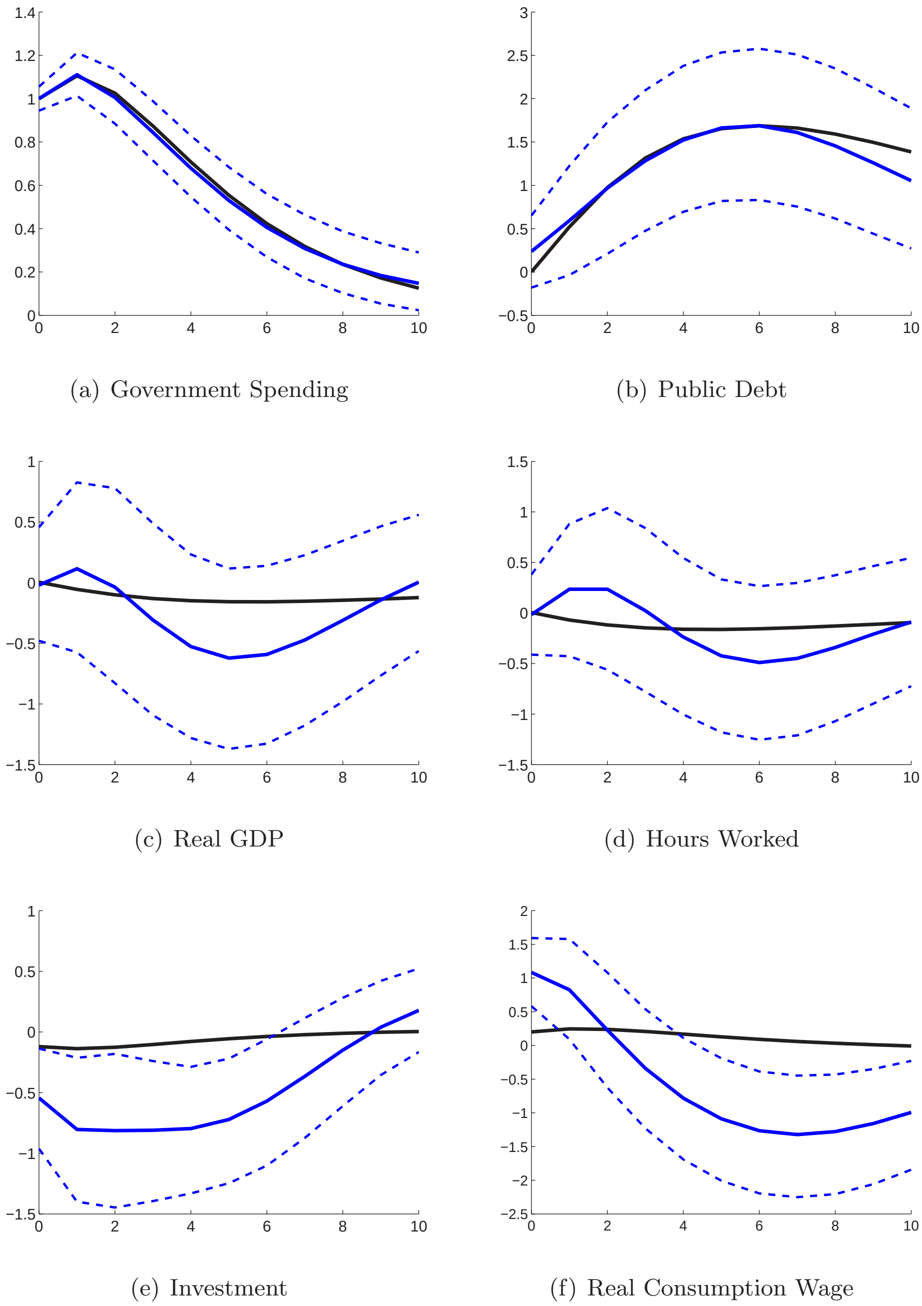


Figure 59: Dynamic Adjustment to an Unanticipated Deficit-Financed Government Spending Shock. Notes: The solid blue line displays point estimates of the VAR model with public debt, with dotted blue lines indicating the 90% confidence bounds; the solid black line displays model predictions in the baseline scenario with imperfect mobility of labor across sectors ($\epsilon = 0.75$) and capital installation costs ($\kappa = 17$).

References

Beetsma, Roel and Massimo Giuliodori (2011) The Effects of Government Purchases Shocks: Review and Estimates for the EU. *Economic Journal*, 121(550), pp. 4-32.

Bermperoglou, Dimitrios, Evi Pappa, and Eugenia Vella (2016) The Government Wage Bill and Private Activity. *Cahiers de Recherches Economiques du Département d'Econométrie et d'Economie politique* 16-24, Université de Lausanne.

Bertinelli, Luisito, Olivier Cardi, Romain Restout. *Technological Change Biased toward the Traded Sector and Labor Market Frictions*, Working Paper of BETA, 2016-05.

Bouakez, Hafedh and Nooman Rebei (2007) Why Does Private Consumption Rise After a Government Spending Shock? *Canadian Journal of Economics*, 40(3), pp. 954-979.

Brückner, Markus, and Evi Pappa (2012) Fiscal Expansions, Unemployment, And Labor Force Participation: Theory And Evidence. *International Economic Review*, 53(4), pp. 1205-1228,

Burstein, Ariel T., João C. Neves and Sergio Rebelo (2004) Investment Prices and Exchange Rates: Some Basic Facts. *Journal of the European Economic Association* 2(2-3), pp. 302-309.

Cardi Olivier and Romain Restout (2015) Fiscal Shocks in a Two Sector Open Economy with Endogenous Markups. *Macroeconomic Dynamics*, vol. 19 (8), pp. 1839-1865.

Cardi, Olivier and Romain Restout (2014) Unanticipated vs. Anticipated Tax Reforms in a Two-Sector Open Economy. *Open Economies Review*, 25(2), pp. 373-406.

Cashin, Paul and John C. McDermott (2003) Intertemporal Substitution and Terms-of-Trade Shocks. *Review of International Economics*, 11(4), pp. 604-618.

Cavallo, Michele (2005) Government Employment and the Dynamic Effects of Fiscal Policy Shocks. *Working Paper Series 2005-16*. Federal Reserve Bank of San Francisco.

Corsetti, Giancarlo, André Meier, and Gernot J. Müller (2012) Fiscal Stimulus with Spending Reversals. *The Review of Economics and Statistics*, 94(4), pp. 878-895.

Cordoba (de), Gonzalo Fernandez and Timothy J. Kehoe (2000) Capital Flows and Real Exchange Rate Fluctuations Following Spain's Entry into the European Community. *Journal of International Economics*, 51(1), 49-78.

Engle Robert F., David F. Hendry and Jean-François Richard (1983) Exogeneity. *Econometrica*, 51, pp. 277-304.

Galí, Jordi, J. David López-Salido and J. Vallés (2007) Understanding the Effects of Government Spending on Consumption. *Journal of the European Economic Association* 5, pp. 227-270.

Granger Clive W.J. (1969) Investigating Causal Relations by Econometrics Models and Cross-Spectral Methods. *Econometrica*, 37, pp. 424-438.

Guajardo, Jaime, Daniel Leigh, and Andrea Pescatori (2014) Expansionary Austerity? International Evidence. *Journal of the European Economic Association*, 12(4), pp. 949-968.

Hadri, Kaddour (2000) Testing for Unit Roots in Heterogeneous Panel Data. *Econometrics Journal*, 3, pp. 148-161.

Jaimovich, Nir and Joseph Floetotto (2008) Firm Dynamics, Markup Variations and the Business Cycle. *Journal of Monetary Economics*, 55, pp. 1238-1252.

Kambourov, Gueorgui (2009) Labour Market Regulations and the Sectoral Reallocation of Workers: The Case of Trade Reforms. *The Review of Economic Studies*, 76, pp. 1321-1358.

Kilian, Lutz and Helmut Lütkepohl (2017) Structural Vector Autoregressive Analysis. Cambridge University Press. Forthcoming.

Li, Rong (2014) (Government Sector and the Government Spending Multipliers. Mimeo. Renmin University of China.

Morshed, Mahbub A. K. M., and Stefen J. Turnovsky (2004) Sectoral Adjustment Costs and Real Exchange Rate Dynamics in a Two-Sector Dependent Economy. *Journal of International Economics* 63, pp. 147-177.

Nekarda, Christopher J. and Valerie A. Ramey (2011) Industry Evidence on the Effects of Government Spending. *American Economic Journal: Macroeconomics*, 3(1), pp. 36-59.

Ostry, Jonathan, and Carmen M. Reinhart (1992) *Private Saving and Terms of Trade Shocks: Evidence from Developing Countries*, IMF Staff Papers 39(3), pp. 495-517.

Pappa, Evi (2009) The Effects of Fiscal Shocks on Employment and the Real Wage. *International Economic Review* 50, pp. 217-244.

Pedroni, Peter (2001) Purchasing Power Parity Tests in Cointegrated Panels. *The Review of Economics and Statistics*, 83(4), pp. 727-731.

Pedroni, Peter (2004) Panel Cointegration: Asymptotic and Finite Sample Properties of Pooled Time Series Tests with an Application to the PPP Hypothesis. *Econometric Theory*, 20, pp. 597-625.

Ramey, Valerie (2013) Government Spending and Private Activity, published in 'Fiscal Policy After the Financial Crisis' eds. Alberto Alesina and Francesco Giavazzi, University of Chicago Press.

Rodrik, Dani (1998) Why Do More Open Economies Have Bigger Governments? *Journal of Political Economy*, 106(5), pp. 997-1032.

Schubert, Stefan F., and Stephen J. Turnovsky (2002) The Dynamics of Temporary Policies in a Small Open Economy. *Review of International Economics* 10(4), 604-622.

Shimer, Robert (2011) Wage and Price Rigidities. Mimeo. `http://www.eief.it/files/2011/03/wage-price-rigidities.pdf`

Stockman Alan C. and Linda L. Tesar (1995) Tastes and Technology in a Two-Country Model of the Business Cycle: Explaining International Comovements. *American Economic Review* 85(1), pp. 168-185.

Wacziarg, Romain and Jessica S. Wallack (2004) Trade Liberalization and Intersectoral Labor Movements. Journal of International Economics, 64, pp. 411-439.

Yang Shu-Chun Susan (2007) Tentative Evidence of Tax Foresight. *Economics Letters*, 96, pp. 30-7.